

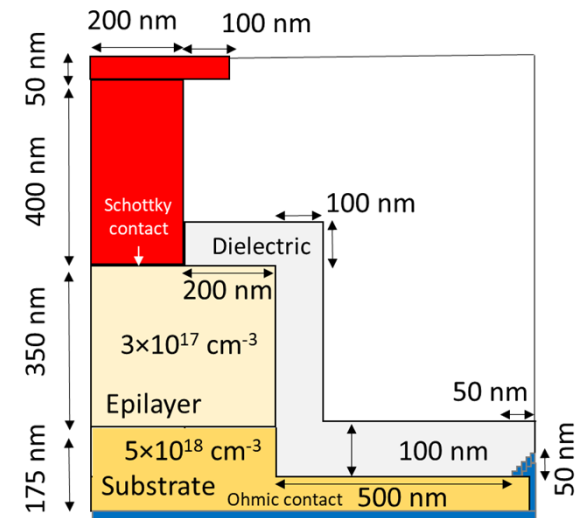
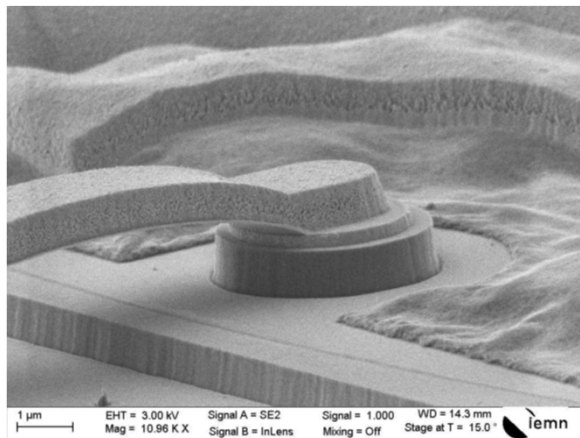
# Modelling of Schottky-Barrier Diodes Operating under Strong Reverse-Bias Conditions

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## OUTLINE

- Introduction
- Ideal full-depletion leakage current model
- Monte Carlo model
- Results
  - ⇒ 1D simulations
  - ⇒ 2D simulations
- Conclusions



# Introduction

THz frequency multipliers based on Schottky-barrier diodes (SBDs): **GaAs** → **GaN**

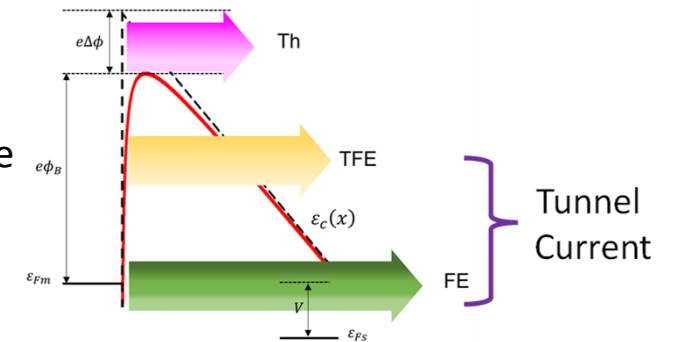
Correct modelling of reverse current → essential to predict their breakdown

**Low-injection conditions** (low voltage, low doping)

Full Depletion (FD) approximation valid → analytical estimation of the barrier profile



Ideal current components: thermionic emission and tunneling currents

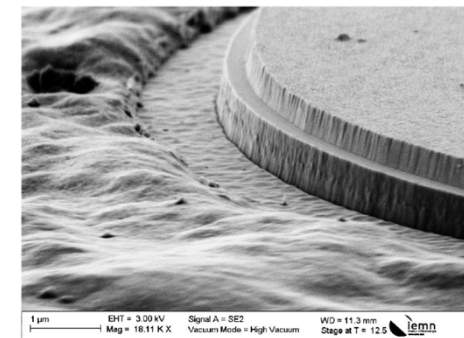


**High-injection conditions** (strong reverse bias, contact edge, inhomogeneities)

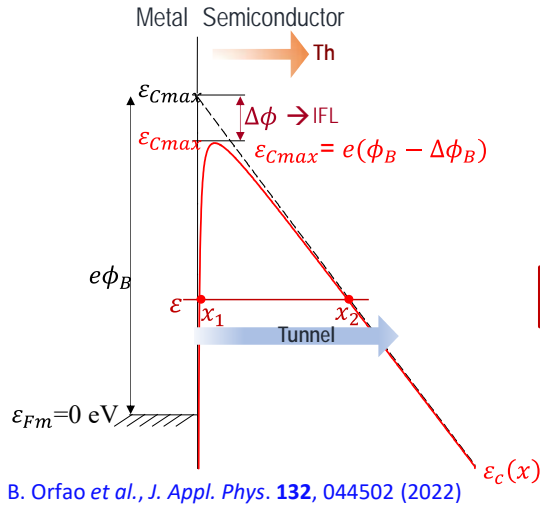
barrier profile → self-consistently calculated with carrier concentration

simulation of carrier transport → electron and hole **impact ionization**

**This work:** analysis of **GaN SBDs** by means of Monte Carlo simulations where all the involved physical effects are taken into account



# Ideal full-depletion leakage current model



$$\varepsilon_c(x) = e\phi_B - e \underbrace{\left[ \frac{2eN_D}{\varepsilon_S} (V_B - V) \right]^{1/2}}_{E_{max}} x + \frac{e^2 N_D x^2}{2\varepsilon_S} - \frac{e^2}{16\pi\varepsilon_S x}$$

↑ doping effect
 ↑ image-charge effect

Parameters:  $\phi_B$ ,  $\varepsilon_S$ ,  $N_D$  and  $m^*$

$$J(\varepsilon)d\varepsilon = -eN(\varepsilon)T_C(\varepsilon)d\varepsilon$$

WKB approximation

$$N(\varepsilon) = \frac{A^*T}{ek_B} \ln \left[ 1 + \exp \left( -\frac{\varepsilon - \varepsilon_F}{k_B T} \right) \right] \Rightarrow \cong \exp \left( -\frac{\varepsilon - \varepsilon_{Fm}}{k_B T} \right) \quad \text{for } \varepsilon - \varepsilon_F \gg k_B T$$

$$T_C(\varepsilon) = \exp \left( -\frac{2}{\hbar} \int_{x_1}^{x_2} \sqrt{2m^*[\varepsilon_C(x) - \varepsilon]} dx \right)$$

$N(\varepsilon)$ : number of electrons per unit area per unit time incident on the barrier per unit energy normal to the barrier

Thermionic emission

$$\varepsilon > \varepsilon_{Cmax} \Rightarrow T_C(\varepsilon) = 1$$

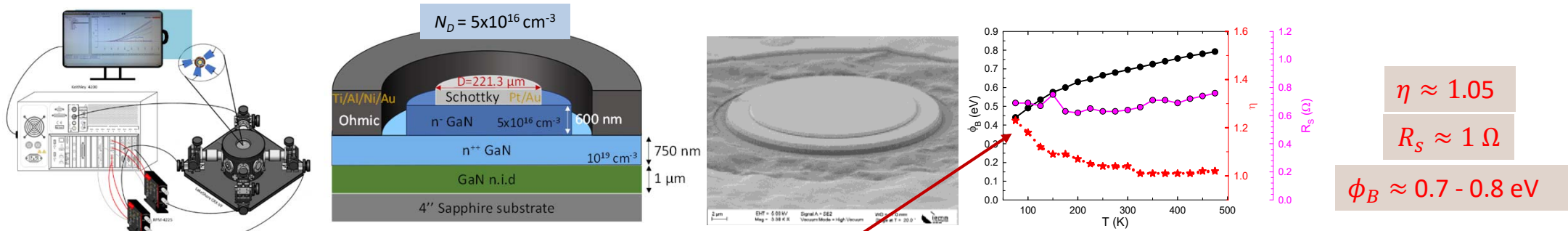
$$J_{Th} = A^*T^2 \exp \left( -\frac{\varepsilon_{Cmax}}{k_B T} \right) \left[ \exp \left( \frac{e(V - J_{th}SR_S)}{\eta k_B T} \right) - 1 \right]$$

Tunneling current

$$\varepsilon < \varepsilon_{Cmax} \Rightarrow 0 < T_C(\varepsilon) < 1$$

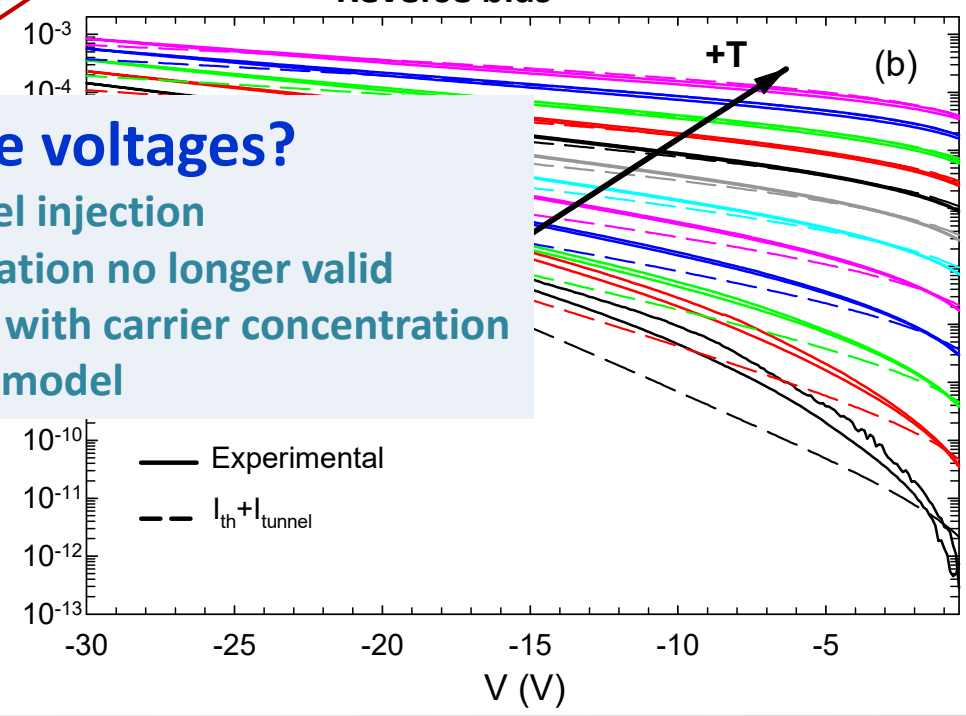
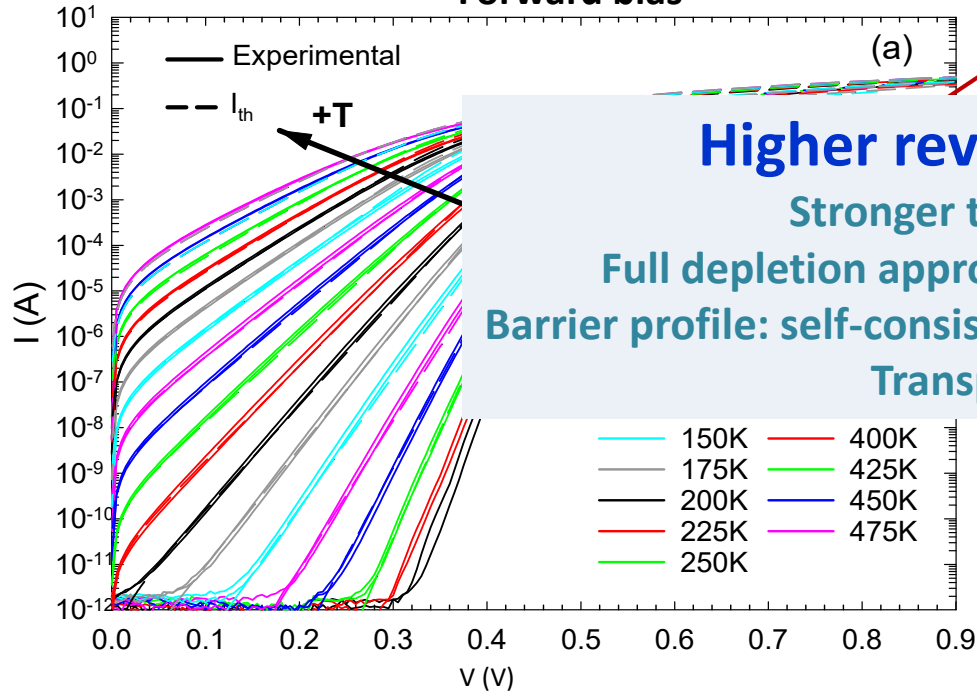
$$J_{tunnel} = e \int_{\varepsilon_{min}}^{\varepsilon_{Cmax}} N(\varepsilon) \cdot T_C(\varepsilon) d\varepsilon$$

# Ideal full-depletion leakage current model: experimental validation



Forward bias

Reverse bias



**Higher reverse voltages?**  
 Stronger tunnel injection  
 Full depletion approximation no longer valid  
 Barrier profile: self-consistent with carrier concentration  
 Transport model

# Monte Carlo model: transport

## Electrons

$\Gamma_1$ -U- $\Gamma_3$  non-parabolic spherical valleys

ionized impurities, polar and nonpolar optical phonons, acoustic phonons, intervalley

S. García et. al. , *J. Appl. Phys.* **115**. 044510 (2014)

**Time step:** 0.2 - 2.5 fs

**Mesh size:** 0.5 - 5 nm

## Holes

heavy, light and split-off bands

ionized impurities, nonpolar optical and acoustic phonons, and polar optical phonons; all including inter-valley transitions

S. Chen and G. Wang, *J. Appl. Phys.* **103**, 023703 (2008)

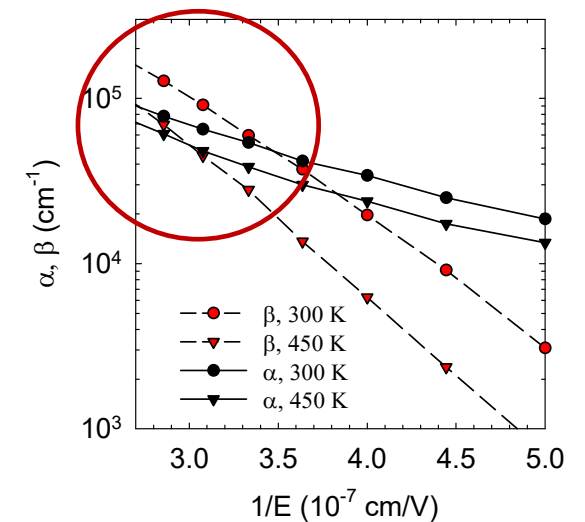
## Impact Ionization

Keldysh approach

$$P(\varepsilon) = S \left( \frac{\varepsilon - \varepsilon_{th}}{\varepsilon_{th}} \right)^2 \quad \varepsilon > \varepsilon_{th}$$

$$P(\varepsilon) = 0 \quad \varepsilon < \varepsilon_{th}$$

	Electrons	Holes
$\varepsilon_{th}$ (eV)	3.0	3.0
$S$ ( $10^{12} \text{ s}^{-1}$ )	5.0	25.0



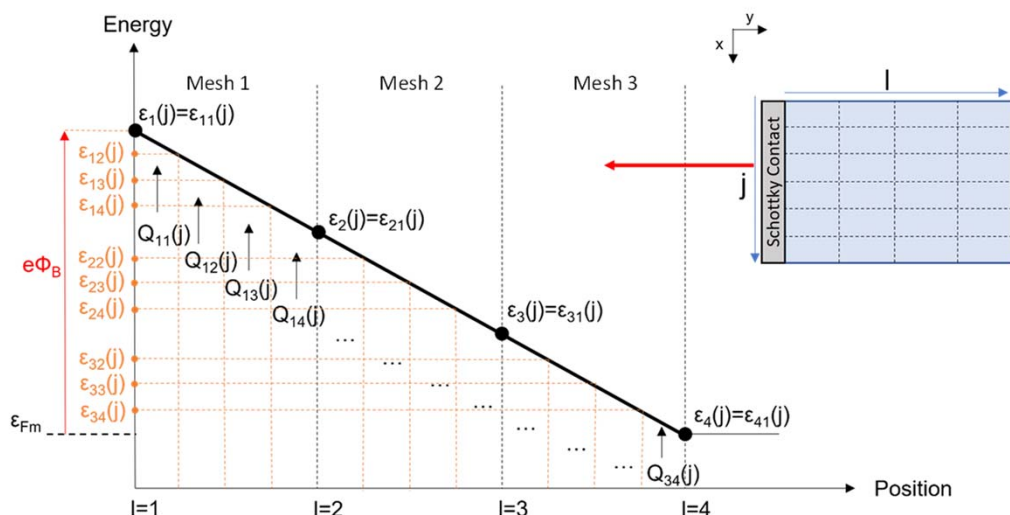
# Monte Carlo model: tunnel injection

## Self consistency

Barrier profile obtained from the self-consistent solution of Poisson's equation

## MC 2-D

Energy discretization linked to the spatial mesh used to solve Poisson's equation





$$J(\epsilon)d\epsilon = -eN(\epsilon)T_C(\epsilon)d\epsilon$$

$$N(\epsilon) = \frac{A^*T}{ek_B} \ln \left[ 1 + \exp \left( -\frac{\epsilon - \epsilon_F}{k_B T} \right) \right]$$

$$T_C(\epsilon) = \exp \left( -\frac{2}{\hbar} \int_{x_1}^{x_2} \sqrt{2m^*[\epsilon_C(x) - \epsilon]} dx \right)$$

$$Q_{ij}(j) = \Delta t e N(\epsilon_{ij}(j)) T_C(\epsilon_{ij}(j)) \Delta \epsilon_{ij}(j)$$

**MC**  Number of injected carriers  
 Mesh and energy interval

## MC 1-D

Energy discretization independent of the spatial mesh. Barrier lowering taken into account

## Simulations

Without tunnel injection  
 With and without impact ionization (II)  
 Estimation of the current with the FD approach

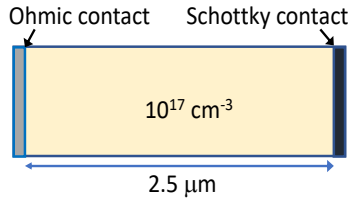
Current evaluated by counting particles at the Schottky contact

Electrons: tunnel injection Holes: impact ionization

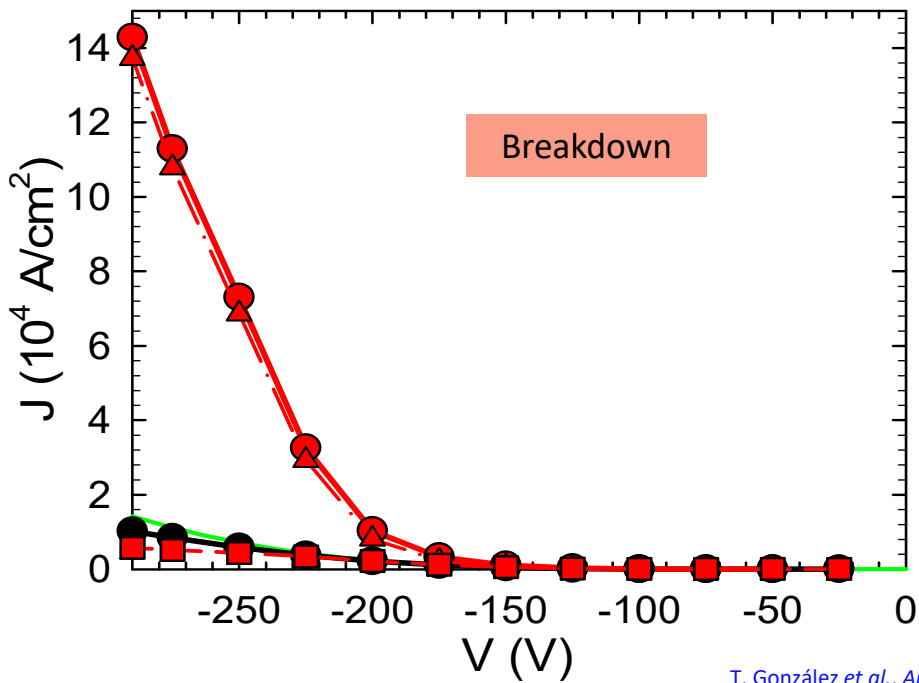
# Results: 1D simulations (diode 1)

## Low-doped diode

$T=450\text{K}$   
 $\phi_B = 0.935\text{ eV}$

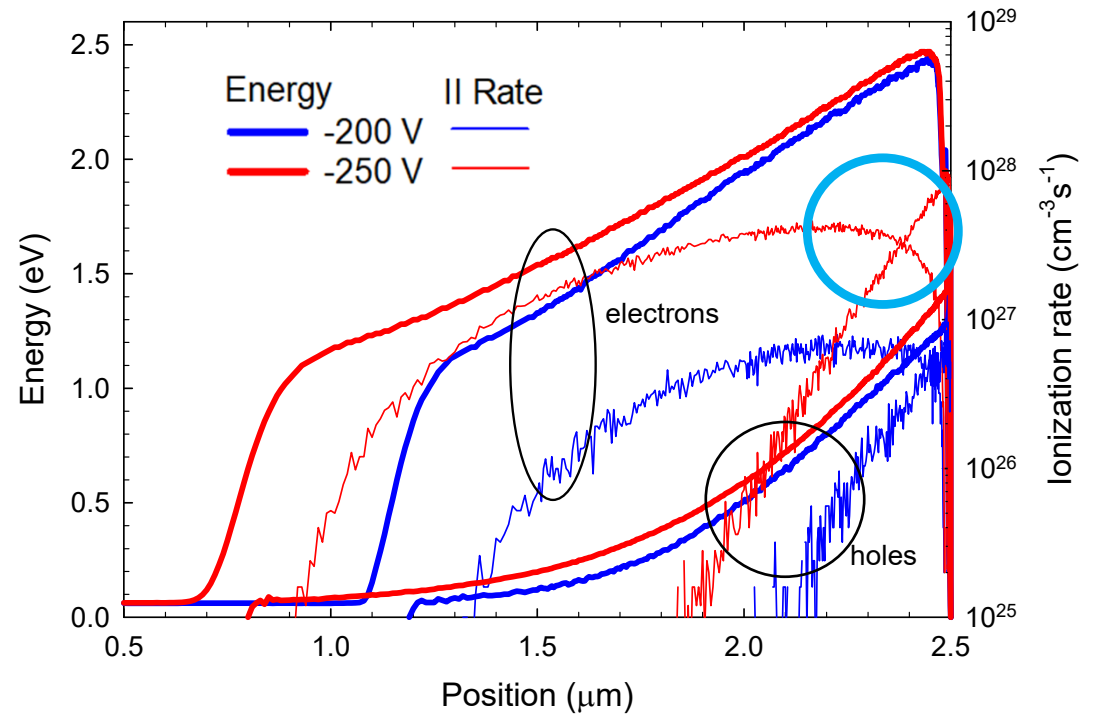


low tunnel injection



T. González et al., *Appl. Phys. Express* 16, 024003 (2023)

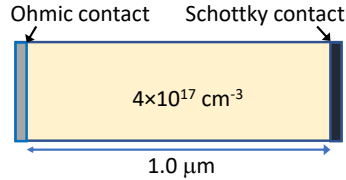
## Energy and ionization rate



# Results: 1D simulations (diode 2)

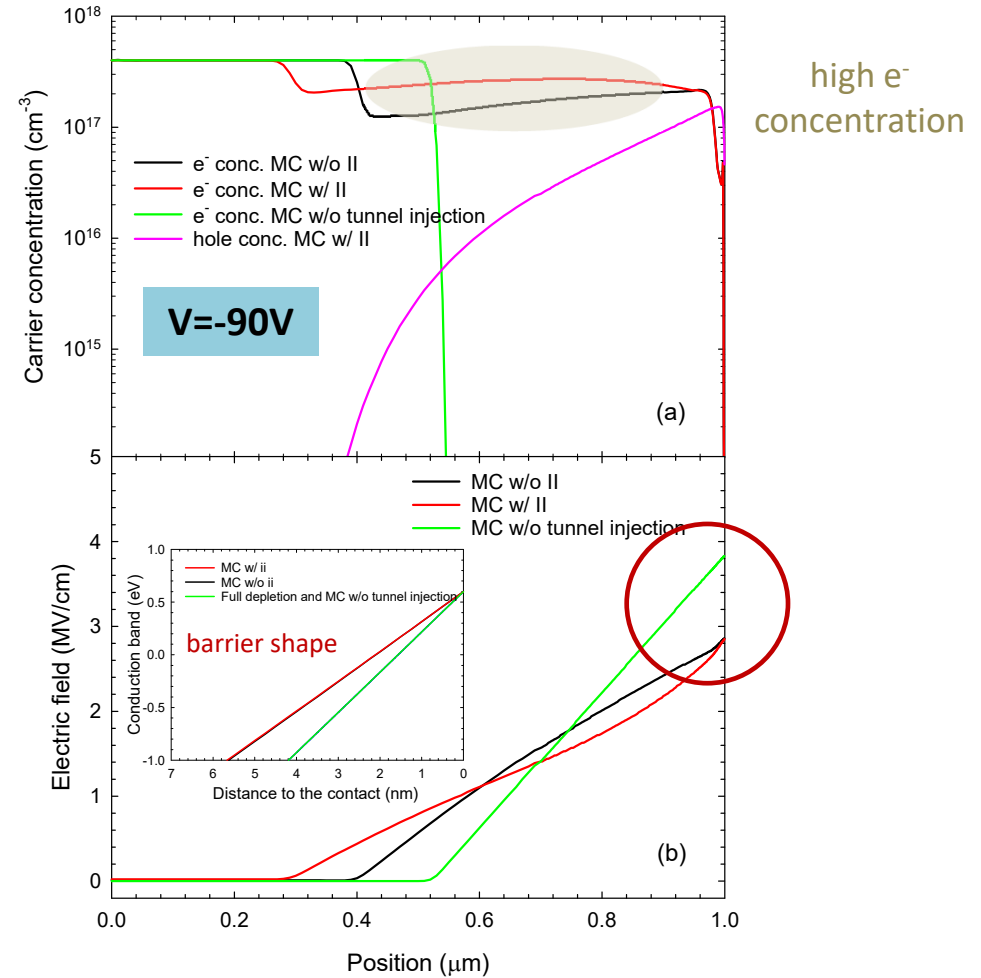
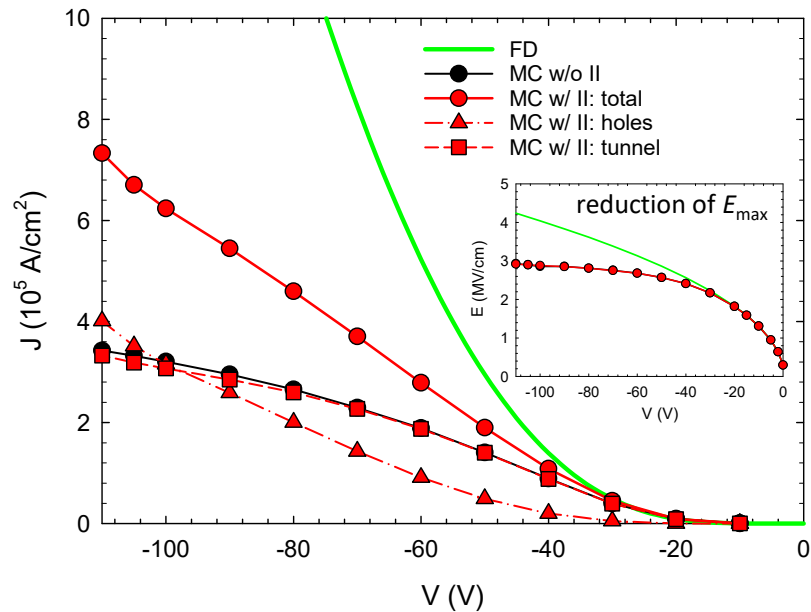
## Highly-doped diode

$T=300\text{K}$   
 $\phi_B = 0.6\text{ eV}$



**strong tunnel injection**

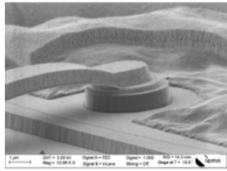
## I-V



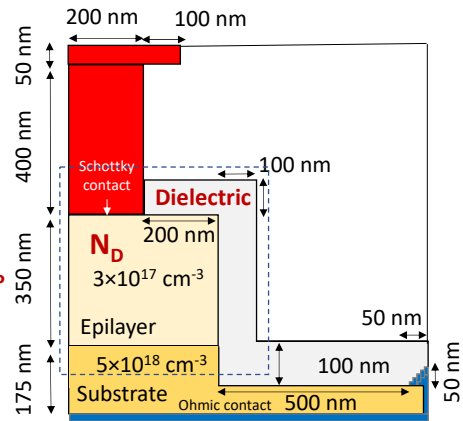


# Results: 2D simulations (without impact ionization) - passivation dielectric

small-size diodes  
for THz frequency multipliers

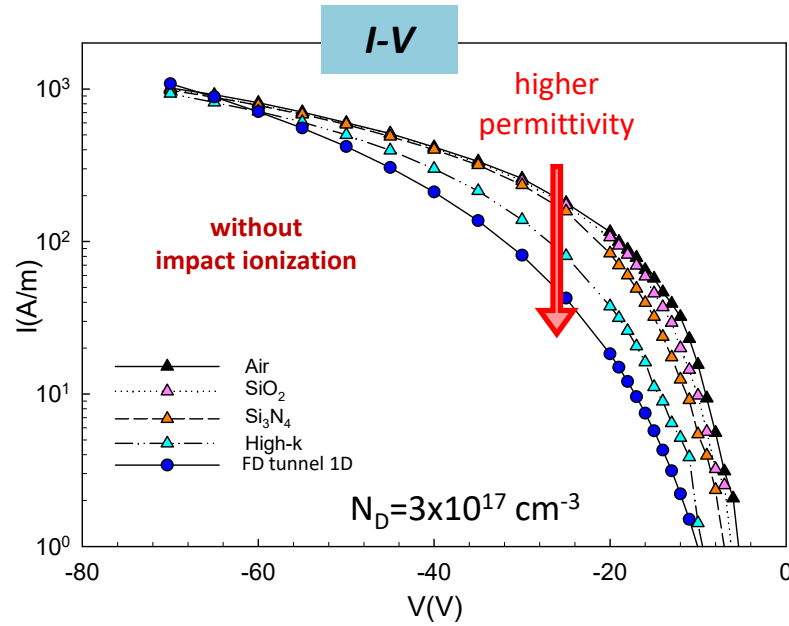


$T=300K$   
 $\phi_B = 0.5 eV$

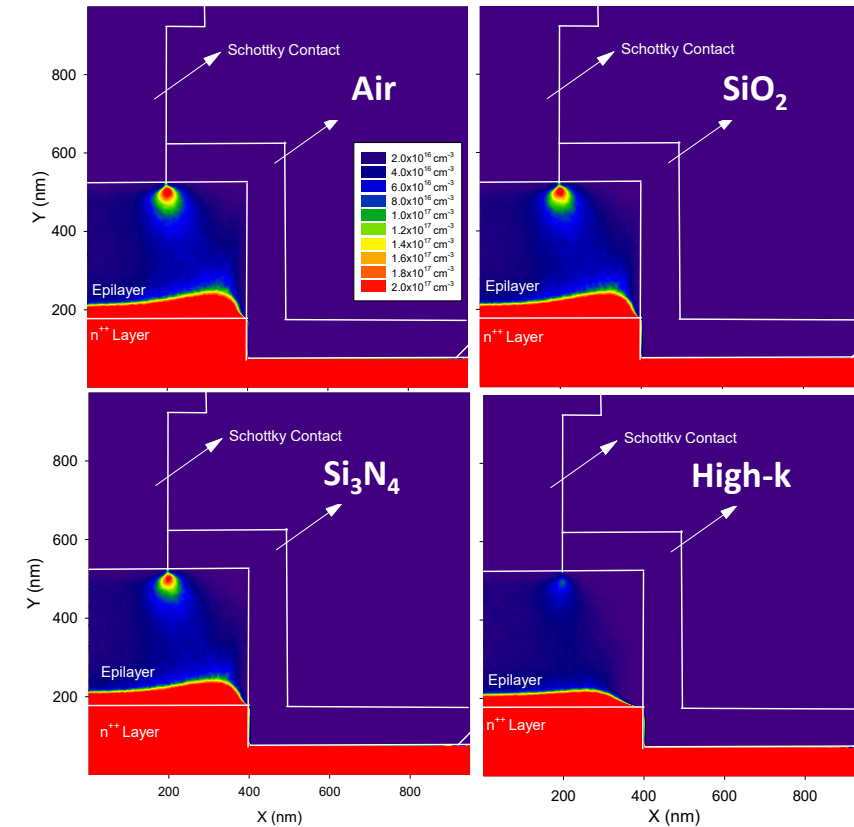


## 2D effects

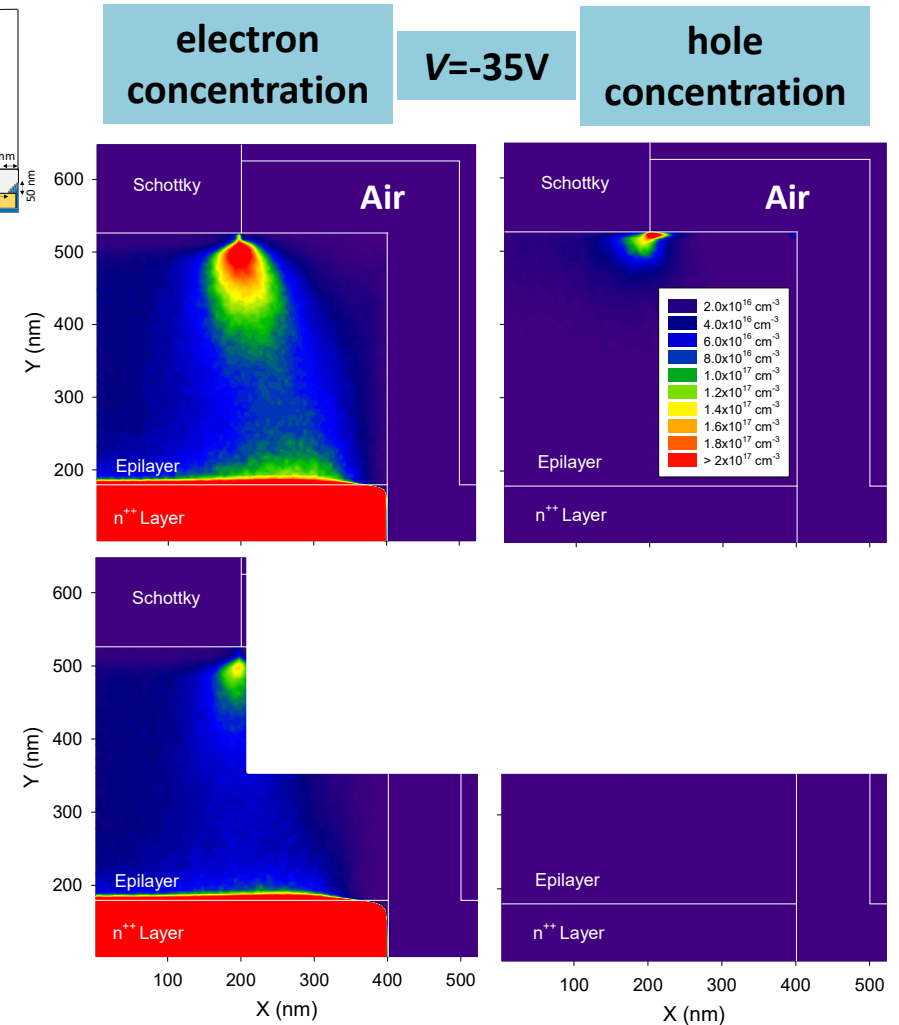
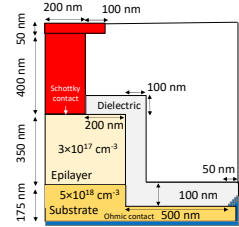
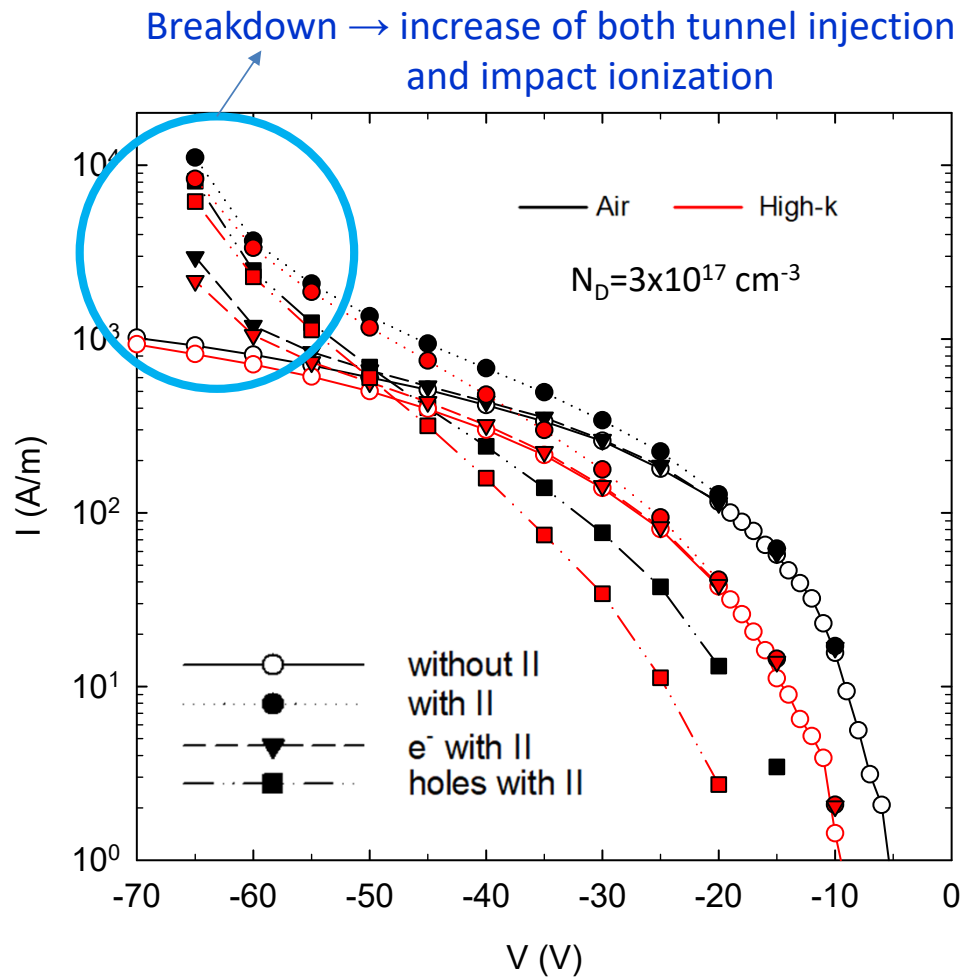
higher electric field at the contact edge  
↓  
current crowding  
smoothed by dielectrics with high-k



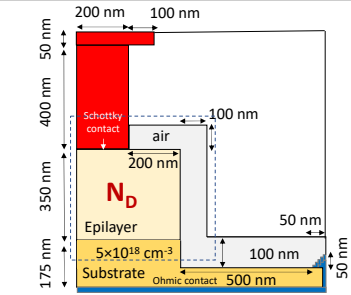
## electron concentration $V=-30V$



# Results: 2D simulations (with impact ionization) - breakdown



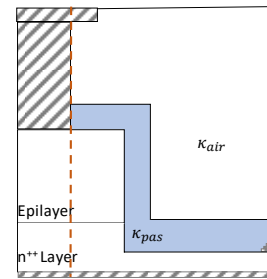
# Results: 2D simulations (with impact ionization) - epilayer doping



$W_{EP} = 350 \text{ nm}$

higher doping

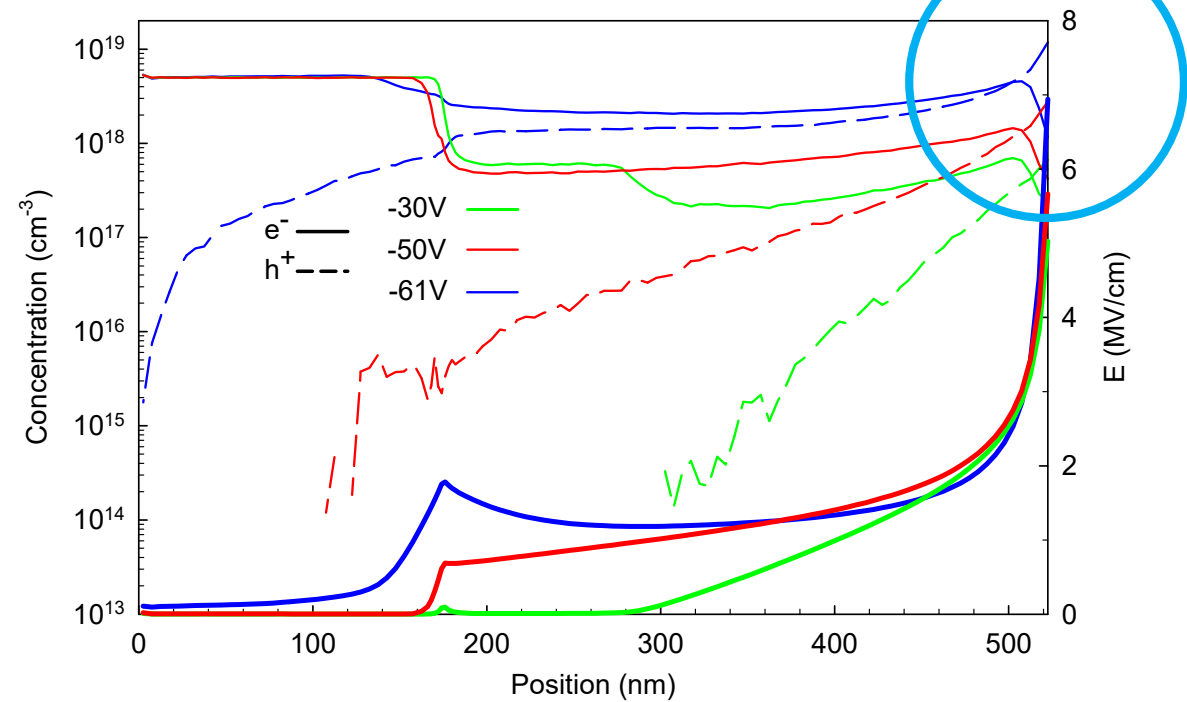
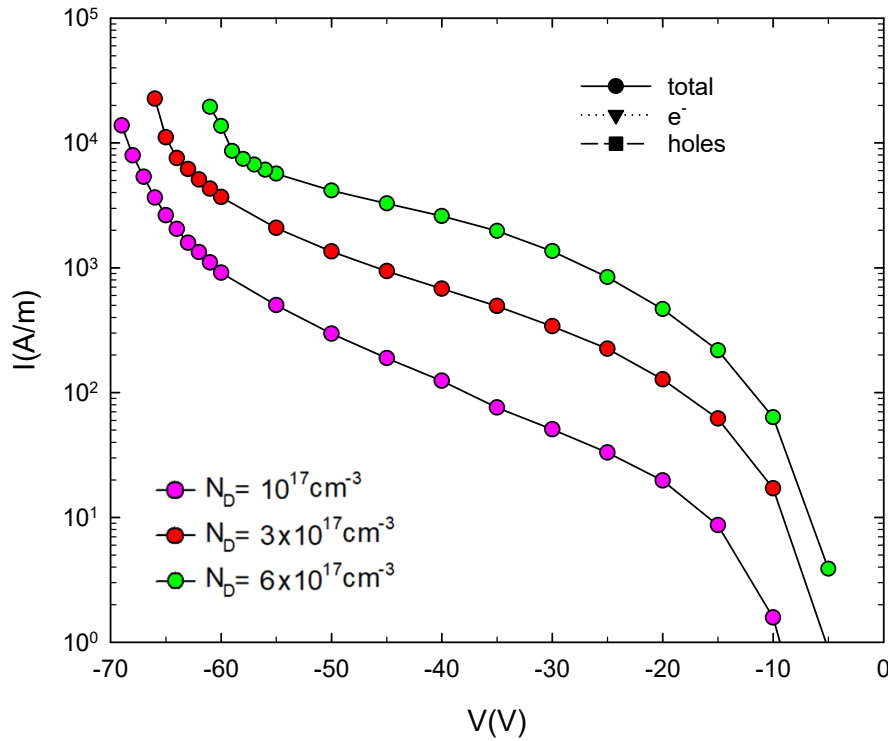
lower breakdown voltage



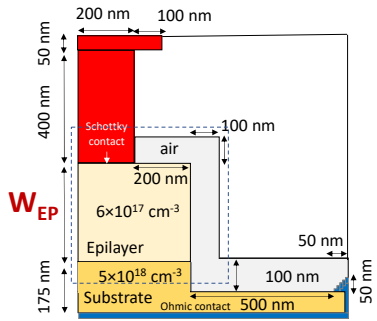
$N_D = 6 \times 10^{17} \text{ cm}^{-3}$

Breakdown

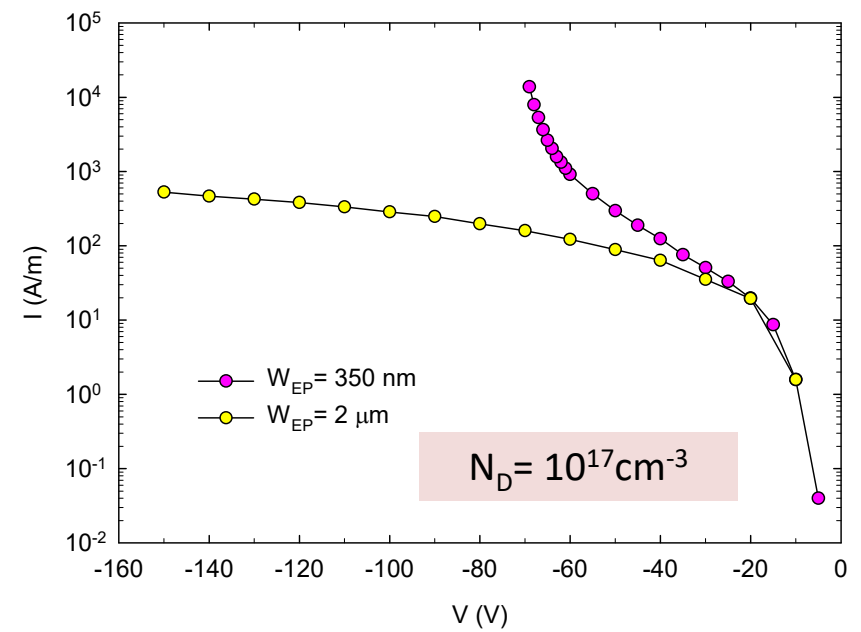
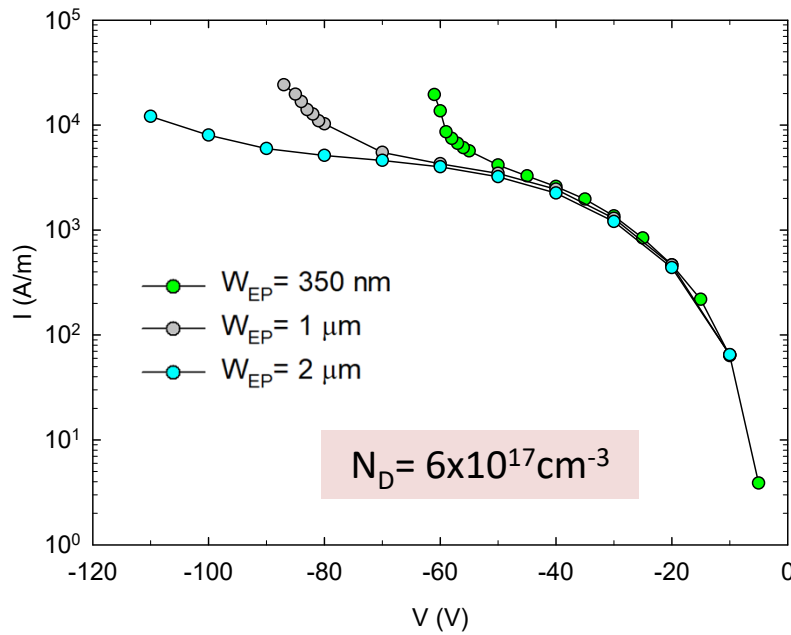
feedback impact ionization  $\leftrightarrow$  tunneling  
(more pronounced for higher  $N_D$ )



# Results: 2D simulations (with impact ionization) - epilayer thickness



Thicker epilayer  
 ↓  
 higher breakdown voltage  
 and softer breakdown  
  
 Breakdown  
 ↓  
 impact ionization



## Conclusions

- Correct prediction of the I-V curves of SBDs at high applied voltages in reverse bias → **shape of the barrier** and associated tunnel injection **self-consistently** calculated with **carrier concentration** in the depletion region → accounting for electrons and holes generated **by impact ionization**
- Voltage range at which these effects are relevant and relative influence of tunnel injection and impact ionization → thickness and doping of the epilayer, and barrier height
- Analyzed effects likely to be present in some specific regions of SBDs: **contact edge** or surface inhomogeneities (high current densities and/or electric fields are locally reached)
- Lower doping and higher thickness of the epilayer → higher breakdown voltage

# Acknowledgements

## Thank you!



M. Zaknoue, Y. Cordier (GaN SBDs)



PID2020-115842RB-I00

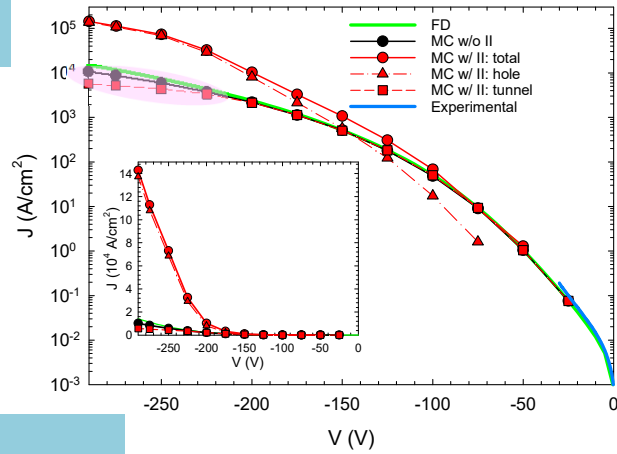


SA254P18

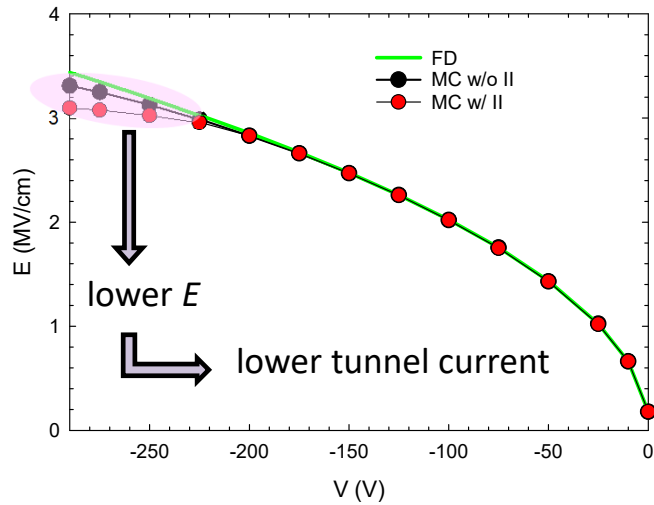


# Results: 1D simulations (diode 1)

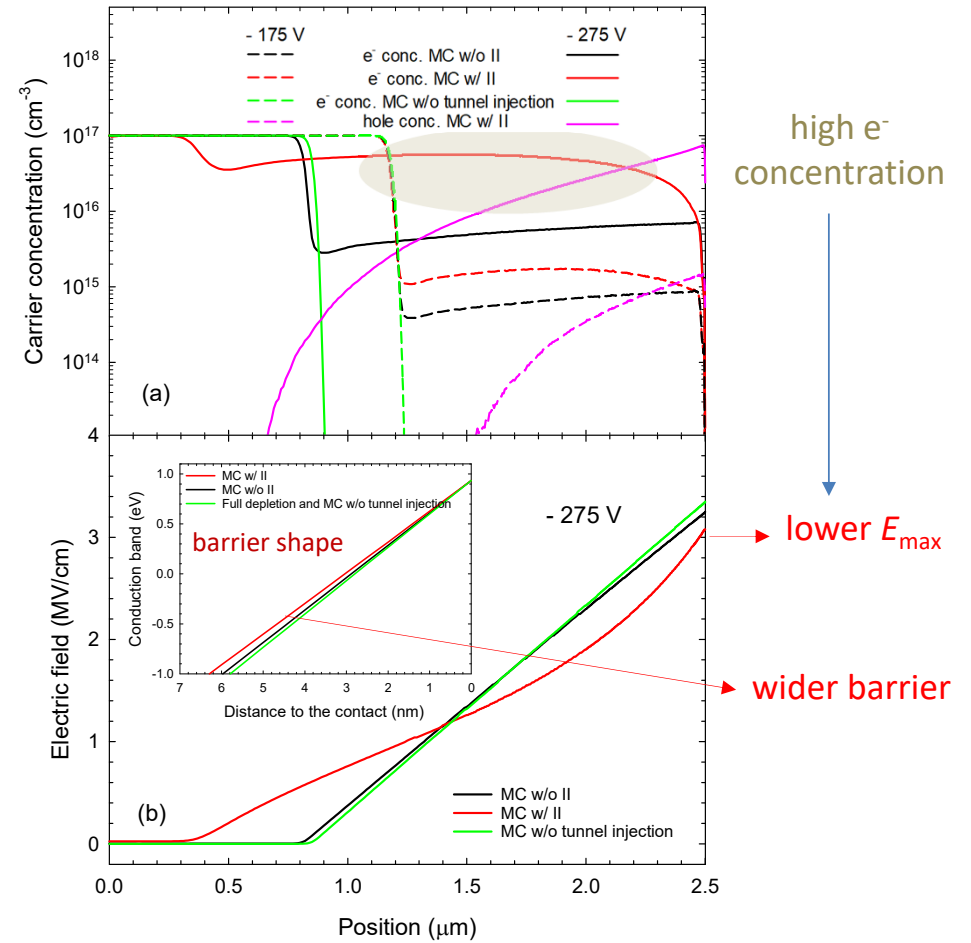
I-V



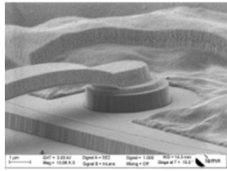
$E_{max}$



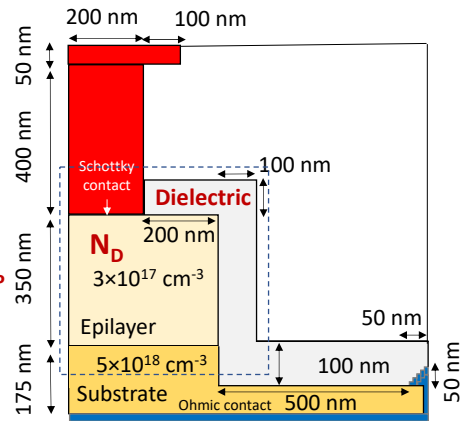
Spatial profiles



# Results: 2D simulations (without impact ionization) - passivation dielectric

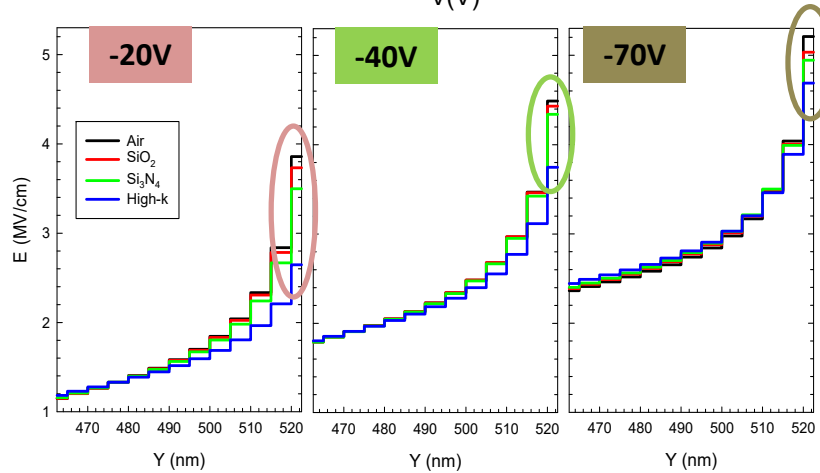
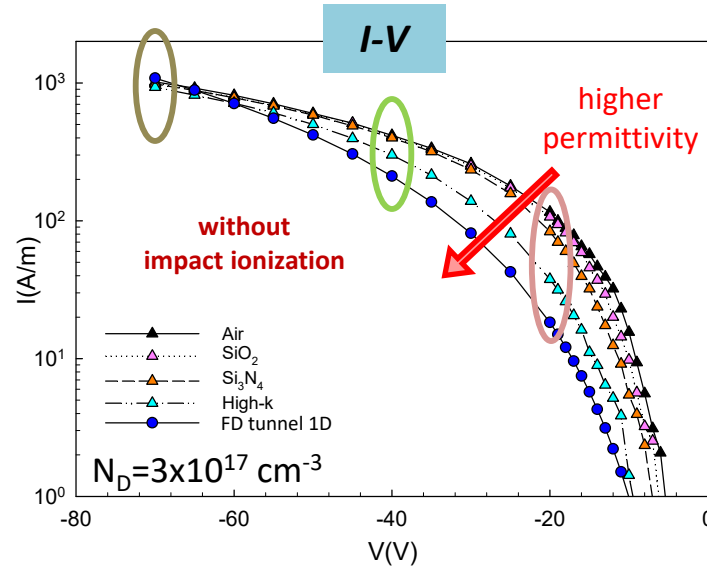


$T=300\text{K}$   
 $\phi_B = 0.5\text{ eV}$

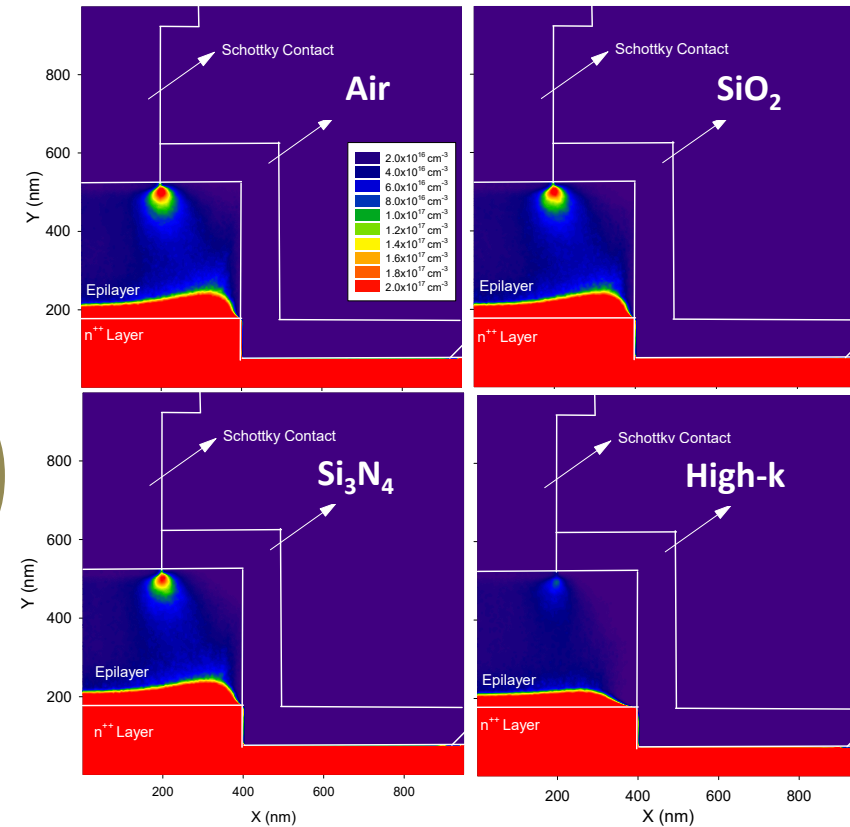


## 2D effects

higher electric field at the contact edge  
↓  
current crowding  
smoothed by dielectrics with high-k



## electron concentration $V=-30\text{V}$

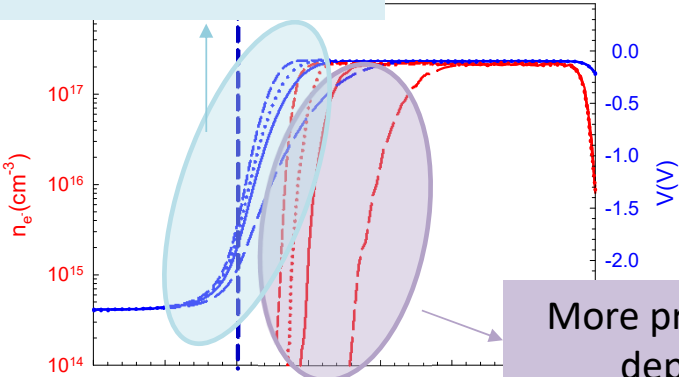




# Influence of Passivation

Stronger penetration of the electric field

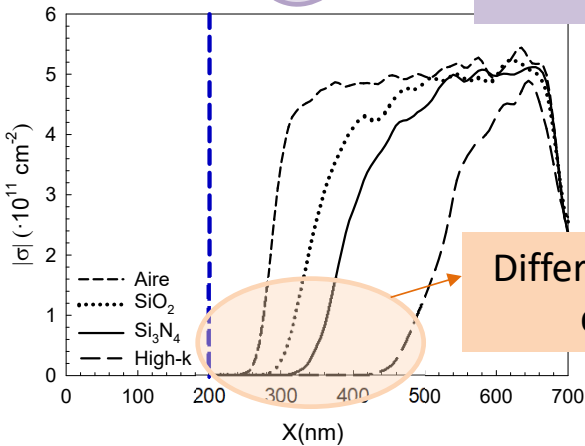
→ Higher  $\kappa_{pas}$



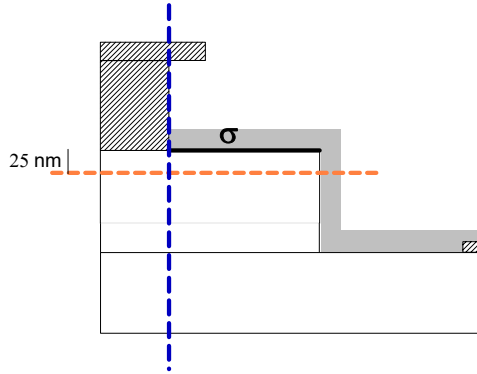
More pronounced depletion

↓  
Higher  $\kappa_{pas}$

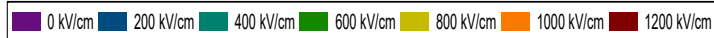
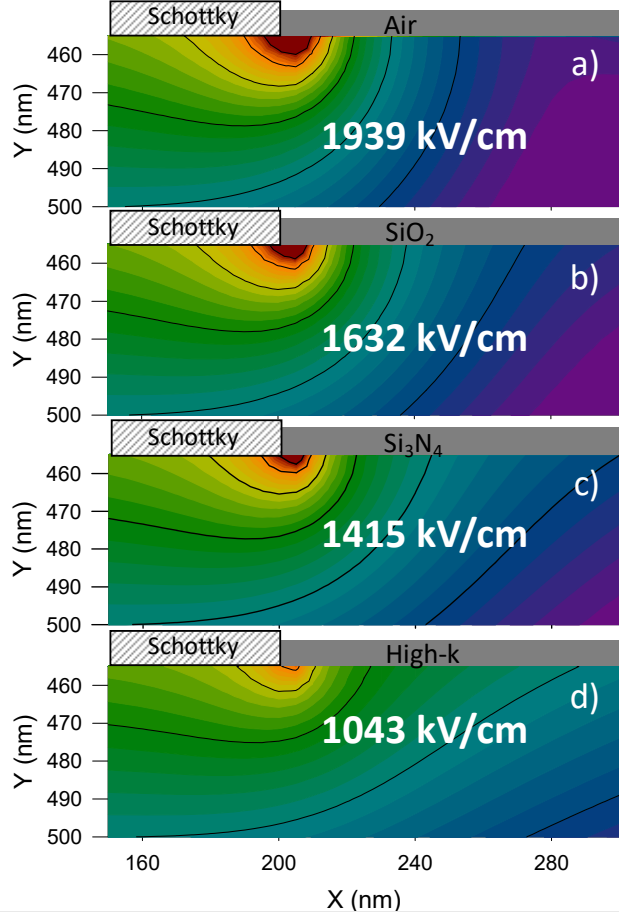
Different due to the depletion



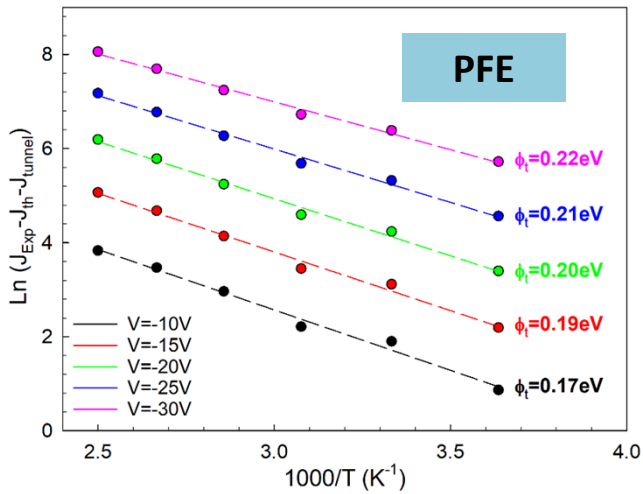
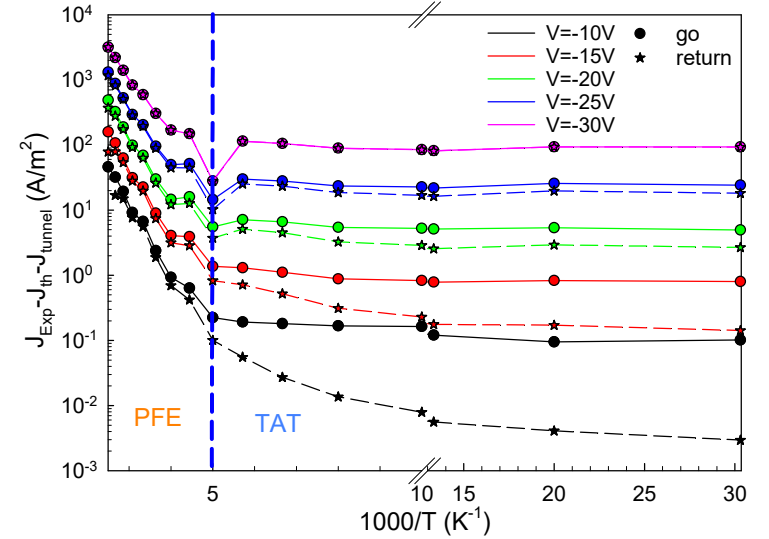
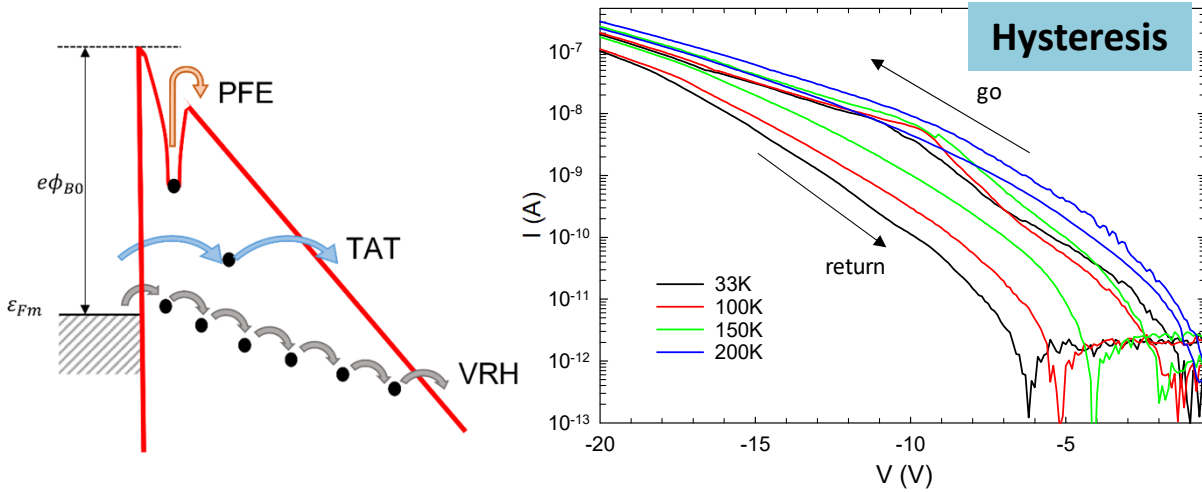
$$V - V_B = -4.1V$$



## Electric Field

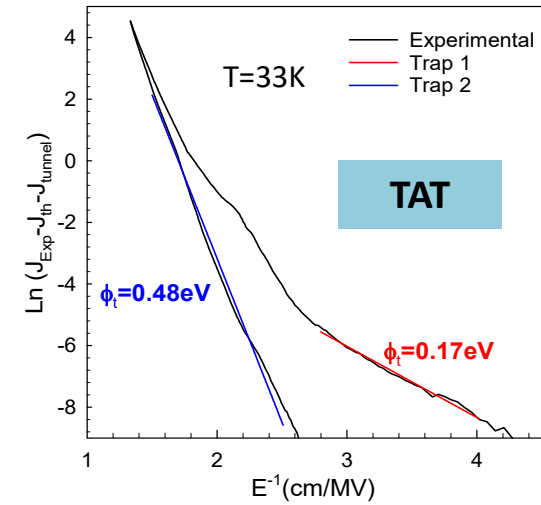


# Leakage current

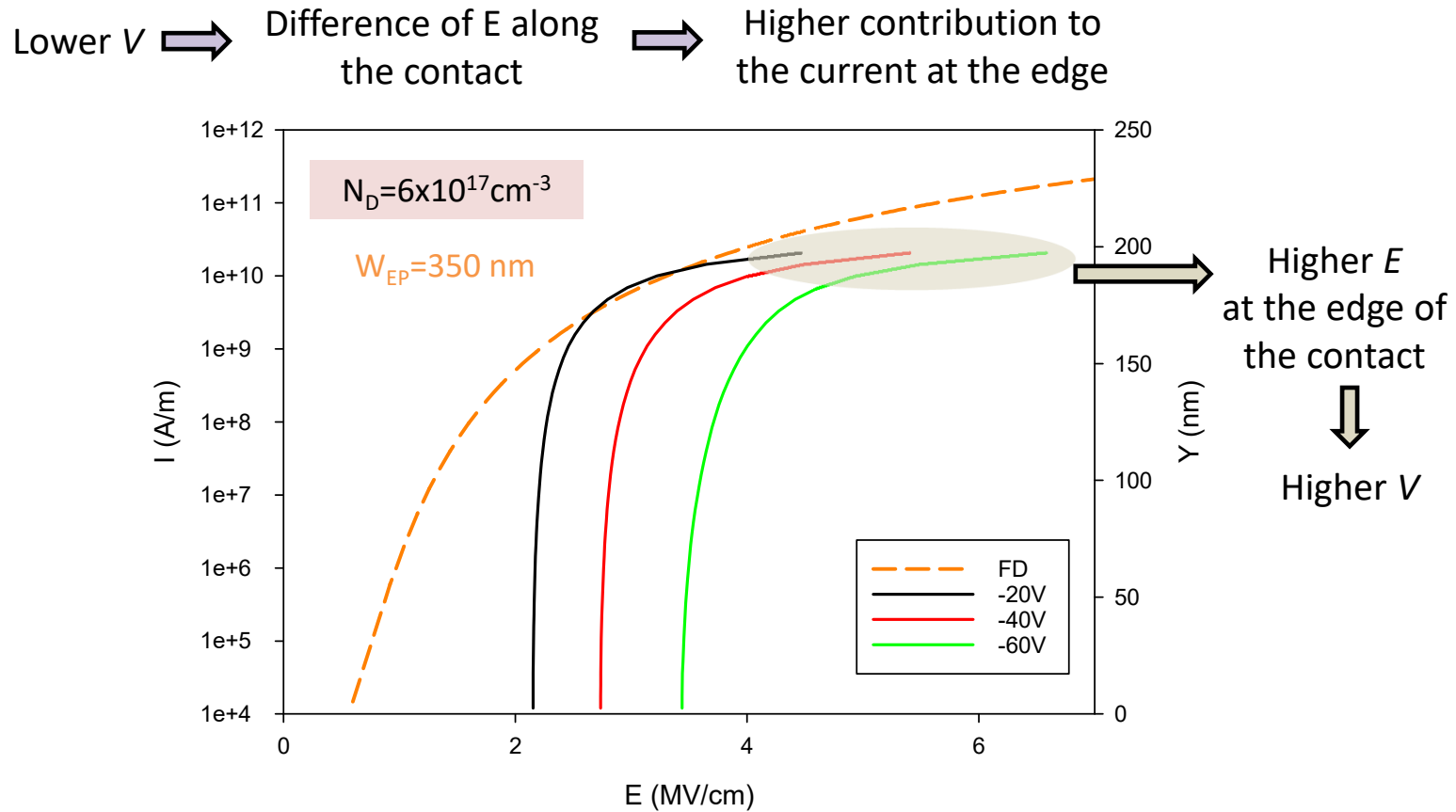


$$J_{TAT} \propto \exp\left(\frac{-4\sqrt{2em^*}\phi_t^{3/2}}{3\hbar E}\right)$$

$$J_{PFE} \propto E \exp\left(\frac{-e(\phi_t - \sqrt{eE/\pi\kappa_{SC}})}{k_B T}\right)$$



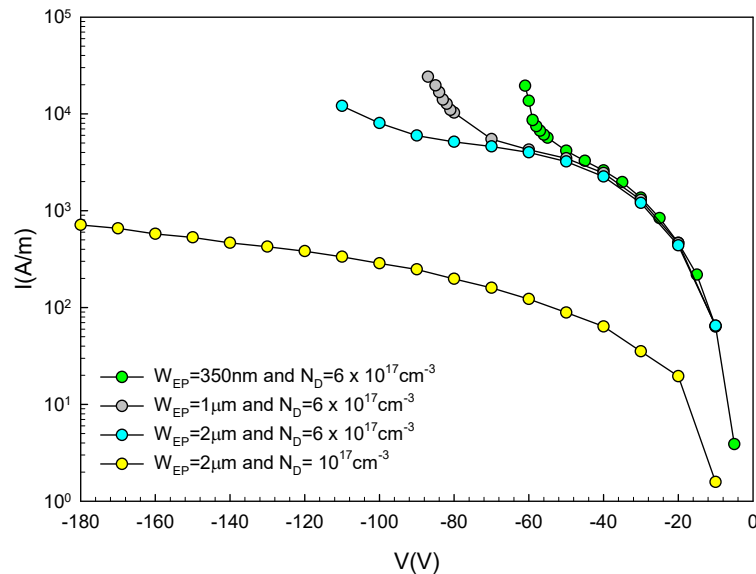
# 2-D effects



# Optimum design

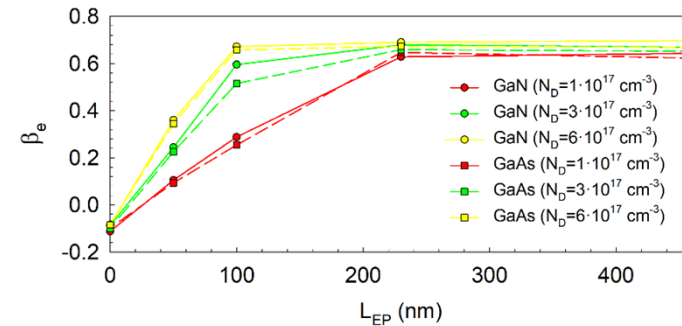
## Improve breakdown

- Passivation material with a **high permittivity**
- Lower **doping**
- High **epilayer thickness**  $\rightarrow$  Higher  $R_s$



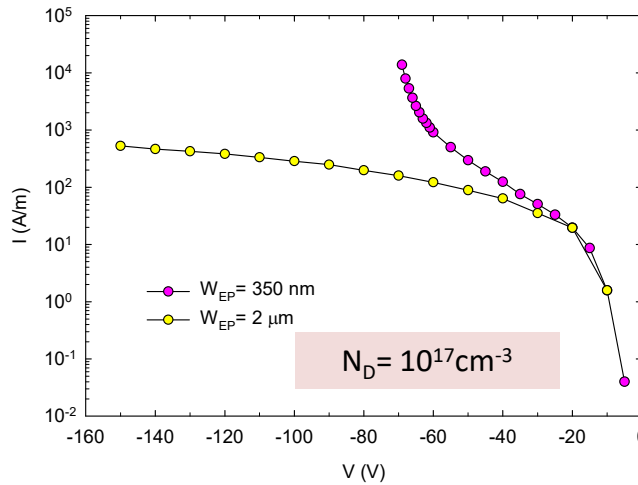
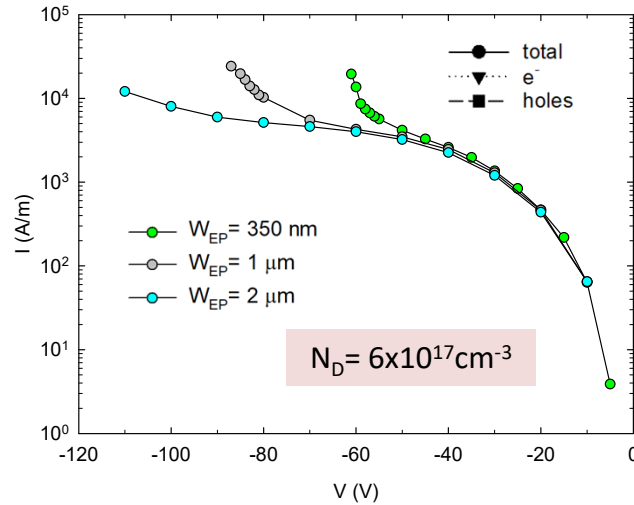
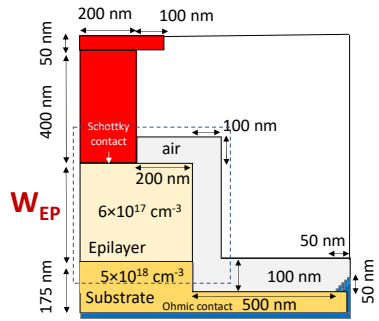
## Reduce capacitance

- A reduction of the **epilayer lateral extension**
- A low **doping** of the epilayer



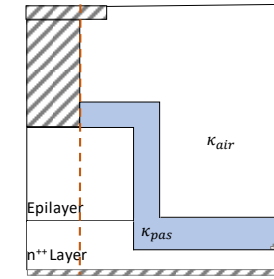
- Passivation material with a **low dielectric constant**
- A reduction of the dielectric **thickness**

# Results: 2D simulations (with impact ionization) - epilayer thickness



Thicker epilayer  
↓  
higher breakdown voltage  
and softer breakdown

$N_D = 6 \times 10^{17} \text{ cm}^{-3}$   
 $W_{EP} = 2 \mu\text{m}$



Breakdown  
↓  
impact ionization

