

# Electro-thermal Properties of 2D Materials

**Zlatan Aksamija**

**Associate Professor, Materials Science and Engineering**

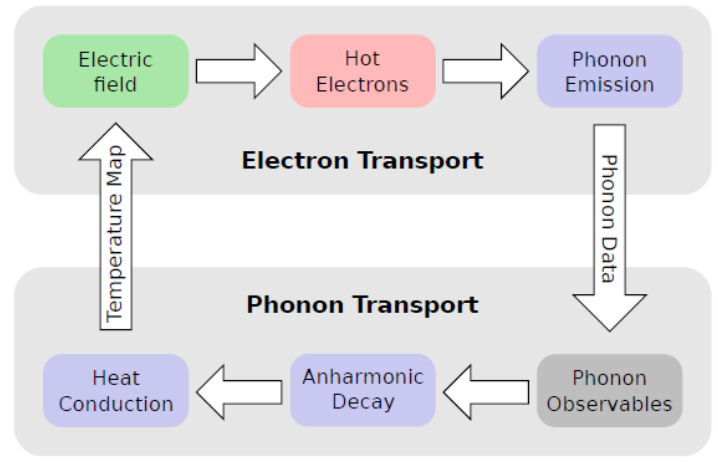
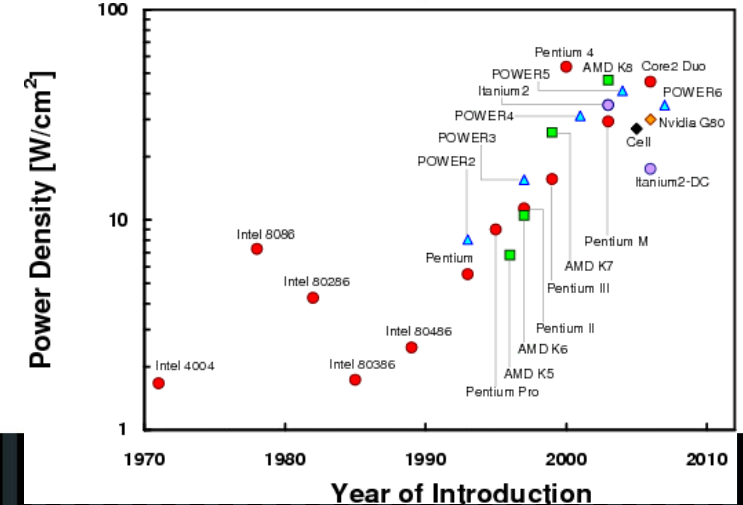
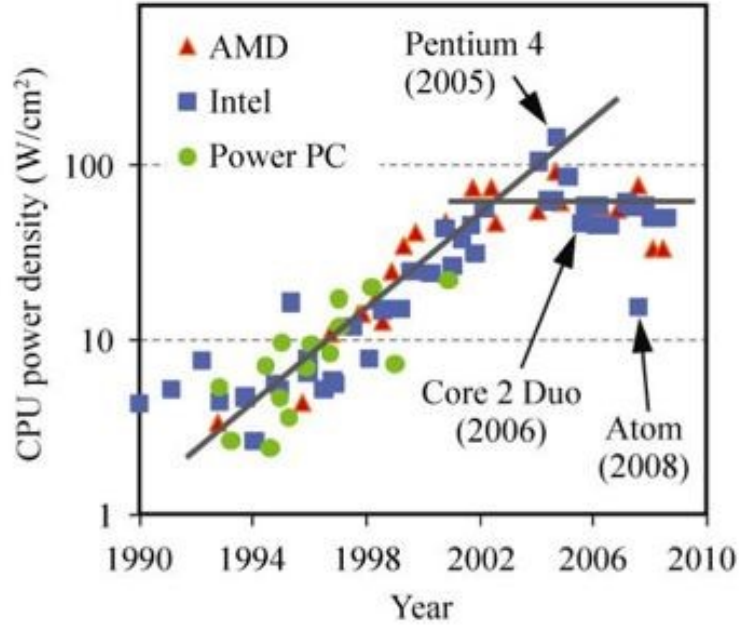
**NanoEnergy Lab, University of Utah**

[zlatan.aksamija@utah.edu](mailto:zlatan.aksamija@utah.edu)

<https://nanoenergy.mse.utah.edu>



# Heat dissipation: a bottleneck to scaling



Hot Spot

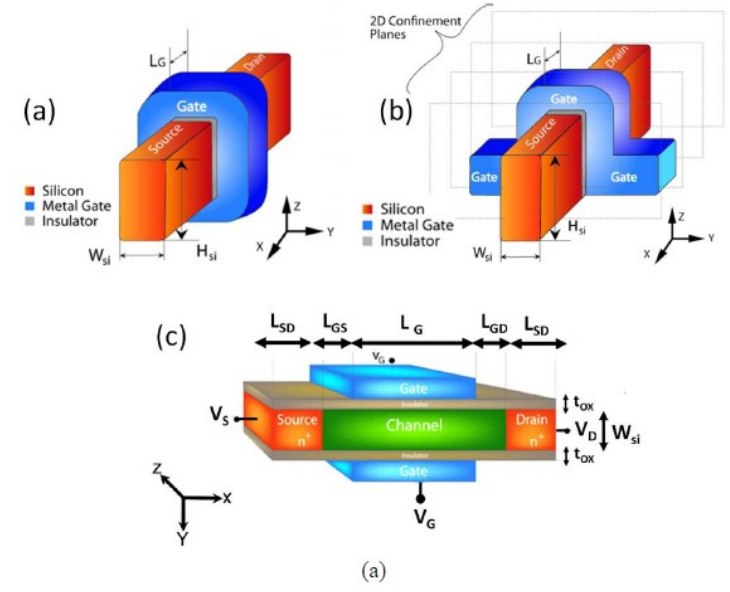
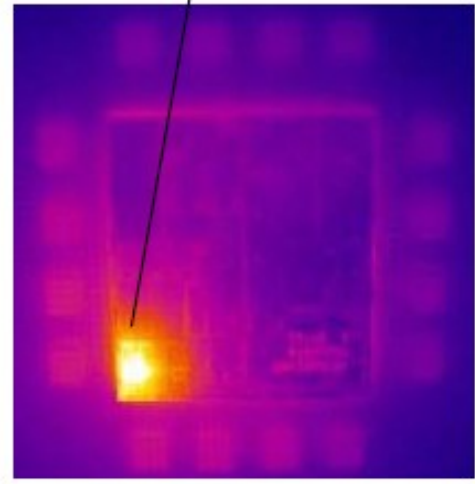
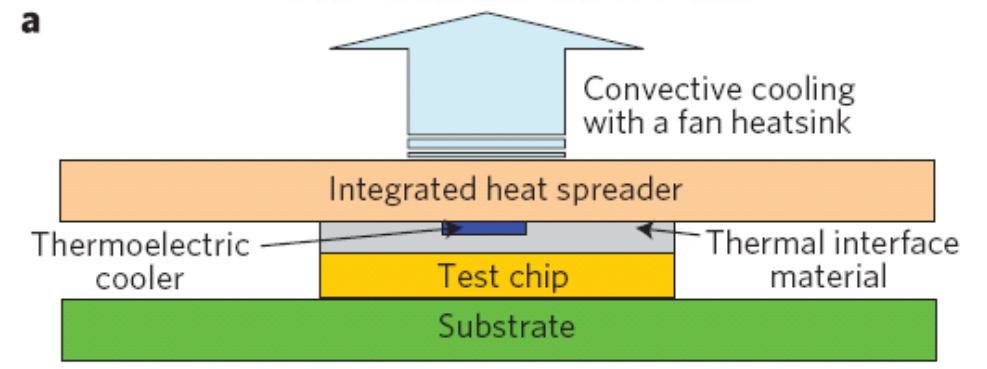


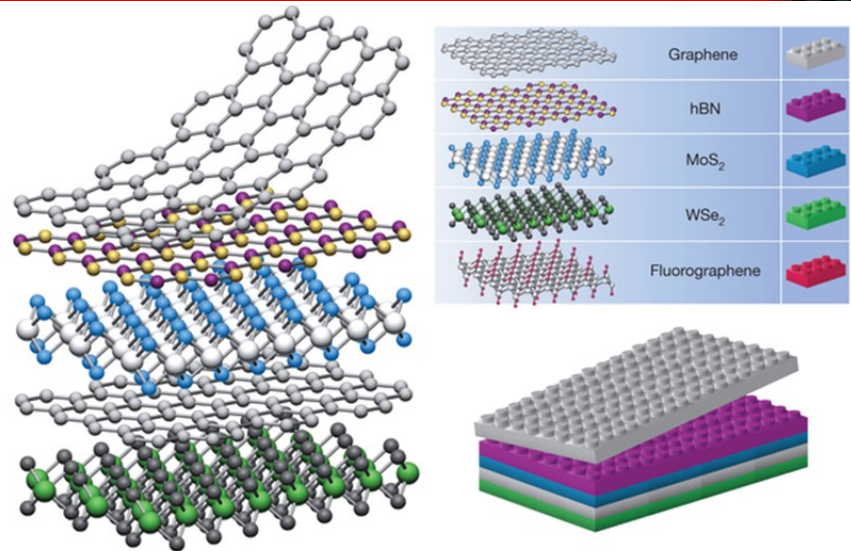
Fig. 4: Schematic of DG, TG and GAA.



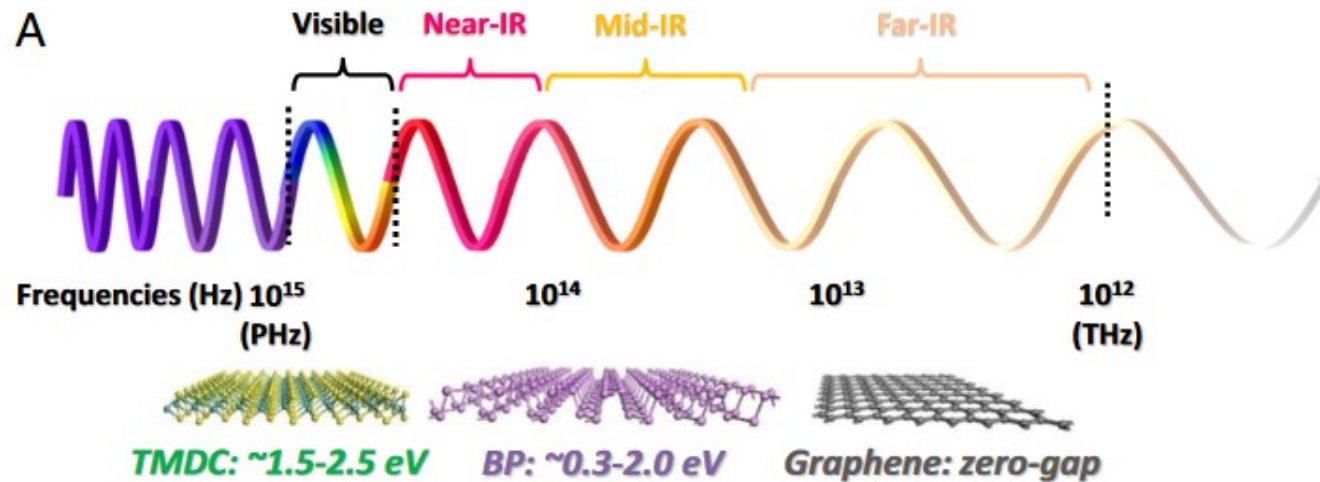
Chowdhury et al., Nature Nano. 4, 235 (2009)



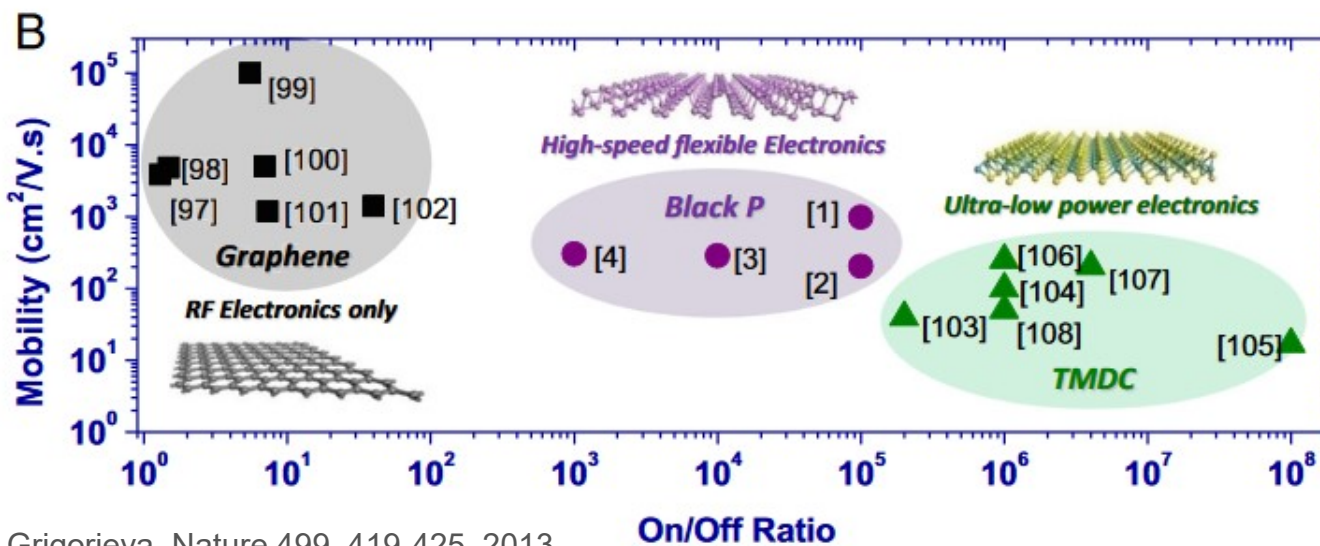
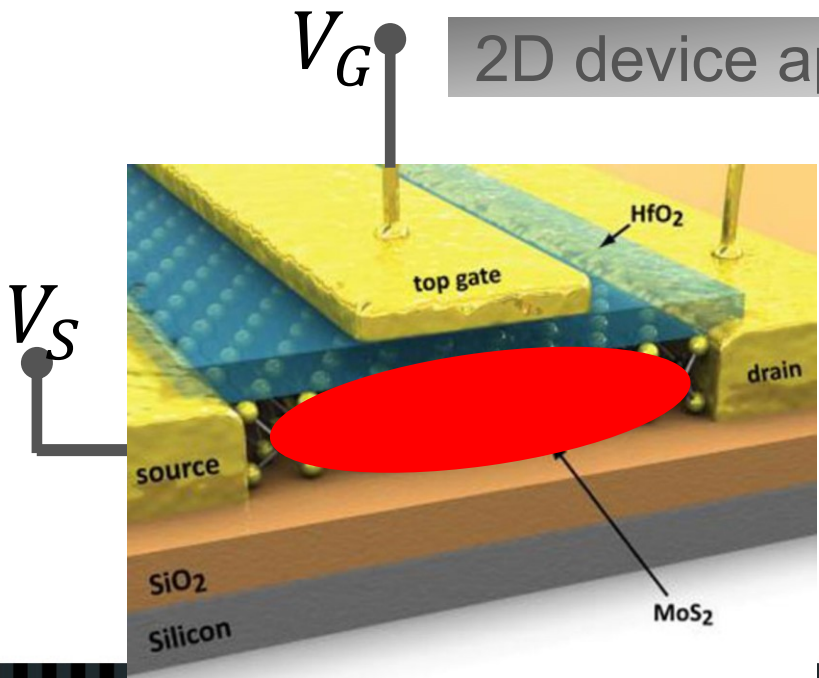
# 2D Materials "lasagna"



# Optoelectronic applications

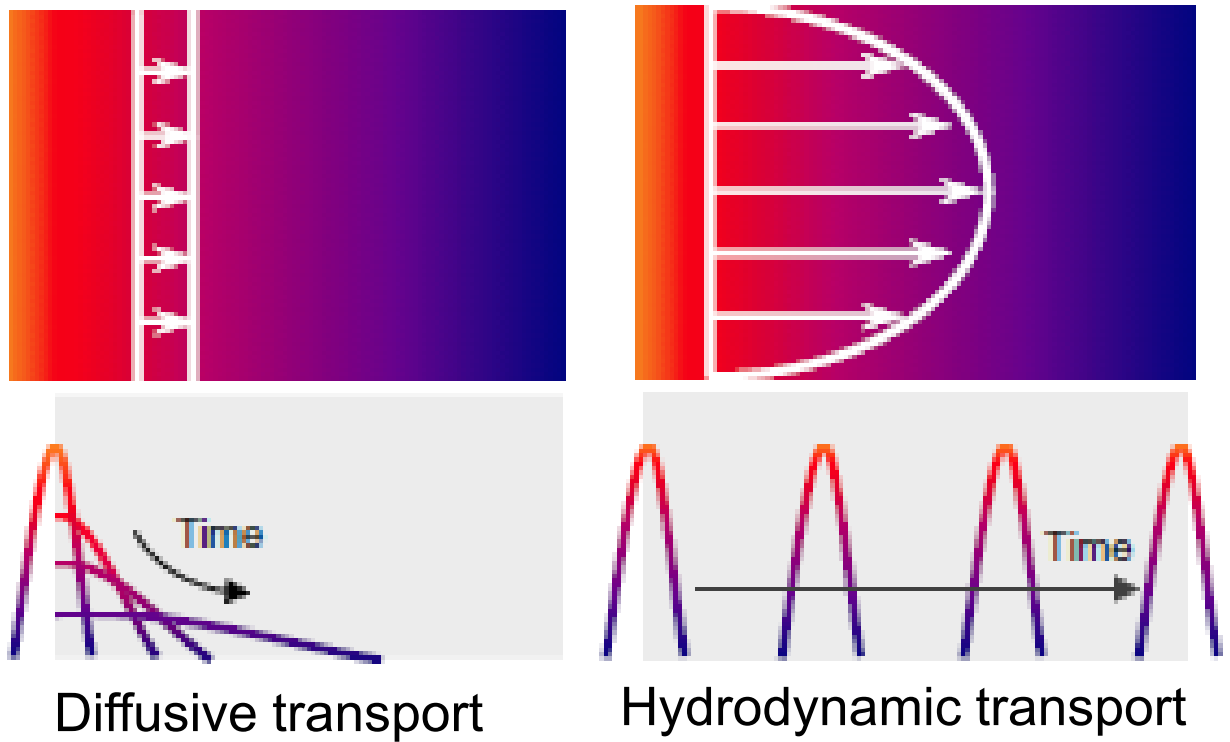


# 2D device applications

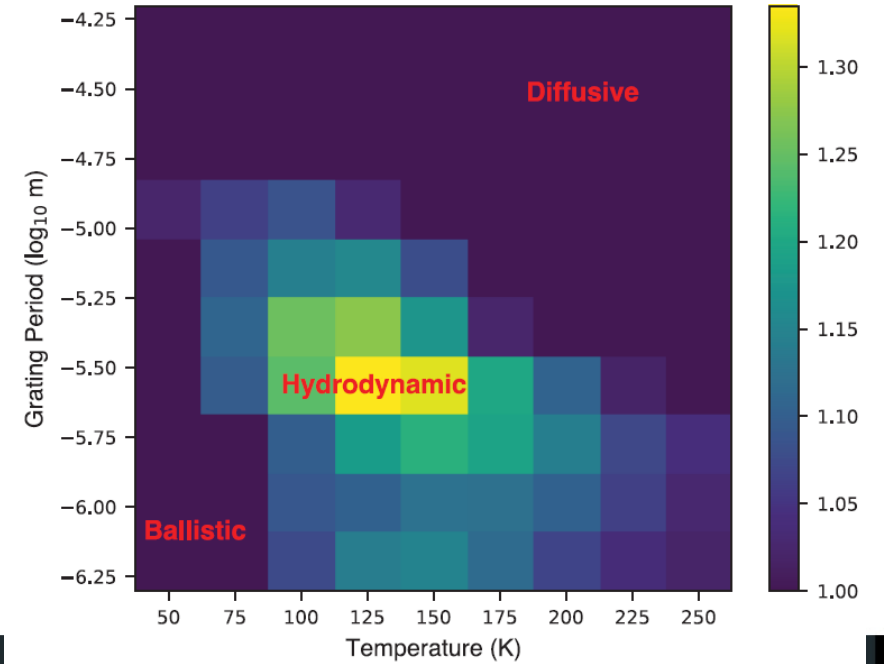
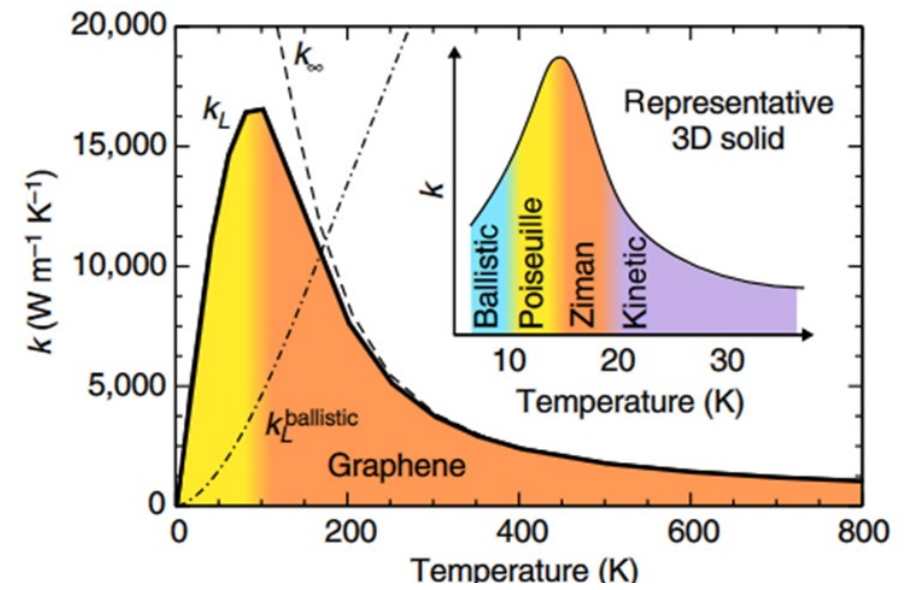


A.K. Geim and I.V. Grigorieva, Nature 499, 419-425, 2013  
Ling et al., Proc. Nat. Acad. Sci. 112, 4523-4530 (2014)

## Effective platform to take advantage of hydrodynamic (wave) transport of heat

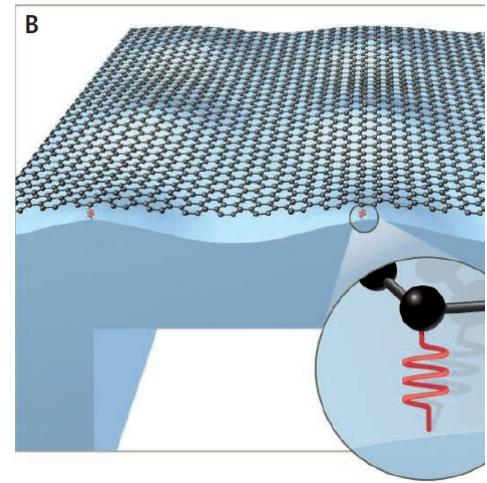
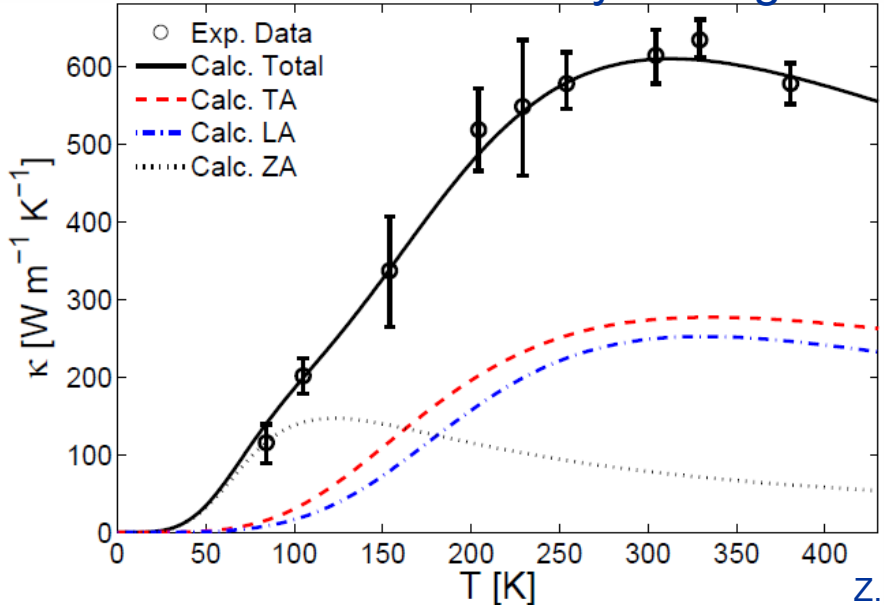


Lee et al., Nat. Commun. 6, 6290, 2015.  
 Cepellotti et al., Nat. Commun. 6, 6400, 2015.  
 Huberman et al., Science 364, 375–379, 2019.

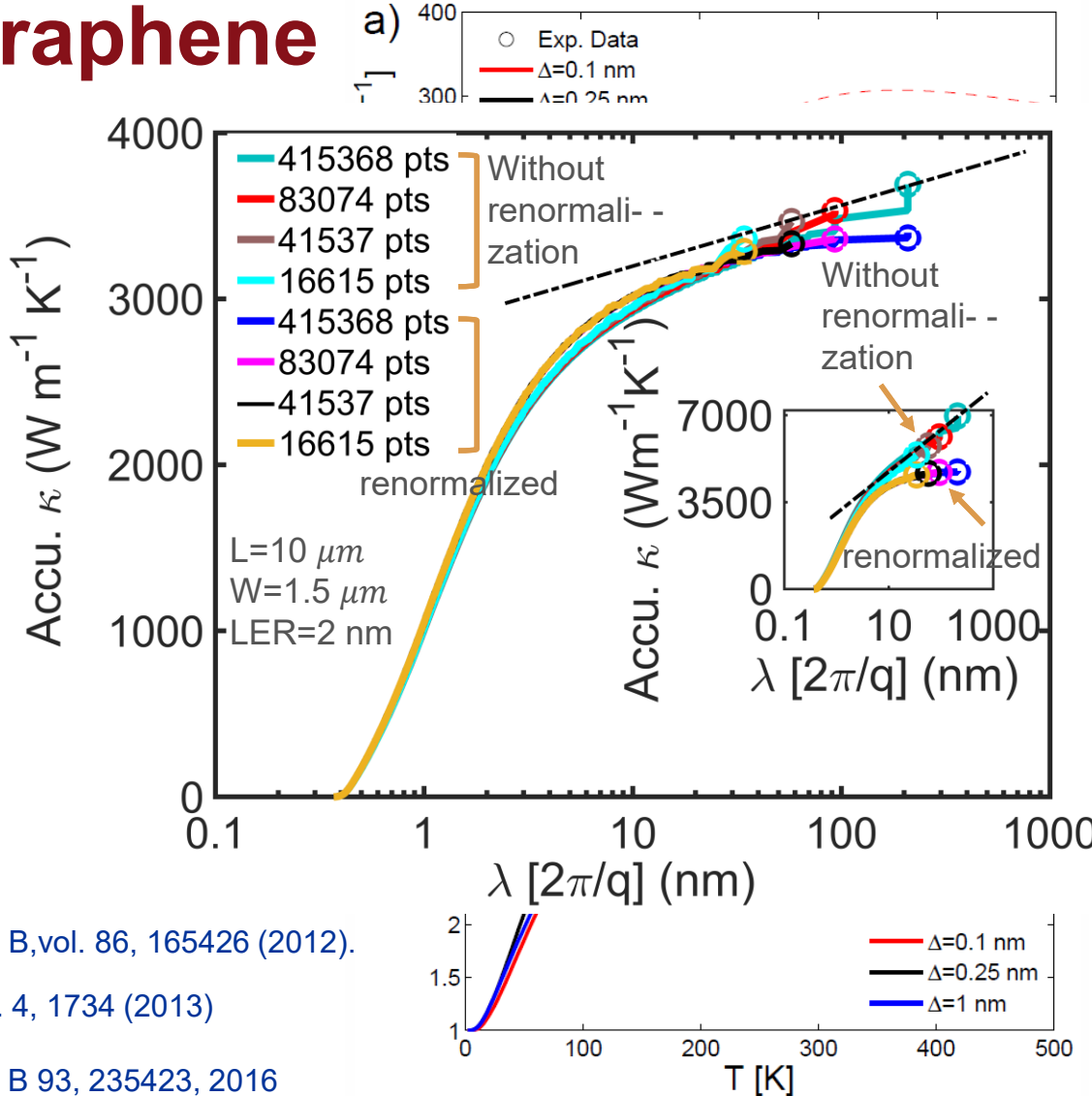


# Thermal transport in supported graphene

- Substrate scattering due to van der Waals interaction
- Drastic reduction in narrow supported GNR samples
- Thermal transport in narrow GNRs is highly anisotropic
- Thermal conductivity “diverges” with length up to 100  $\mu\text{m}$

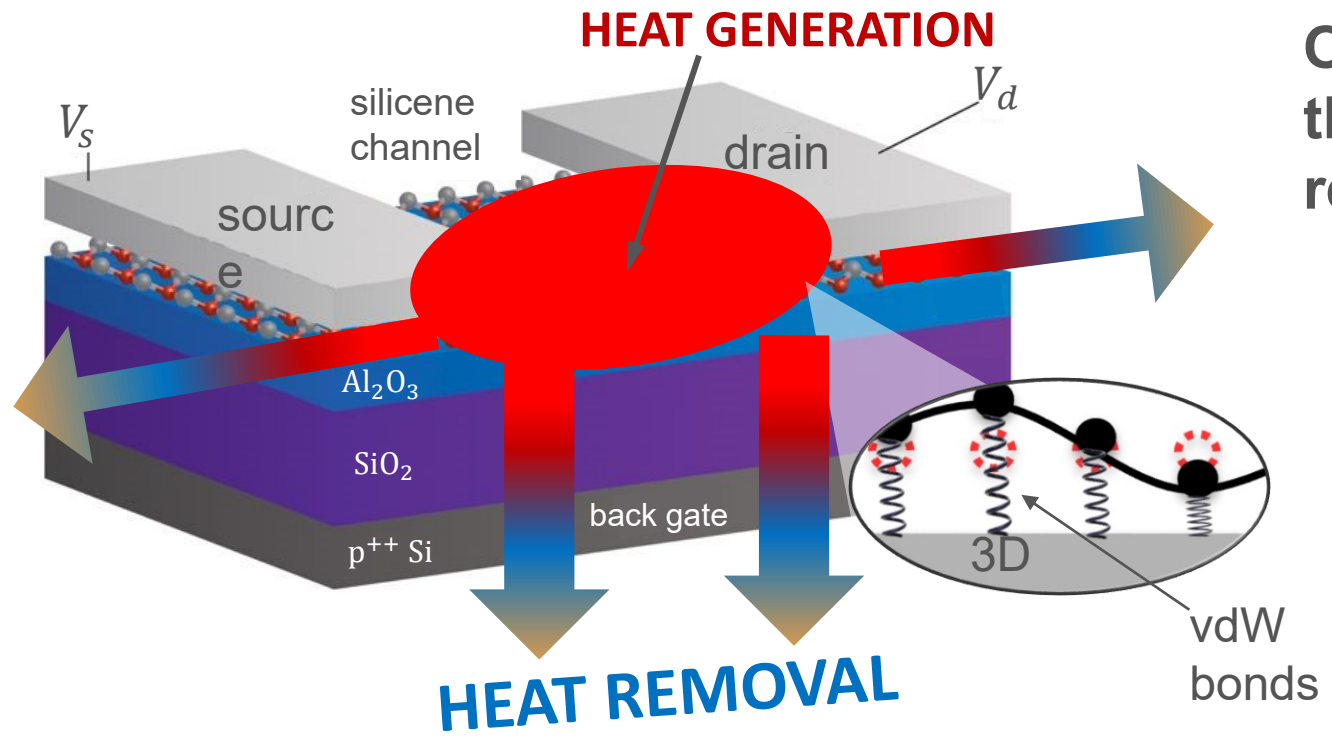


Z. Aksamija and I. Knezevic, Phys Rev. B, vol. 86, 165426 (2012).  
 Bae, Li, Aksamija, et al., Nature Comm. 4, 1734 (2013)  
 A.K. Majee and Z. Aksamija Phys. Rev. B 93, 235423, 2016

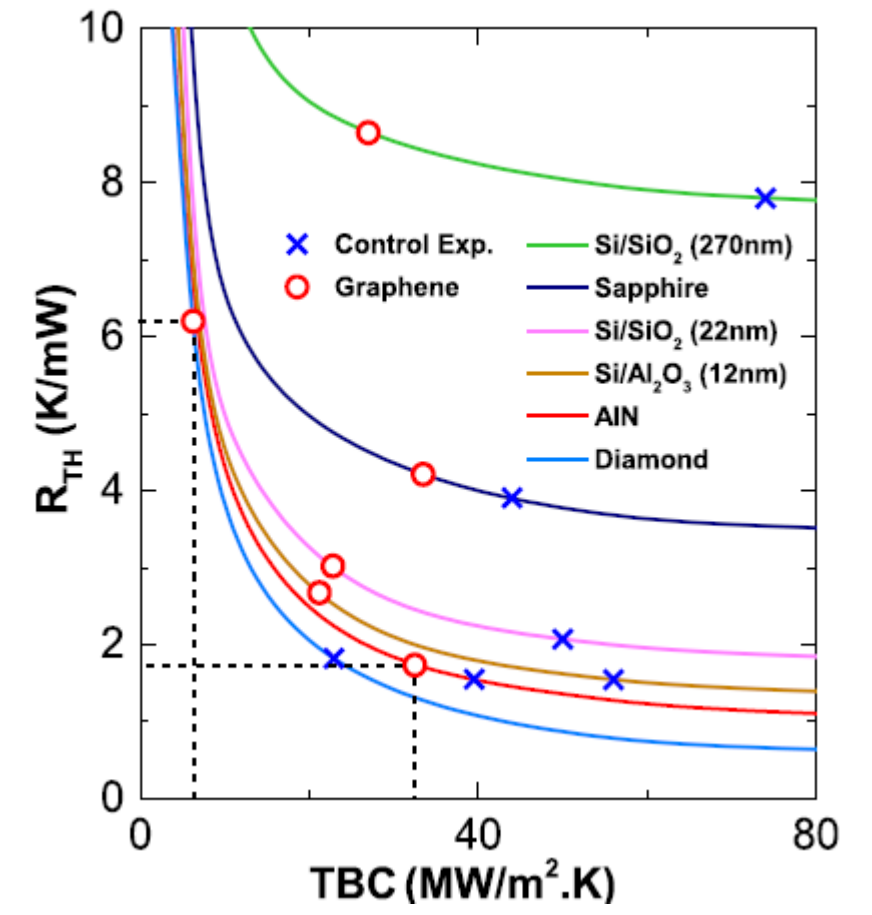




# 2D-3D thermal interface problem



Overall thermal resistance



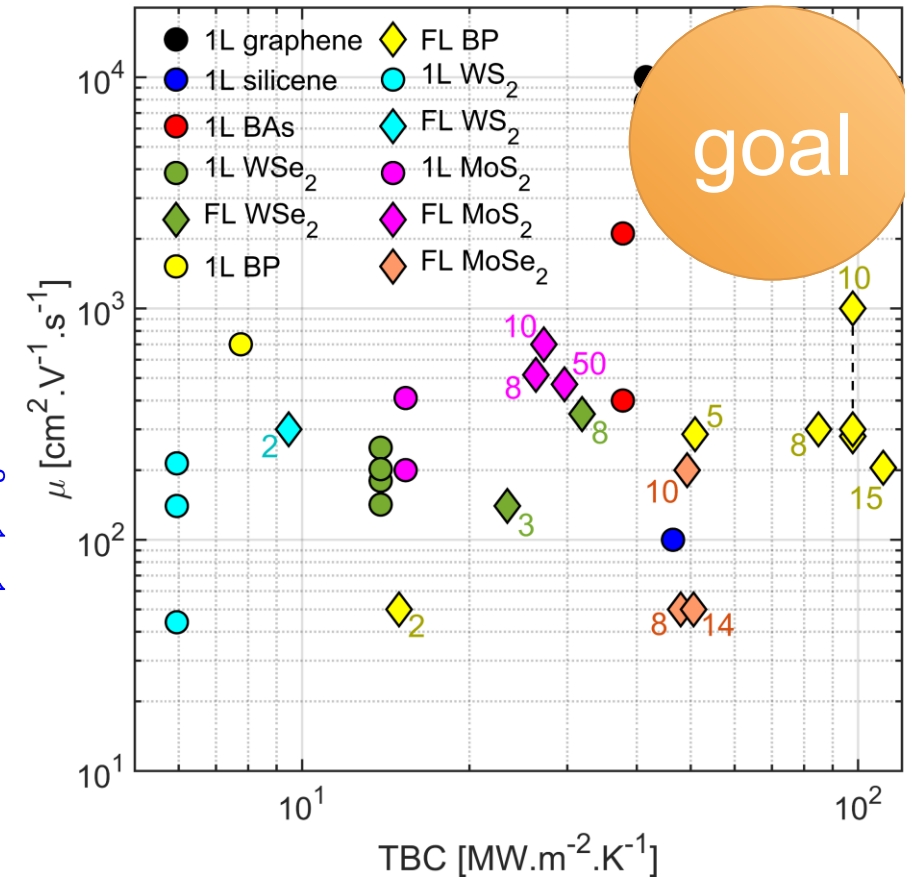
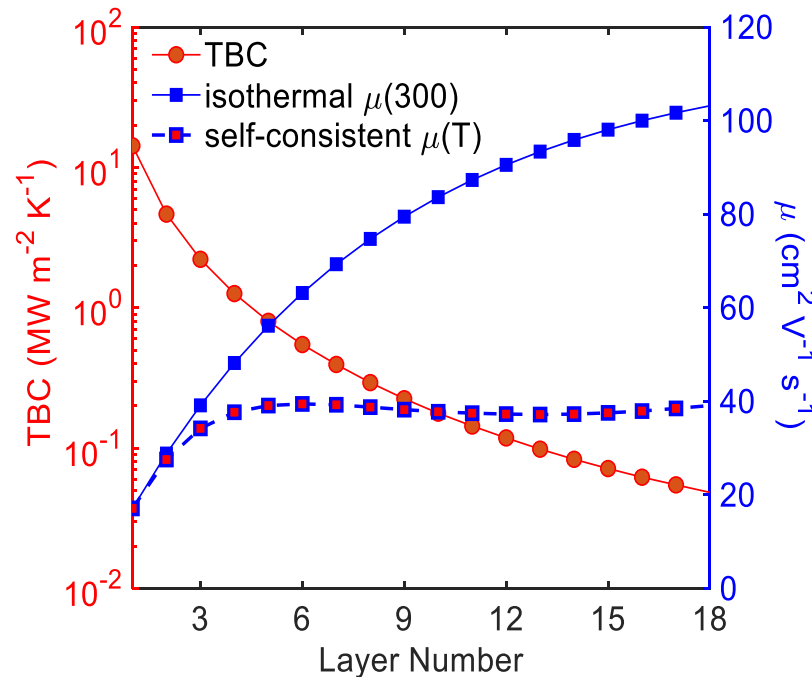
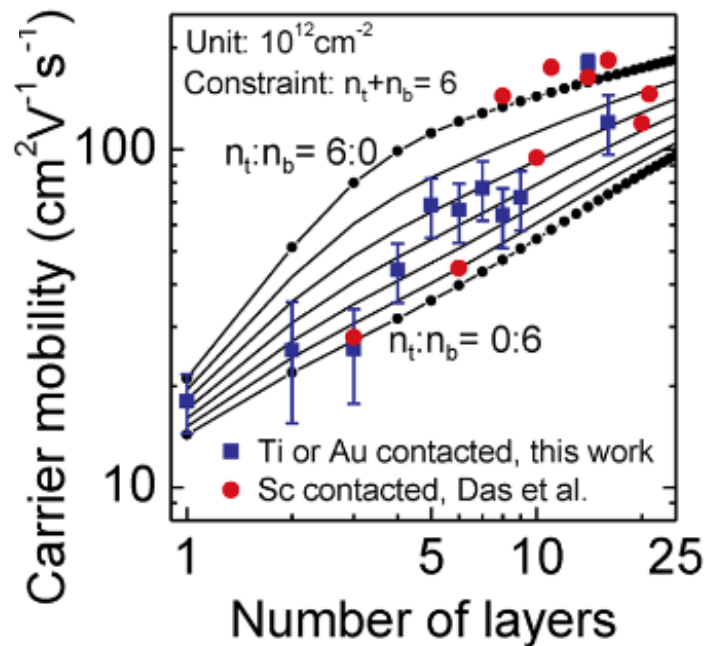
2D-3D thermal interfaces pose significant concerns

- governed by **vdW** forces
- **sensitive** to approaches in synthesis
- essentially **all interface**

*Most heat generated in a 2D device dissipates into the supporting substrate. Hence, the thermal (2D/3D) interface formed strongly dictates the capabilities of thermal management in 2D devices.*

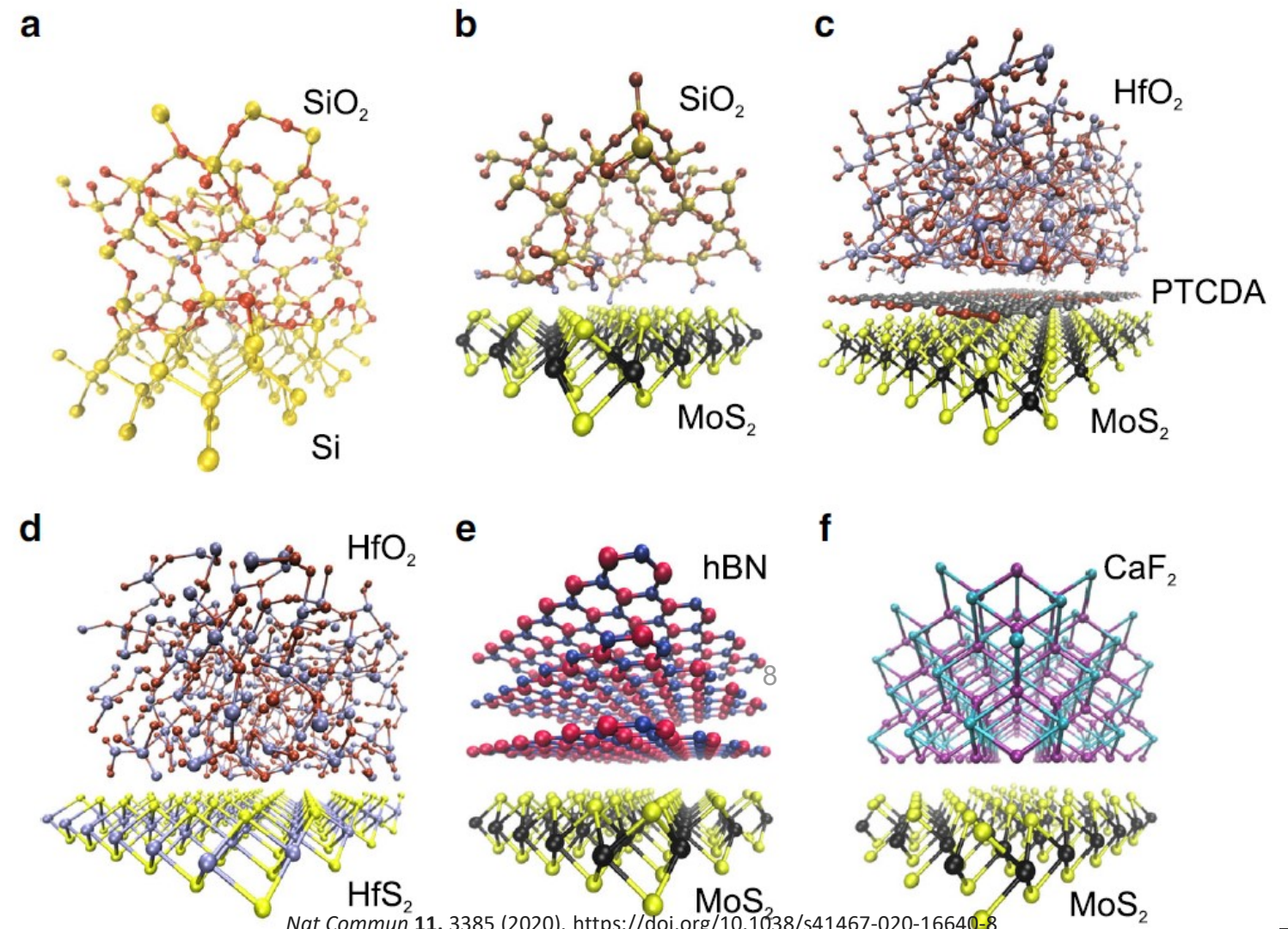
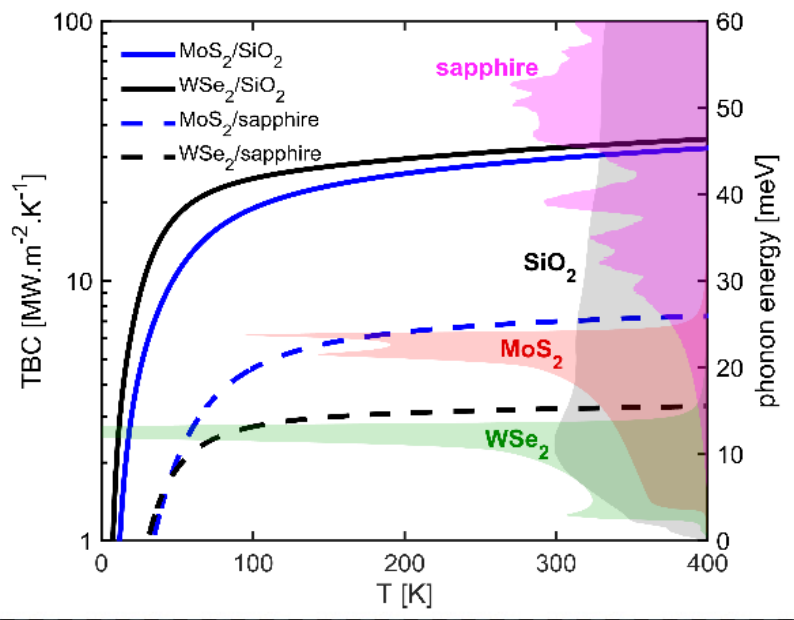
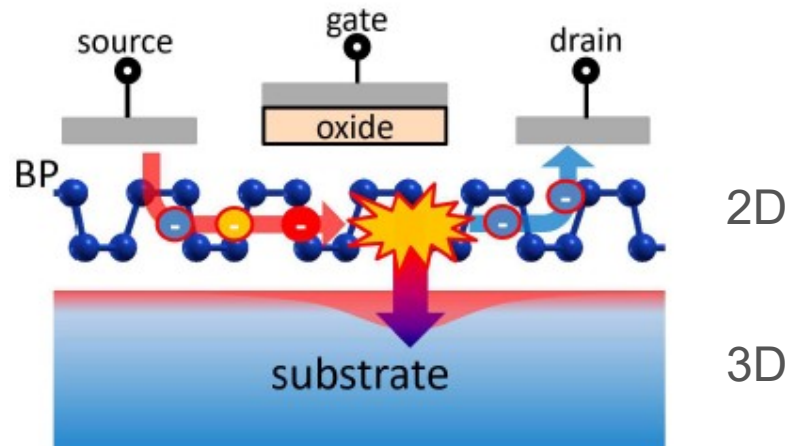
# 2D stacks for device applications

- Problem: self-heating degrades carrier mobility
- No 2D materials has simultaneously high mobility and thermal boundary conductance
- Mobility improves with thickness, which degrades thermal management

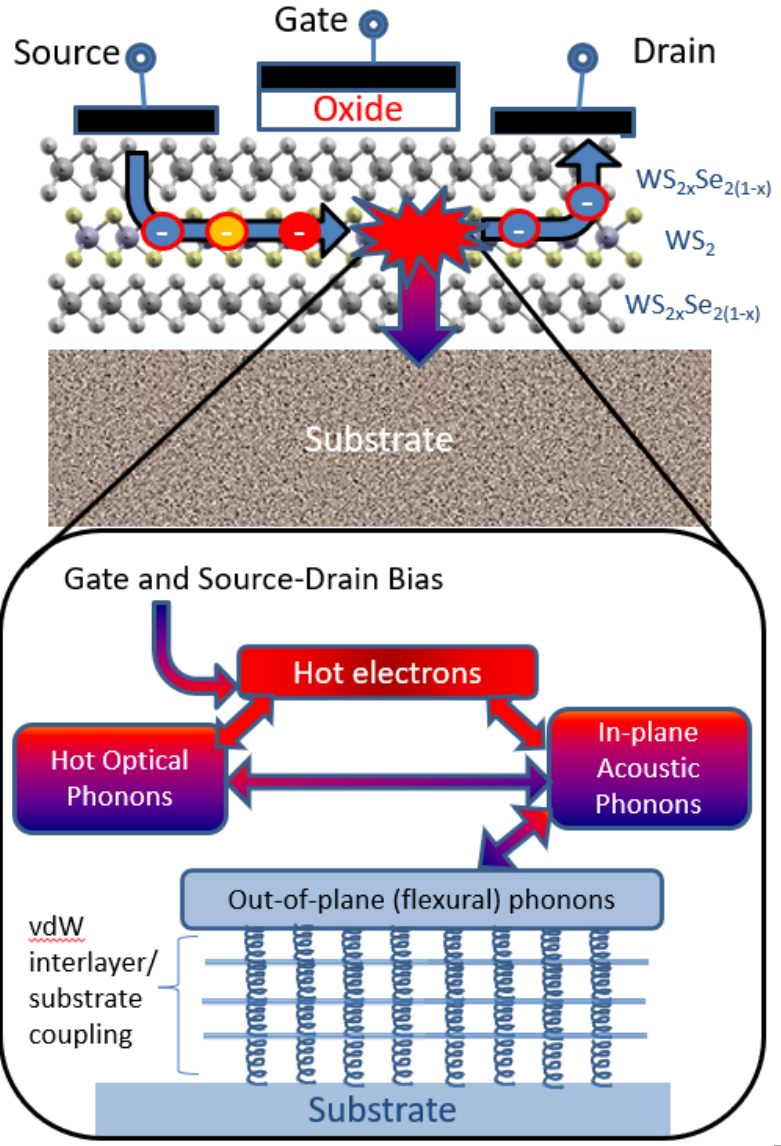


# 2D/3D Interface thermal resistance

NanoEnergy Lab, MSE@Utah







# Flexural pathway of 2D-3D thermal transport

## 2D-3D TBC:

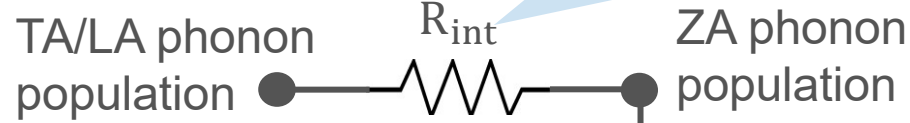
- weak van der Waals (vdW) bonding
- No cross-plane propagation ( $v_g = 0$ )
- Primary carrier of heat is ZA (flexural) phonons
- Scattering facilitates transport across the interface

$$\Gamma_{TBC}(\omega)$$

Correa et al., Nanotechnology 28 (2017) 135402  
 Adv. Mater. Interfaces (2017), 4, 1700334  
 Adv. Mater. (2018), 30, 1801629.

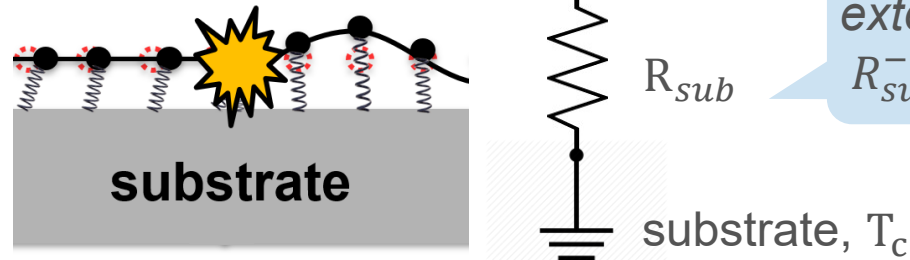
Internal resistance:

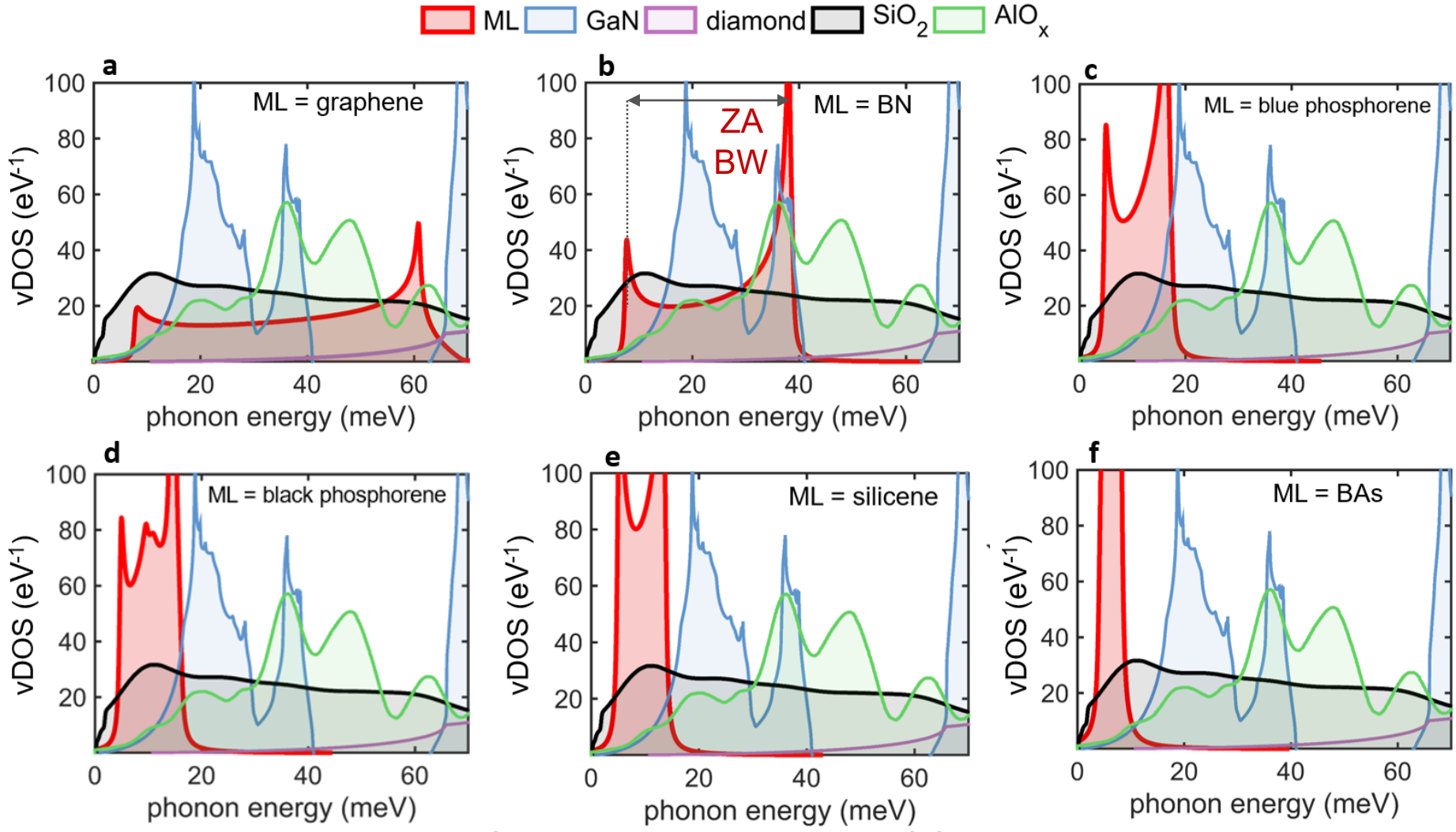
$$R_{int}^{-1} = G_{int} \propto \Gamma_{int}$$



external resistance:

$$R_{sub}^{-1} = G_{sub} \propto \Gamma_{sub}$$





...at low energies!

**Amorphous (boson peak):**

$$D_{sub}(\omega) > \frac{\omega^2}{v_s^3}$$

**Crystal (Debye):**

$$D_{sub}(\omega) \propto \frac{\omega^2}{v_s^3}$$

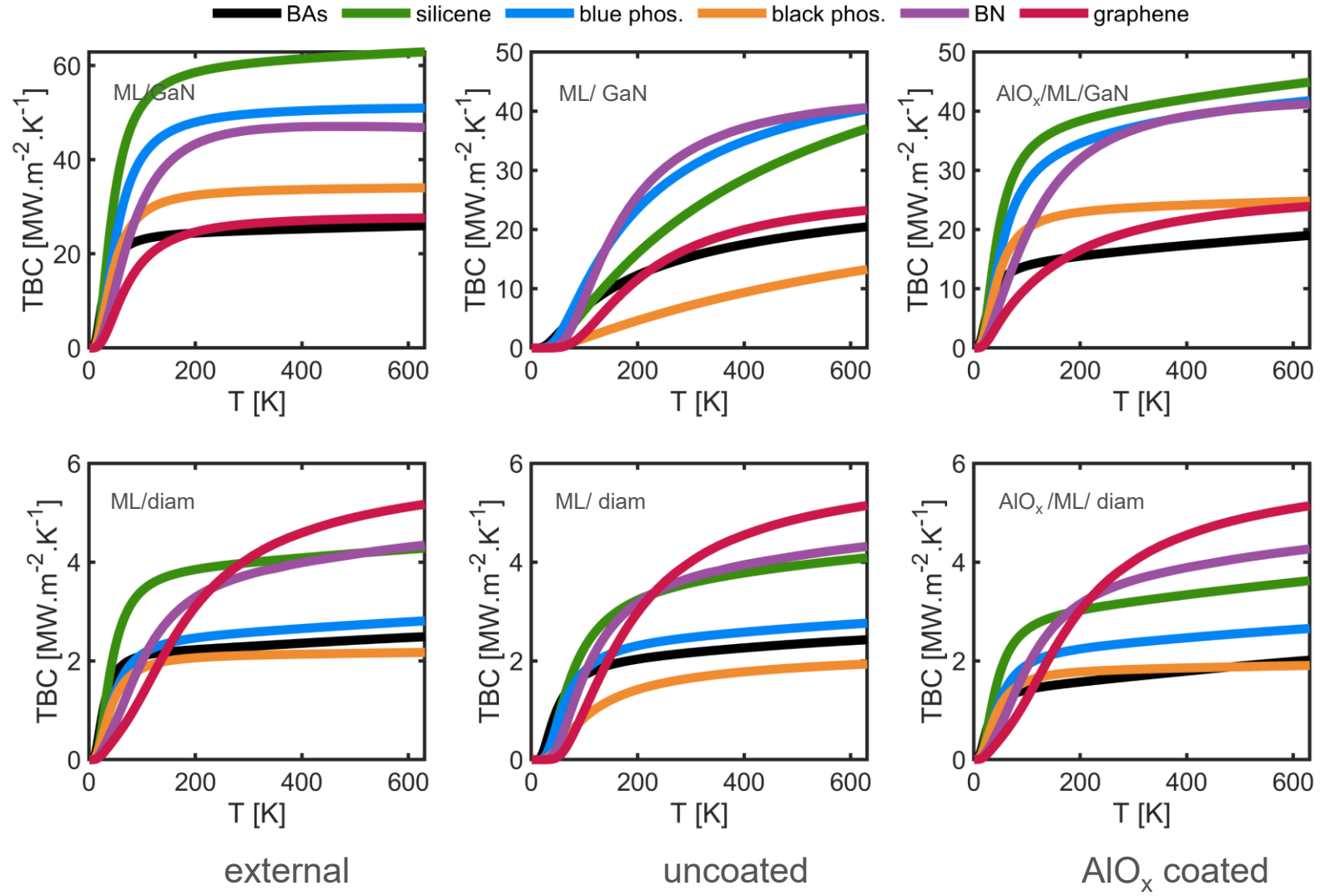
$$G_{ext}(T) \propto D_{2D} D_{sub}$$

$$\Gamma_{sub} \propto \frac{1}{\omega^2}$$

ML=monolayer  
BW=bandwidth

External TBC strongly depends on DOS overlap.  
A narrower ZA bandwidth should lend itself to a larger external TBC.

# TBC of 2D-crystalline interfaces



On crystals with high sound velocity (i.e., small low energy vDOS) like diamond, 2D materials with broader ZA BWs are preferred such as graphene and BN.

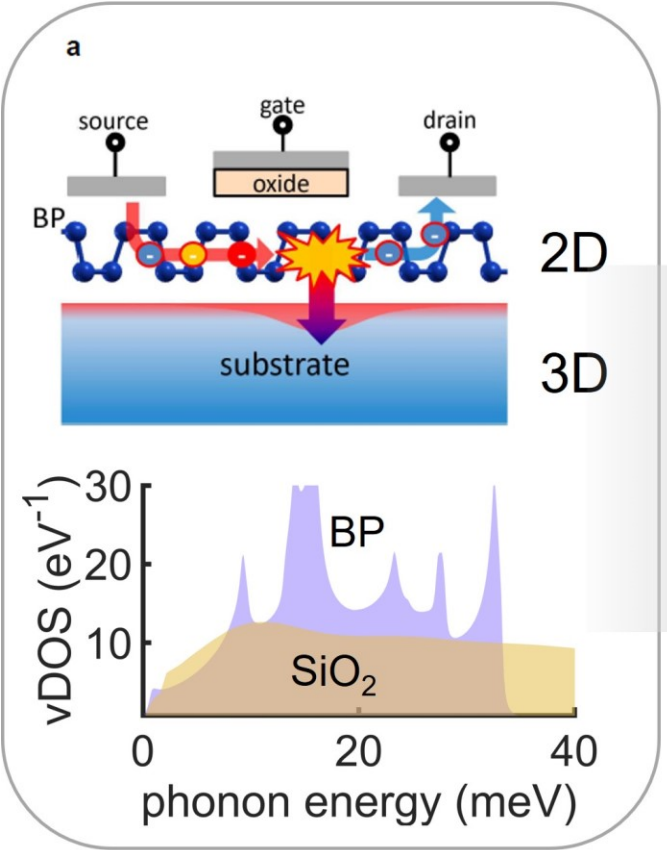
$$\Gamma_{sub} \propto \frac{1}{\omega^2}$$

Cameron Foss and Zlatan Aksamija  
2021 *Nanotechnology* **32** 405206

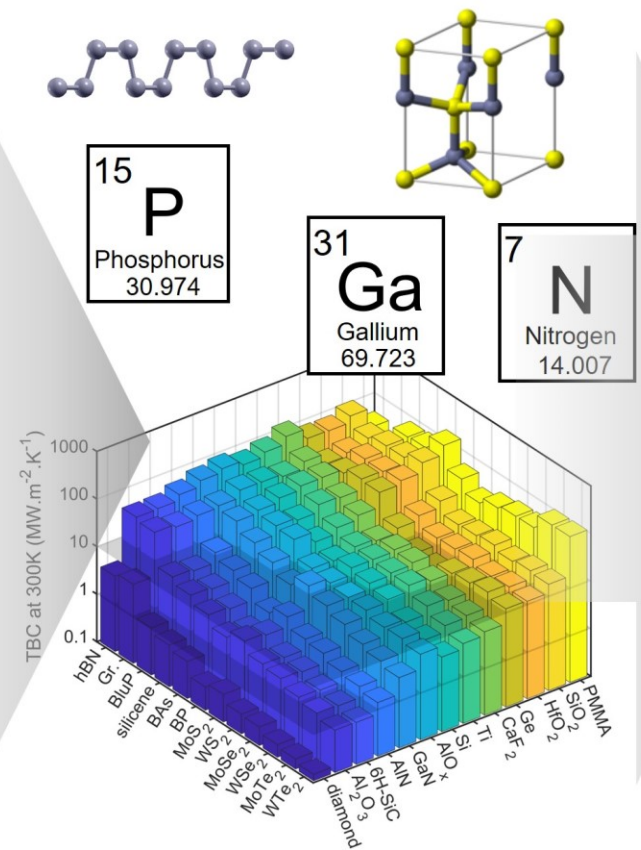


# Machine learning model for 2D/3D TBC

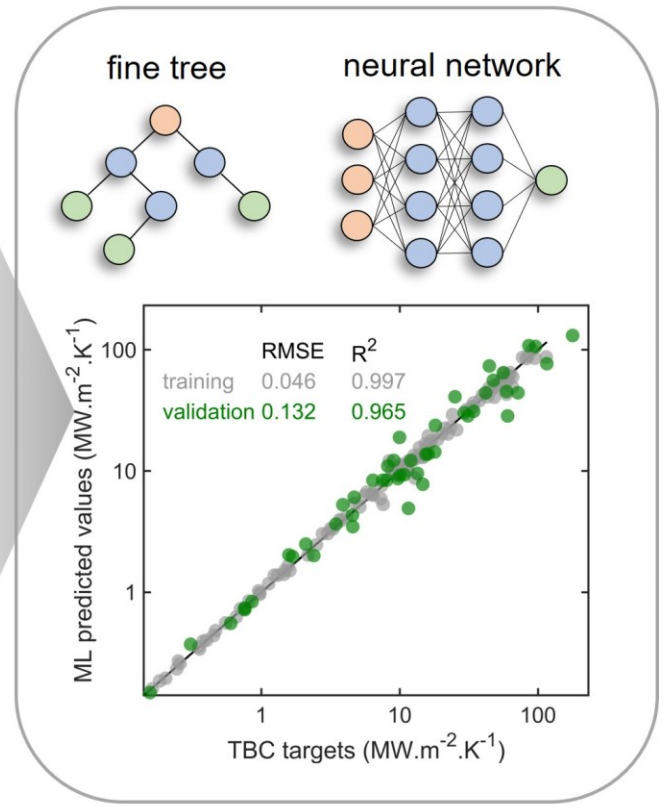
DFT+pBTE calculations



data collection

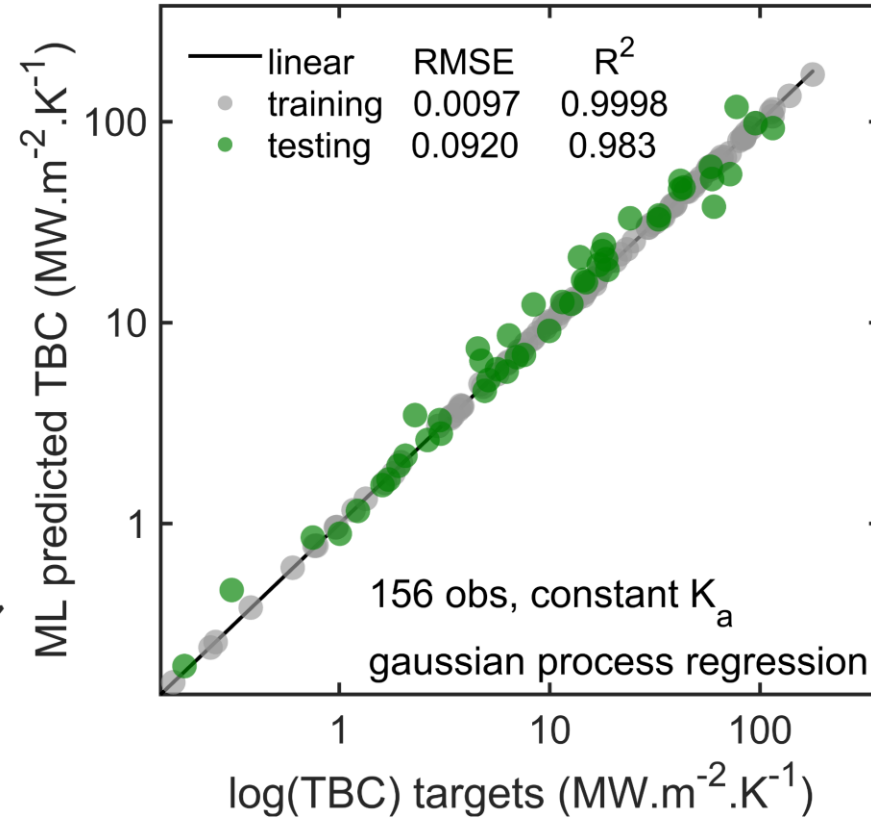
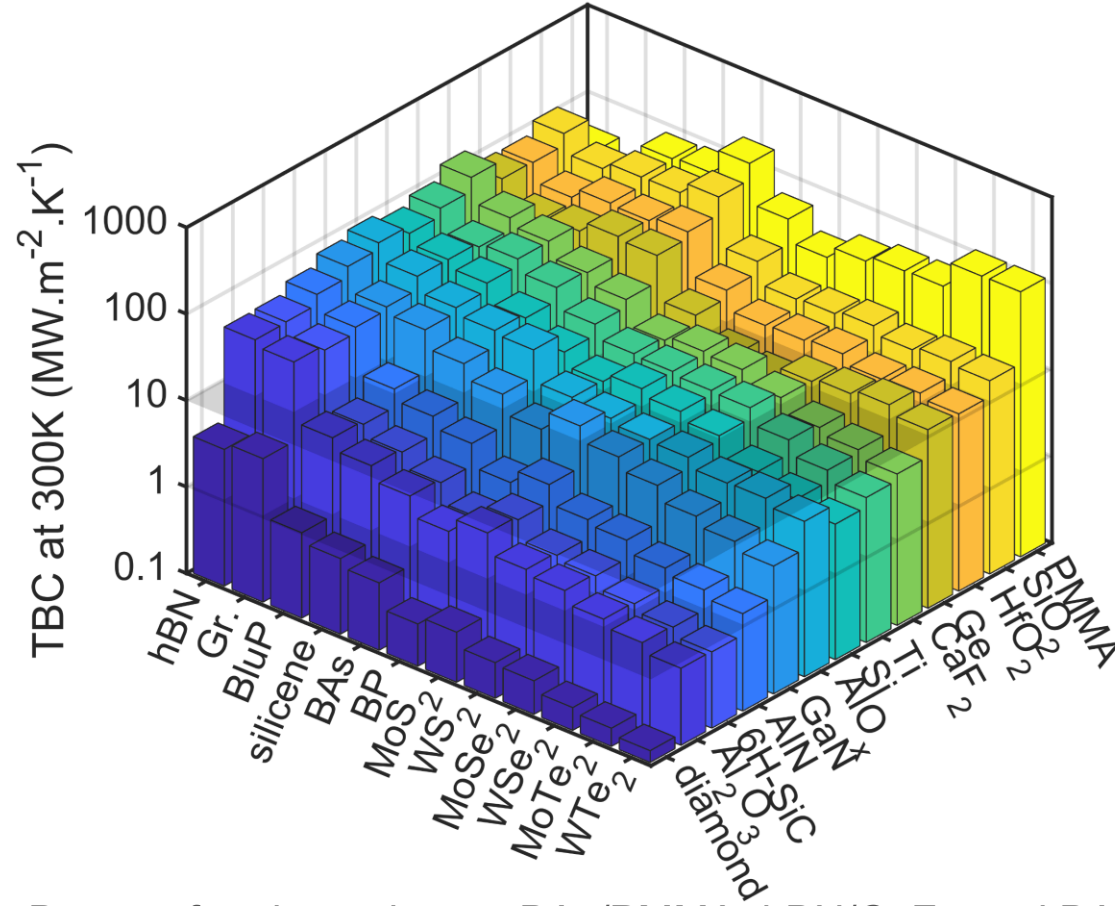


machine learning analysis



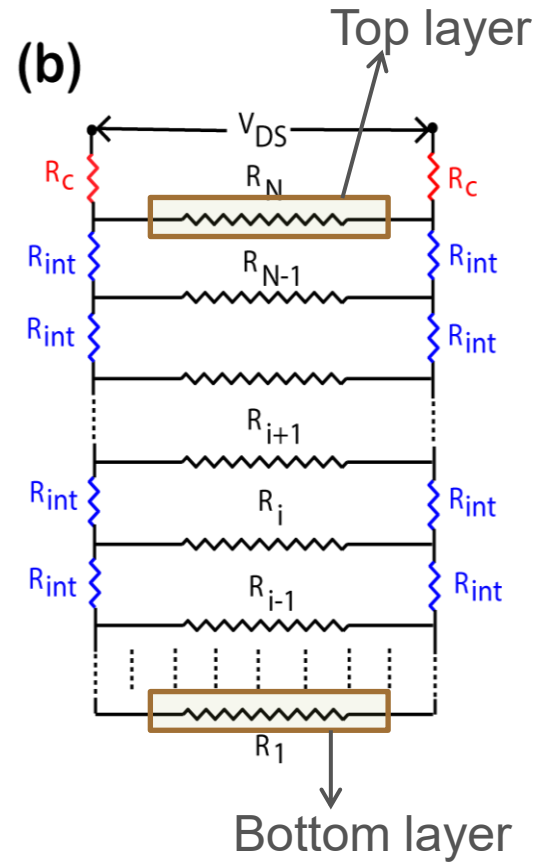
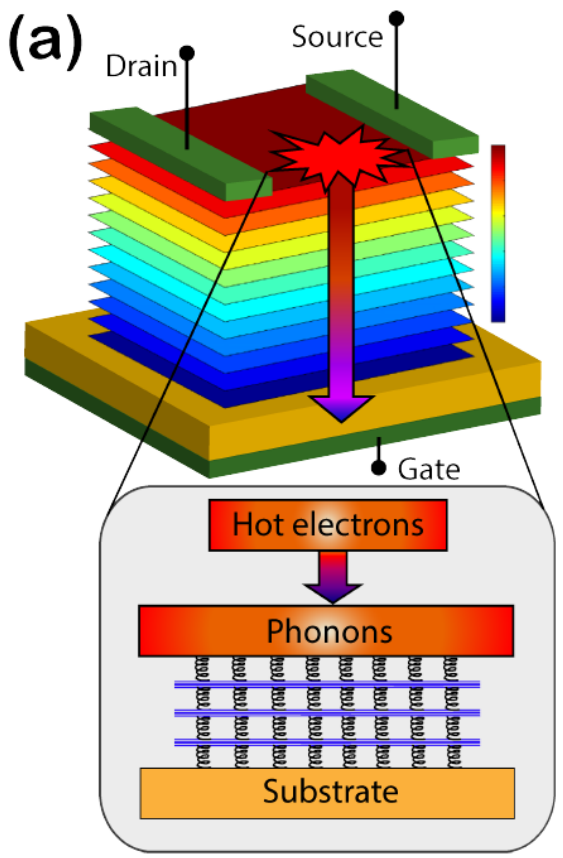
**Goal(s):** Develop a streamlined predictive model that can be used to suggest ultrahigh/low TBC pairings and distill the most impactful material descriptors from our theoretical model using sensitivity analysis.

# Results: room-temperature TBC and ML fitting

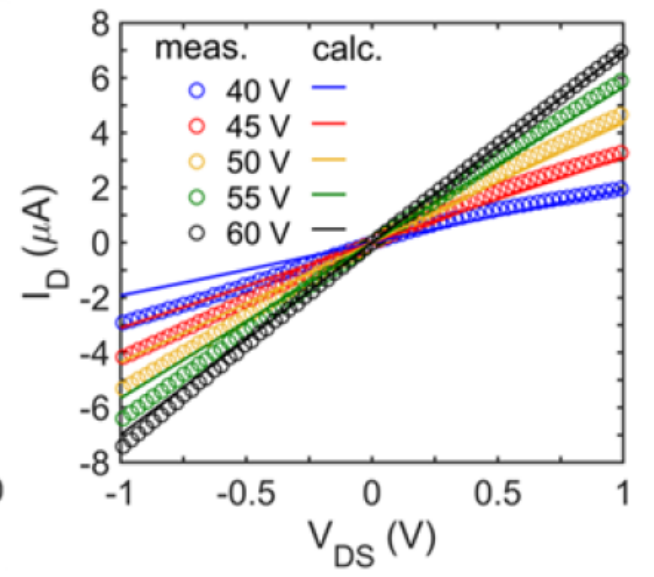
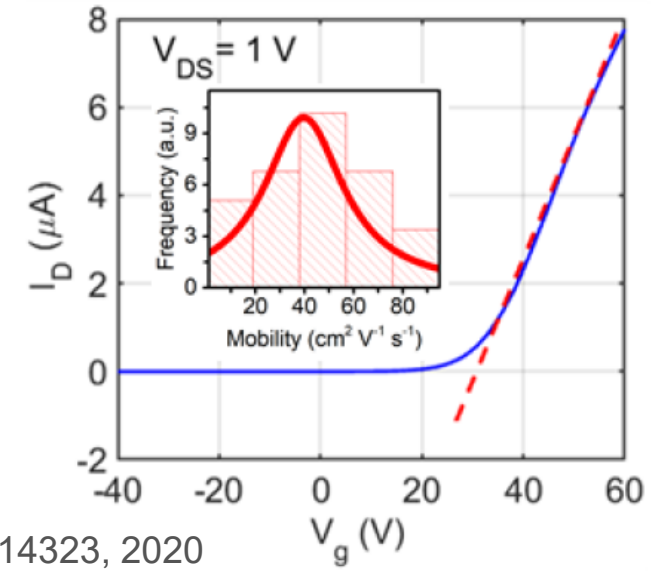


- Best performing pairs are BAs/PMMA, hBN/CaF<sub>2</sub>, and BAs/SiO<sub>2</sub> (100-150 MW.m<sup>-2</sup>.K<sup>-1</sup>)
- Worst performing substrates are diamond, Al<sub>2</sub>O<sub>3</sub>, and 6H-SiC (<10 MW.m<sup>-2</sup>.K<sup>-1</sup>)
- Paper: Foss and Aksamija, Appl. Phys. Lett. 122, 062201 (2023), Data: <https://nanoenergy.mse.utah.edu/codesdata/>

# Dissipation and self-heating in 2D WSe<sub>2</sub> devices



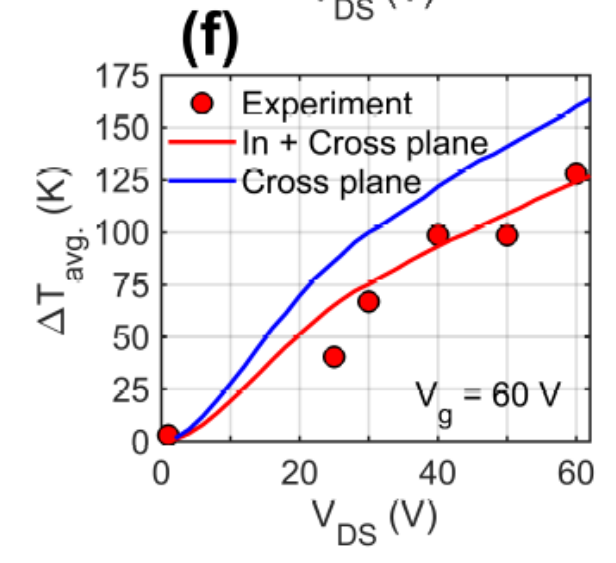
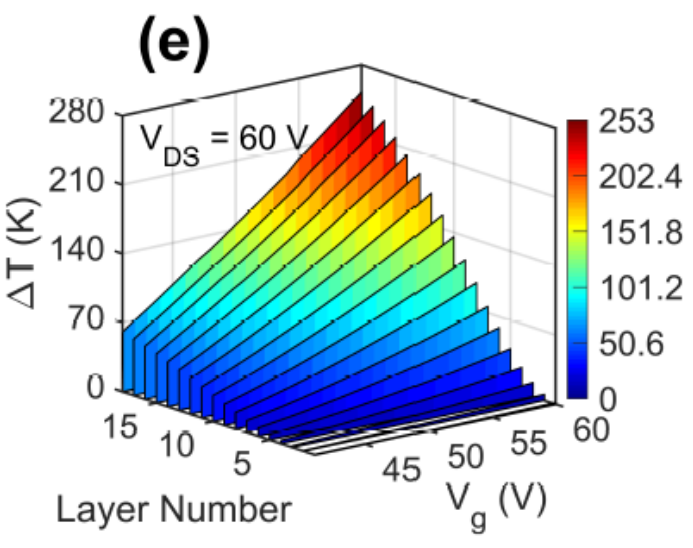
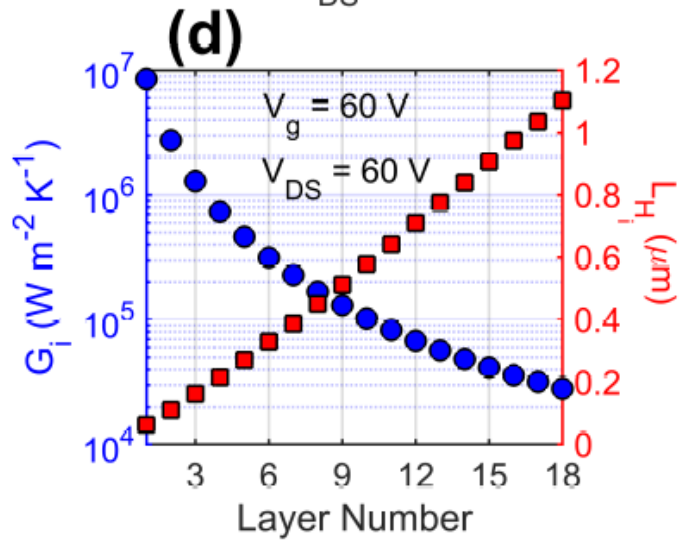
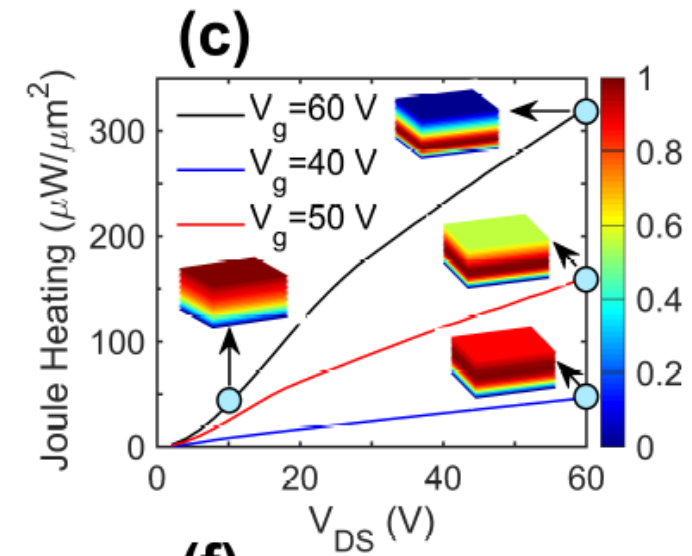
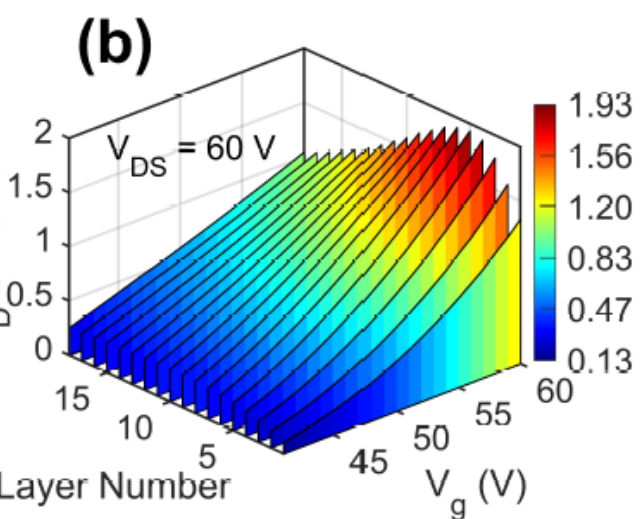
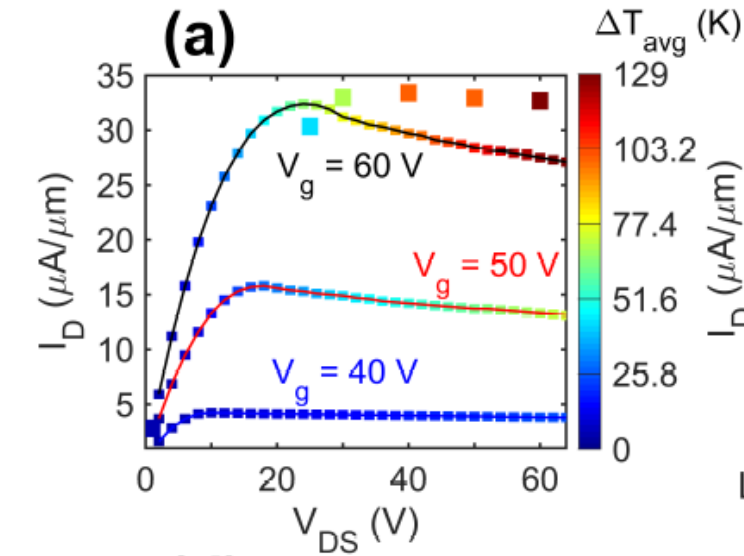
- Few-layered 2D devices offer higher mobility and current carrying capacity
- Current flow and heat dissipation are not uniform
- We characterized and simulated an 18-layer WSe<sub>2</sub> FET
- Raman measurements quantify temperature
- Significant self-heating leads to mobility degradation



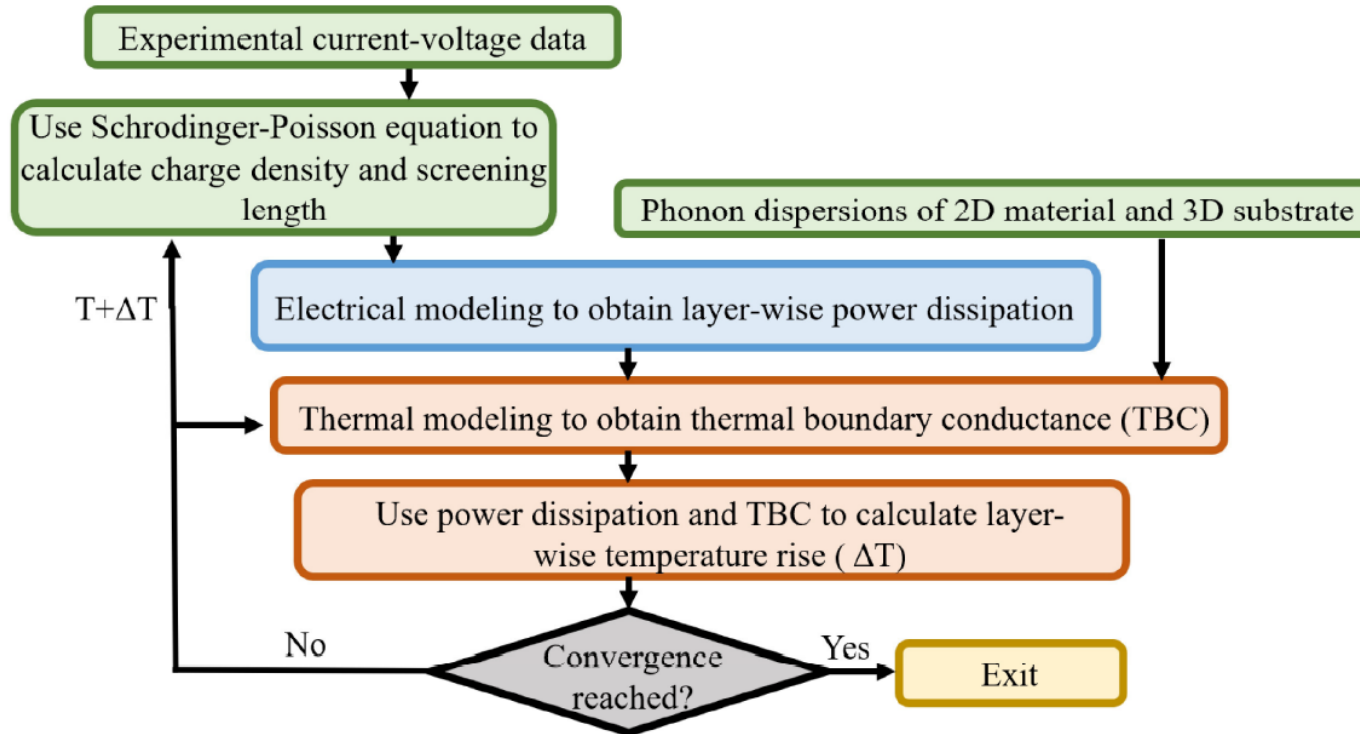
Initial model: Das and Appenzeller, Nano Lett. 2013, 13, 7, 3396–3402  
 Our model+experiments: Majee et al., ACS Appl. Mater. Interfaces 20, 14323, 2020



# Novel current re-routing mechanism

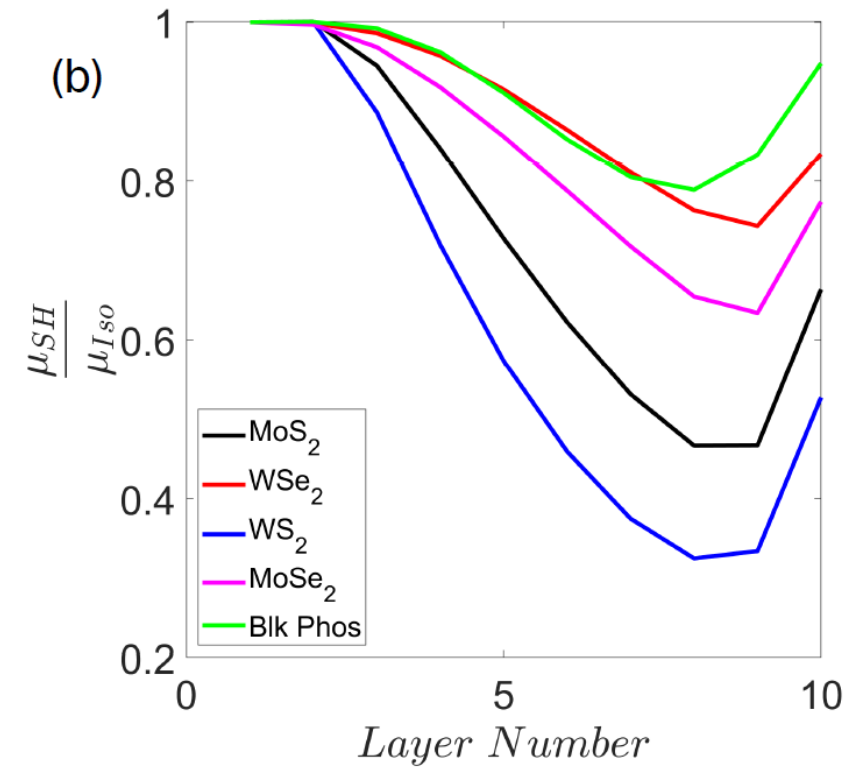
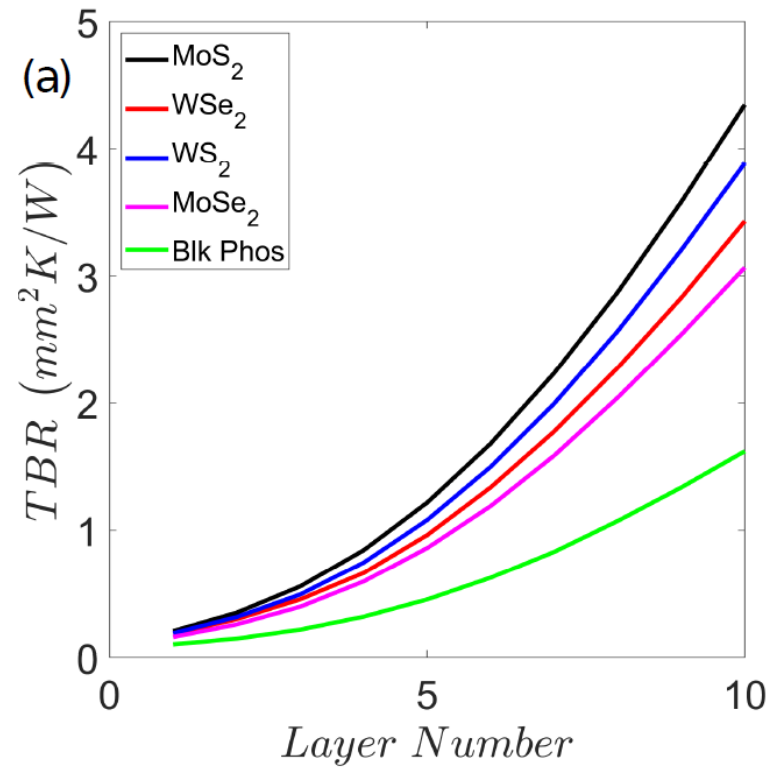


# Adding self-consistent Schroedinger-Poisson



- Solve the coupled Schroedinger-Poisson in the vertical (through-plane) direction at every “slice” along channel
- Wrap the self-consistent electro-thermal loop around the electron transport model
- Each layer has a temperature-dependent mobility, Joule heating, and effective thermal conductance

# Mobility degradation for 10-layer stacks



- We compare mobility degradation due to self-heating across the 4 canonical TMDs and BP
- BP has the highest TBC (lowest TBR), resulting in the lowest mobility degradation



# Conclusions

- Heat dissipation a crucial bottleneck to 2D devices
- Heat transfer primarily via vdW bonds to substrate
- Exacerbated in 2D stacks: added interlayer thermal resistance
- Matching 2D layer to 3D substrate controls TBC
- Machine Learning to predict ideal 2D-substrate pairings
- Coupled electro-thermal model to identify best performing materials
  
- QUESTIONS?                      [zlatan.aksamija@utah.edu](mailto:zlatan.aksamija@utah.edu)