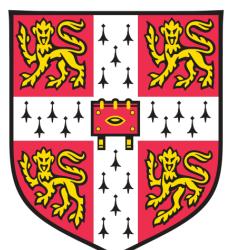




# QUANTUM ESPRESSO:

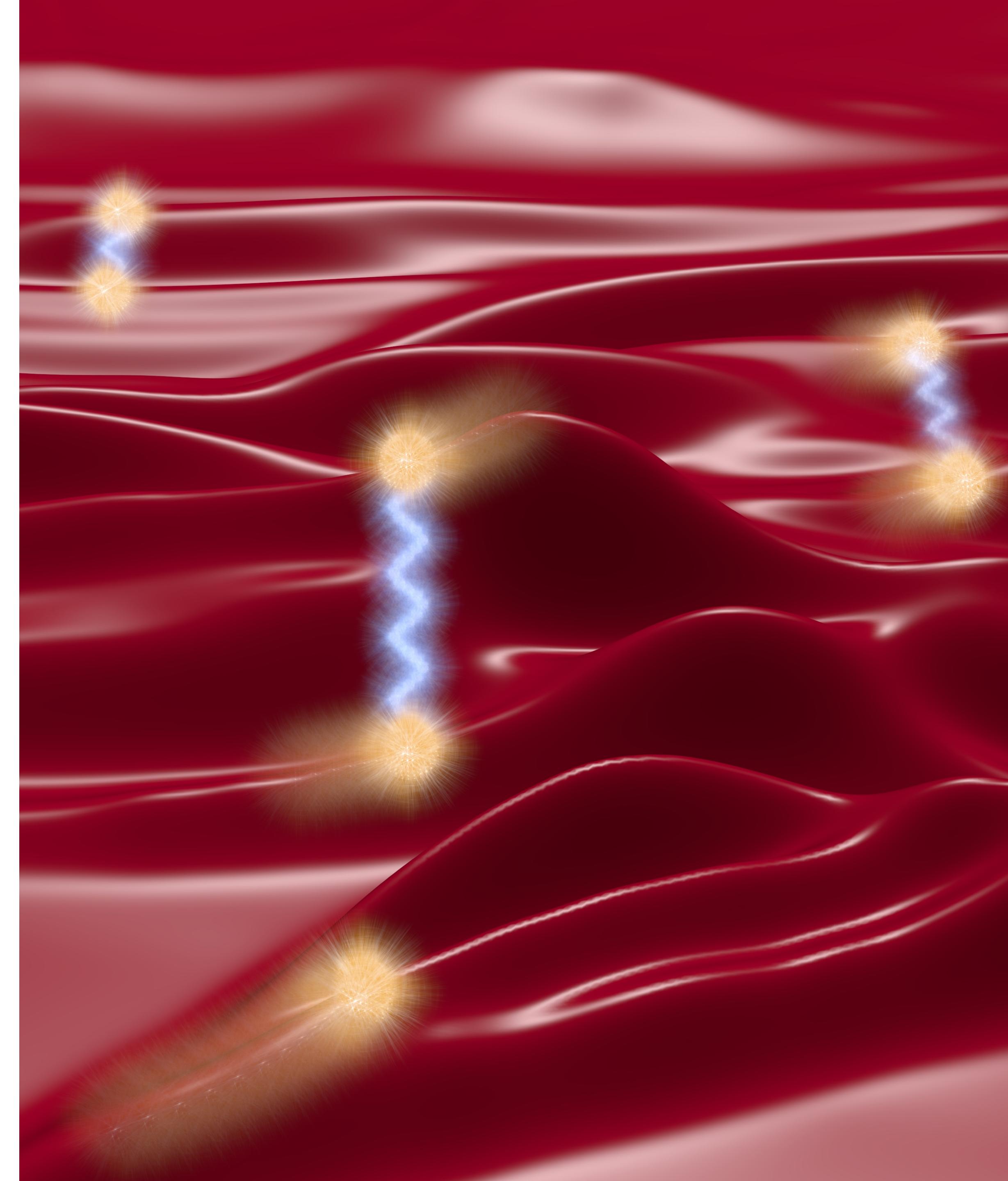
from density-functional theory to  
dual wave-particle transport and  
device simulation

Michele Simoncelli  
[ms2855@cam.ac.uk](mailto:ms2855@cam.ac.uk)



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# OUTLINE



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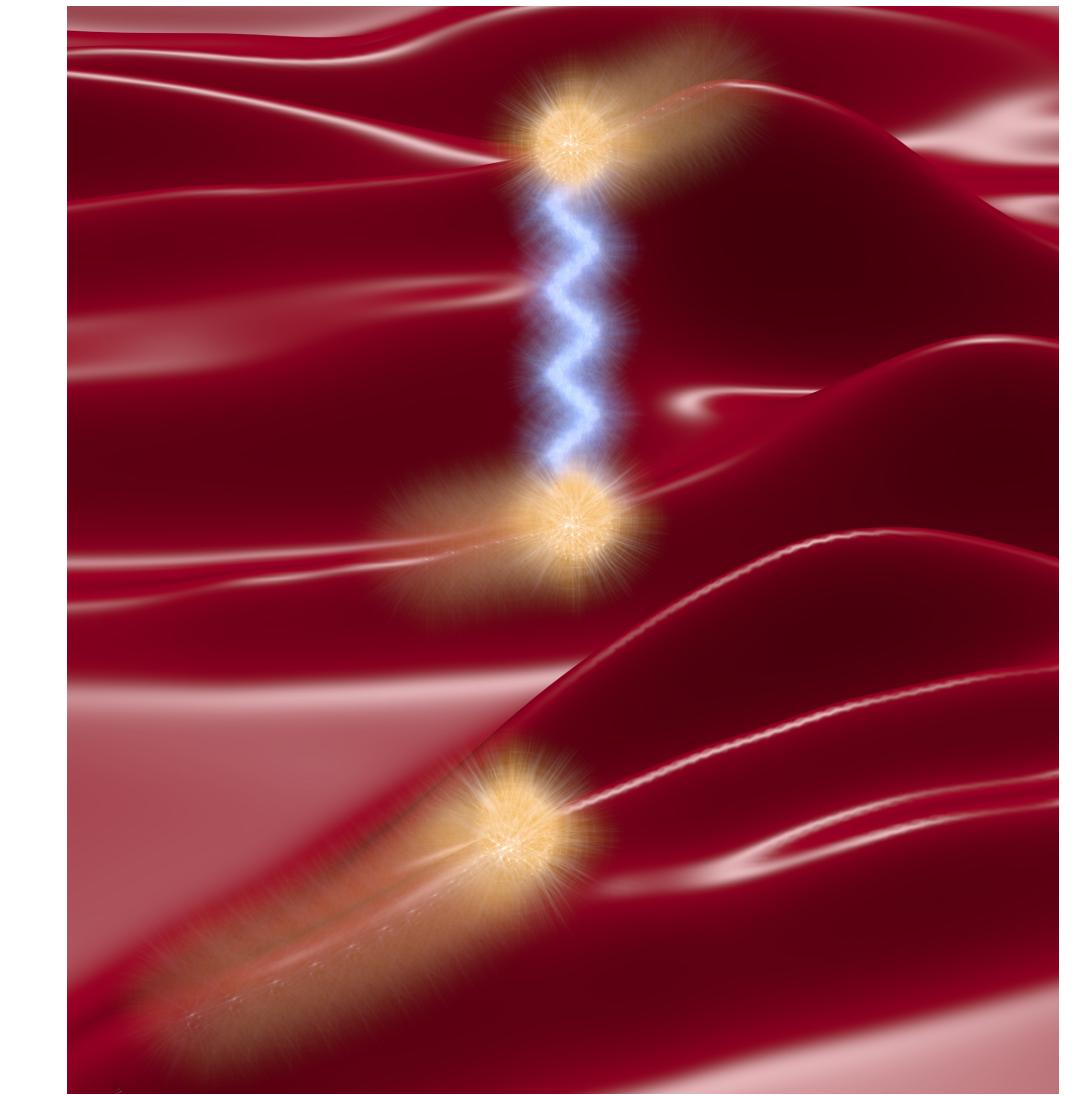
## Density functional theory and dual wave-particle transport

Wigner formulation for electron and phonon transport

*Simoncelli, Marzari, Mauri, Nat. Phys. 15 (2019)*

*Simoncelli, Marzari, Mauri, Phys. Rev. X 12 (2022)*

*Cepellotti and Kozinsky, Materials Today Physics 19 (2021)*



nm –

## Raman spectra: structural & quasiparticles' properties

## Beyond band transport

Charge transport in solid state ionic conductors

*Kahle, Marcolongo, & Marzari, Energy Environ. Sci. 13 (2020)*

Thermal transport in glasses from first principles

*Simoncelli, Mauri, Marzari, npj Comput. Mater. 9 (2023);*

*Harper, Iwanowski, Payne, Simoncelli arXiv 2303.08637 (2023)*

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## First-principles parametrisation of mesoscopic models

Viscous heat equations & diffusive-hydrodynamic crossover

*Simoncelli, Marzari, Cepellotti, Phys. Rev. X 10 (2020)*

*Dragašević and Simoncelli, arXiv:2303.12777 (23.03.2023)*

Predicting reflectivity and colour of metals

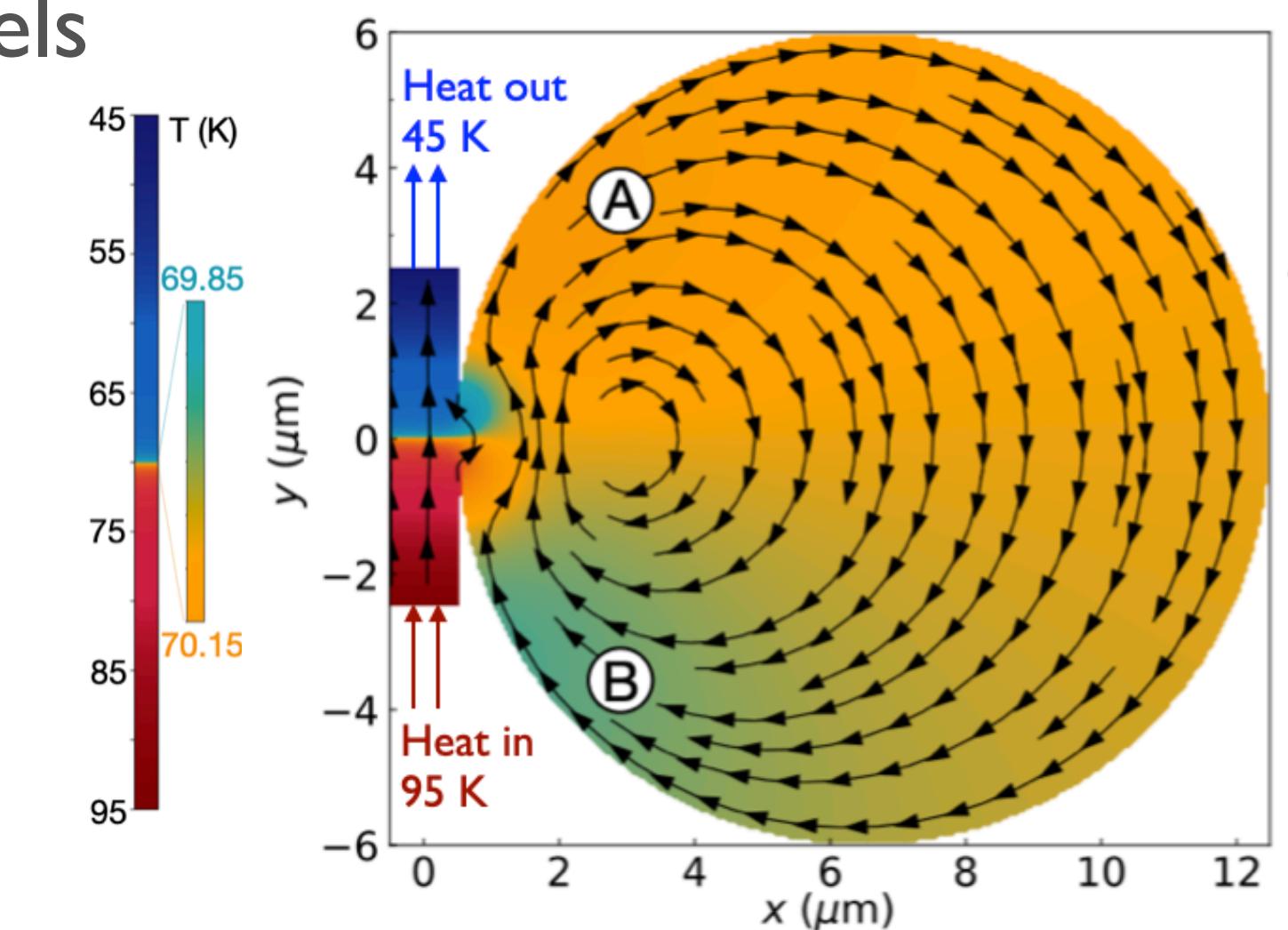
*Prandini, Rignanese, & Marzari, npj Comput. Mater. 129 (2019)*



μm –

mm –

Size





QUANTUM ESPRESSO  
[www.quantum-espresso.org](http://www.quantum-espresso.org)



## Quantum opEn-Source Package for Research in Electronic Structure, Simulation, and Optimization

*J. Phys.: Condens. Matter 21, 395502 (2009) and J. Phys.: Condens. Matter 29, 465901 (2017)*

Composed of several packages: **CP**: Car-Parrinello molecular dynamics

**PWneb**: Nudged Elastic Band (NEB) for reaction pathways and barriers

**atomic**: pseudopotential generation code

**PWcond**: ballistic conductance

**Xspectra**: Calculation of X-ray near-edge adsorption spectra (XANES)

**GWL**: GW band structure with ultralocalized Wannier functions

**TD-DFPT**: Time-Dependent Density-Functional Perturbation Theory

**HP**: Hubbard parameters from linear response

**turboMagnon**: spin-wave spectra using TD-DFPT

**PWscf**: self-consistent electronic structure, structural optimization, molecular dynamics

**Phonon**: linear-response calculations (phonons, dielectric properties)

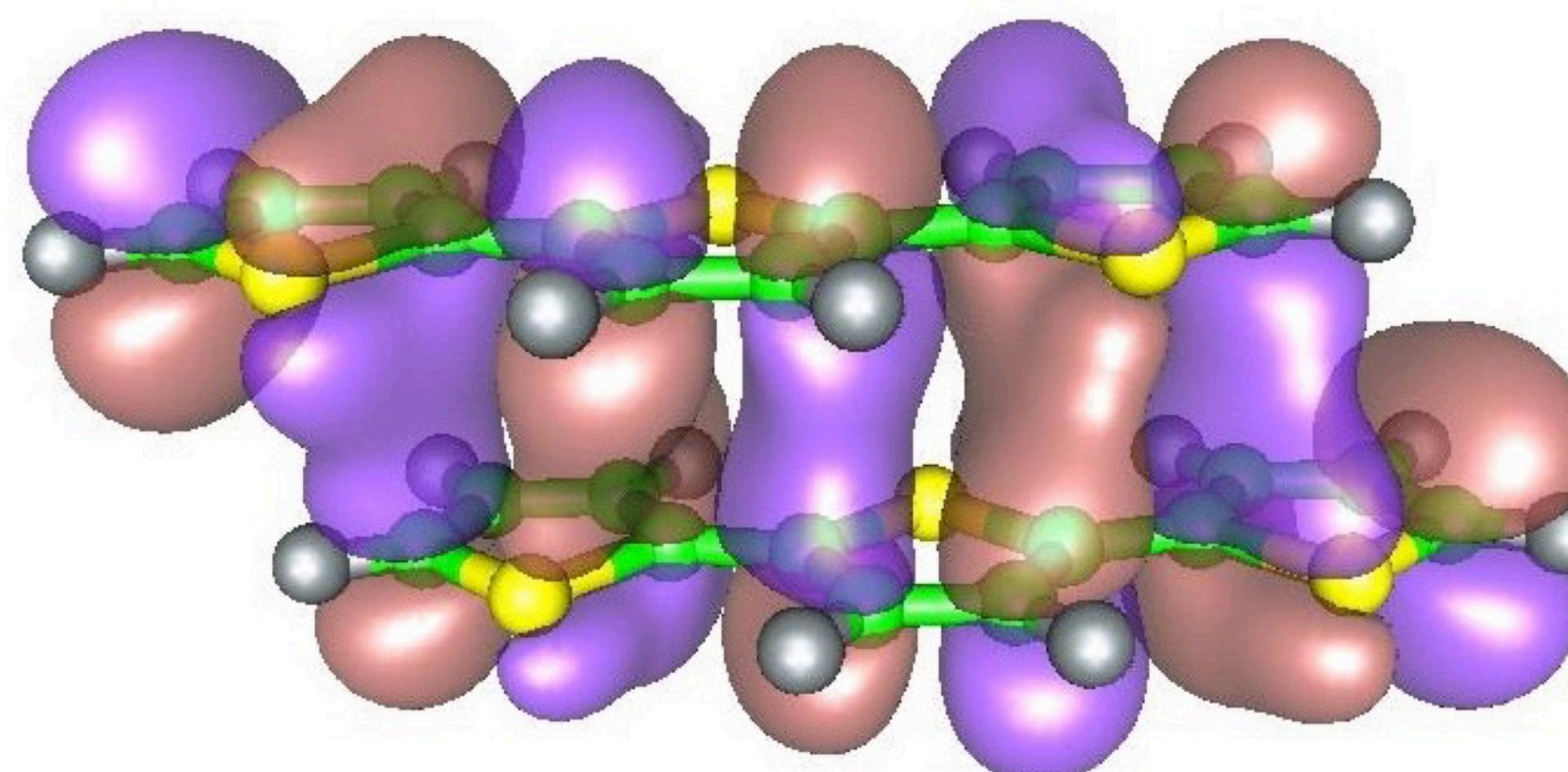
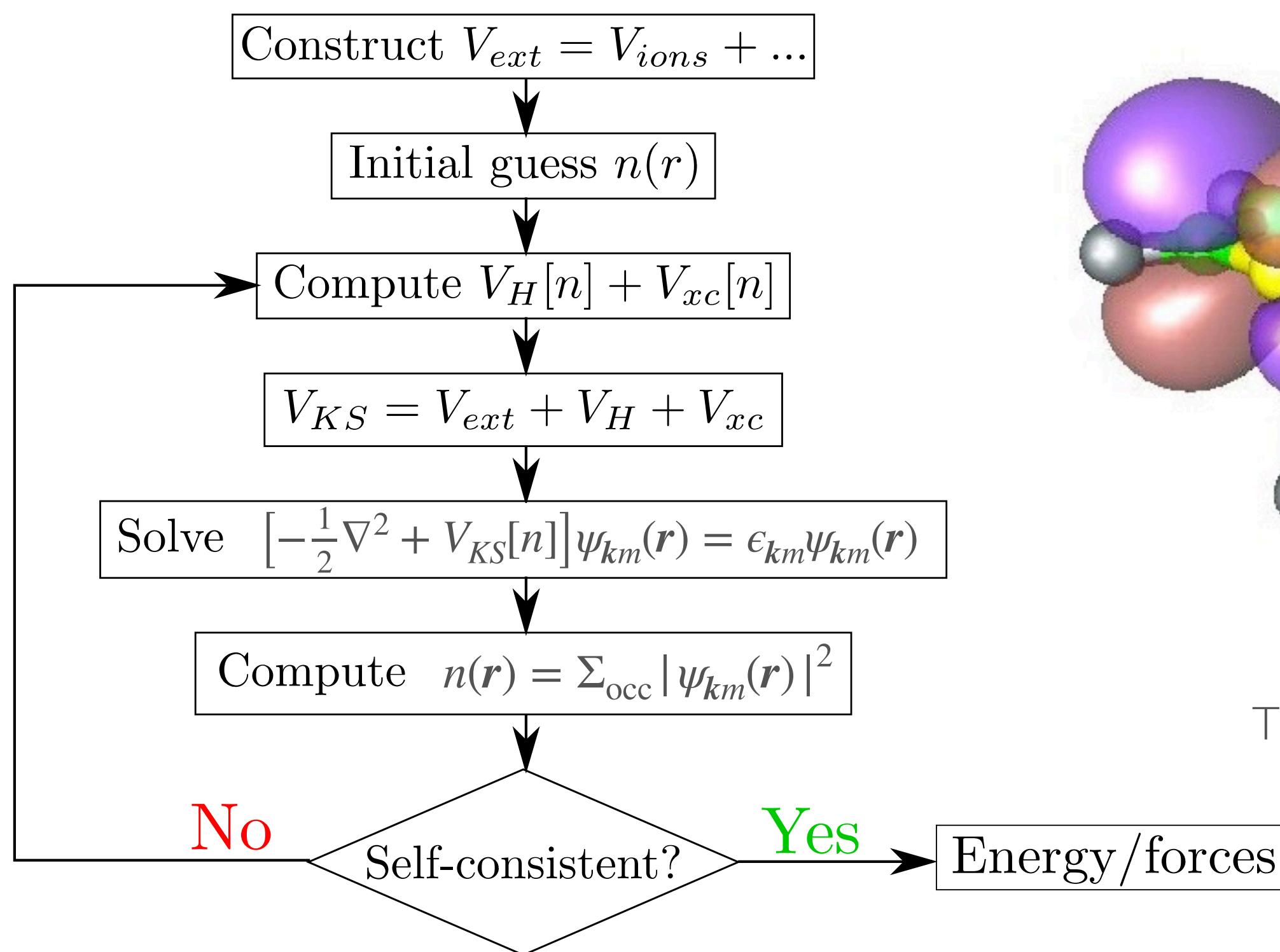
**D3Q**: Phonon-phonon interaction and thermal conductivity

**EPW**: Electron-phonon coefficients and related properties

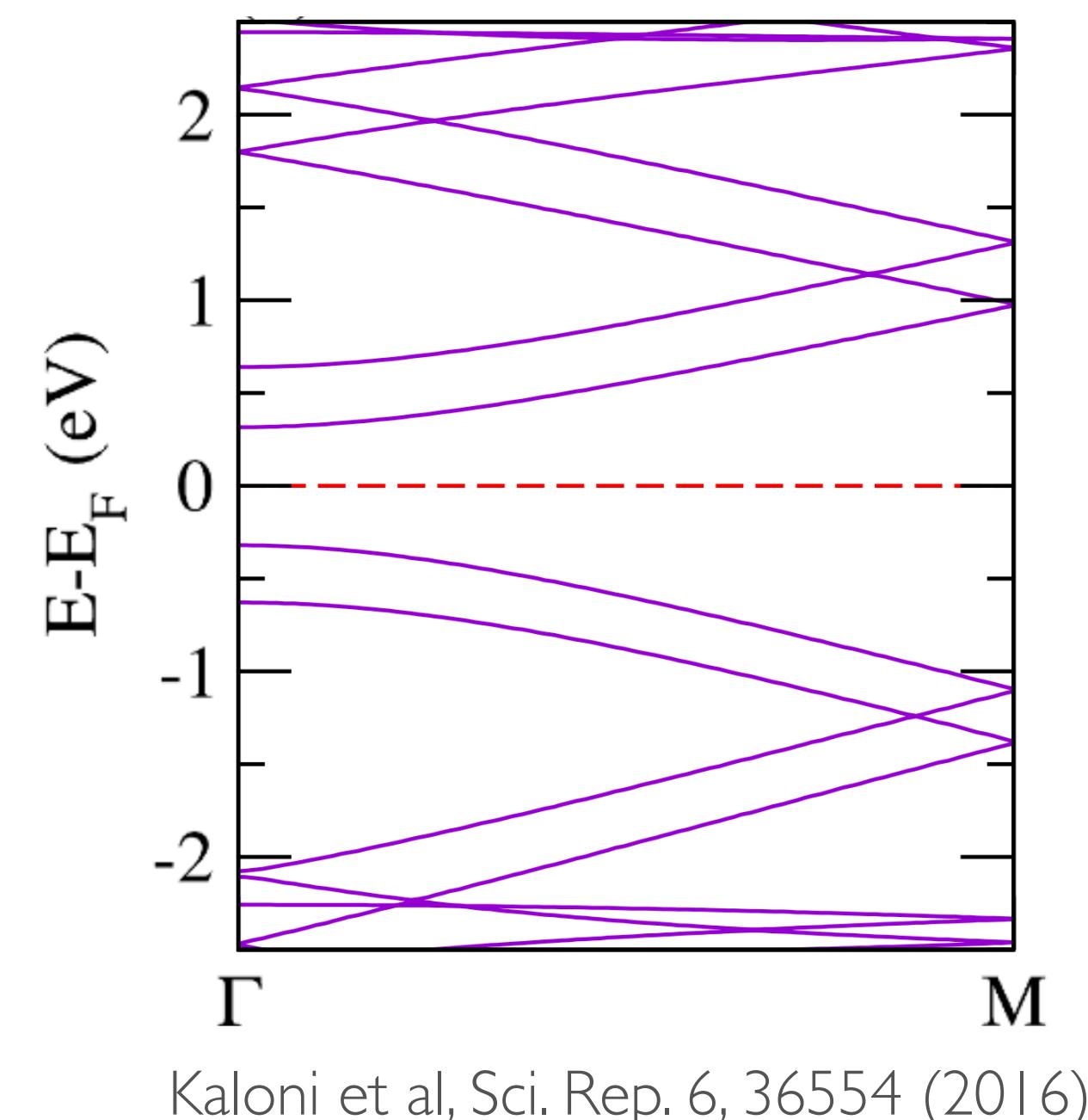
# CHARGE DENSITY AND BAND STRUCTURE

Ground state electronic energy and density,  $n(\mathbf{r}) = \sum_{km \in \text{Occ}} |\psi_{km}(\mathbf{r})|^2$

Self-consistent solution of Kohn Sham equation:  $\left[ -\frac{1}{2}\nabla^2 + V_{\text{ext}} + V_H[n] + V_{xc}[n] \right] \psi_{km}(\mathbf{r}) = \epsilon_{km} \psi_{km}(\mathbf{r})$

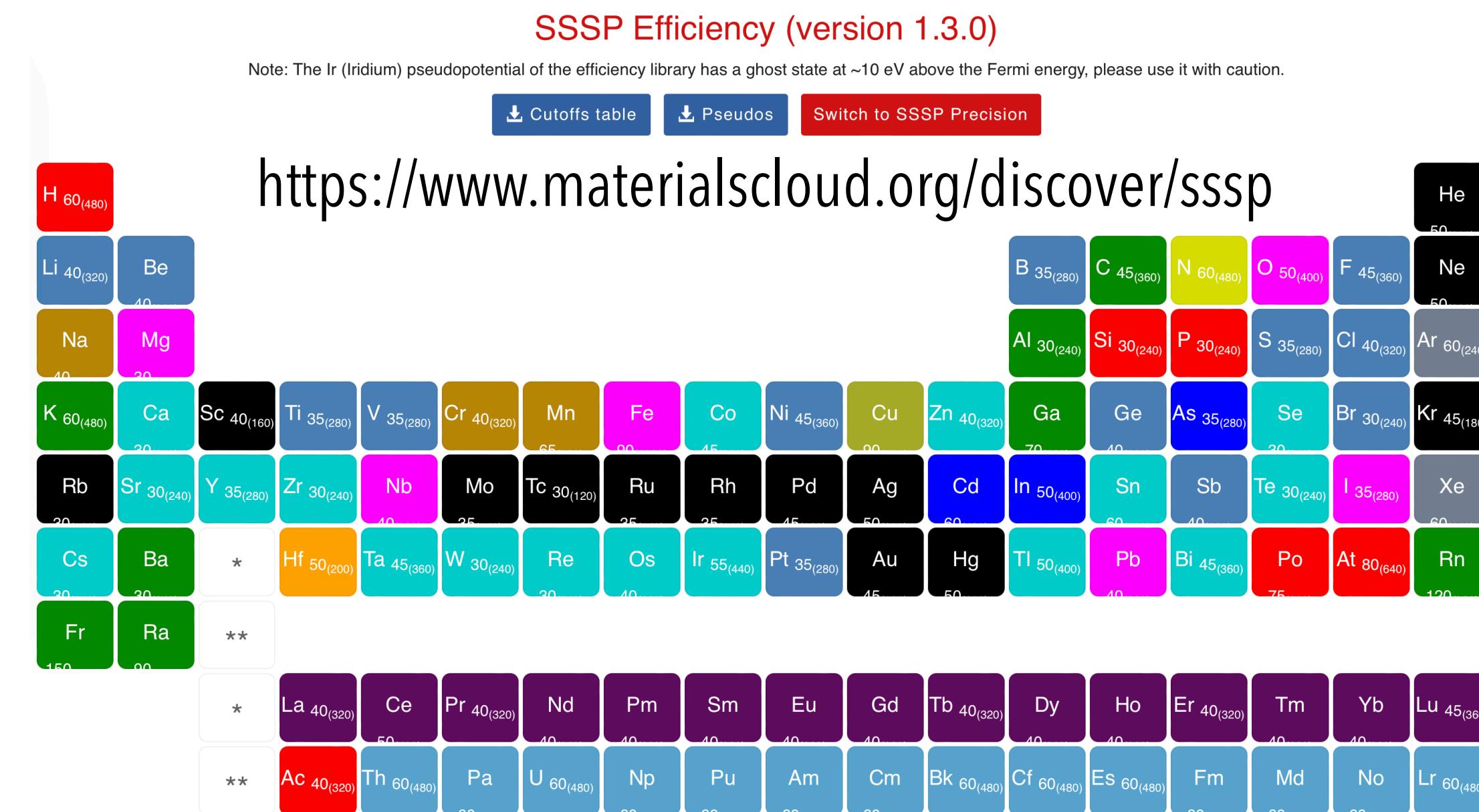
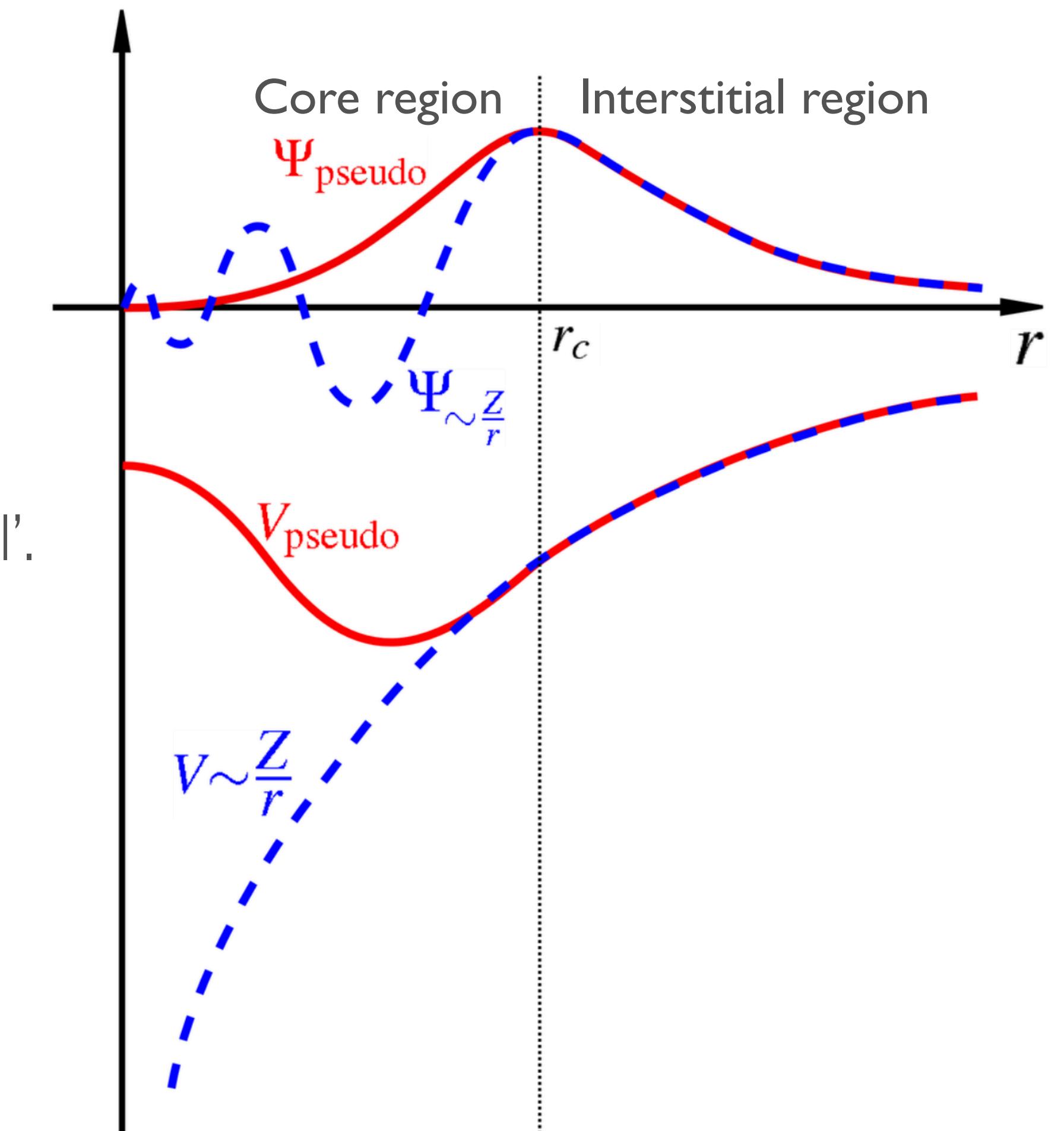


Thiophene ( $C_4H_4S$ ), Scherlis and Marzari, JPCB (2004)



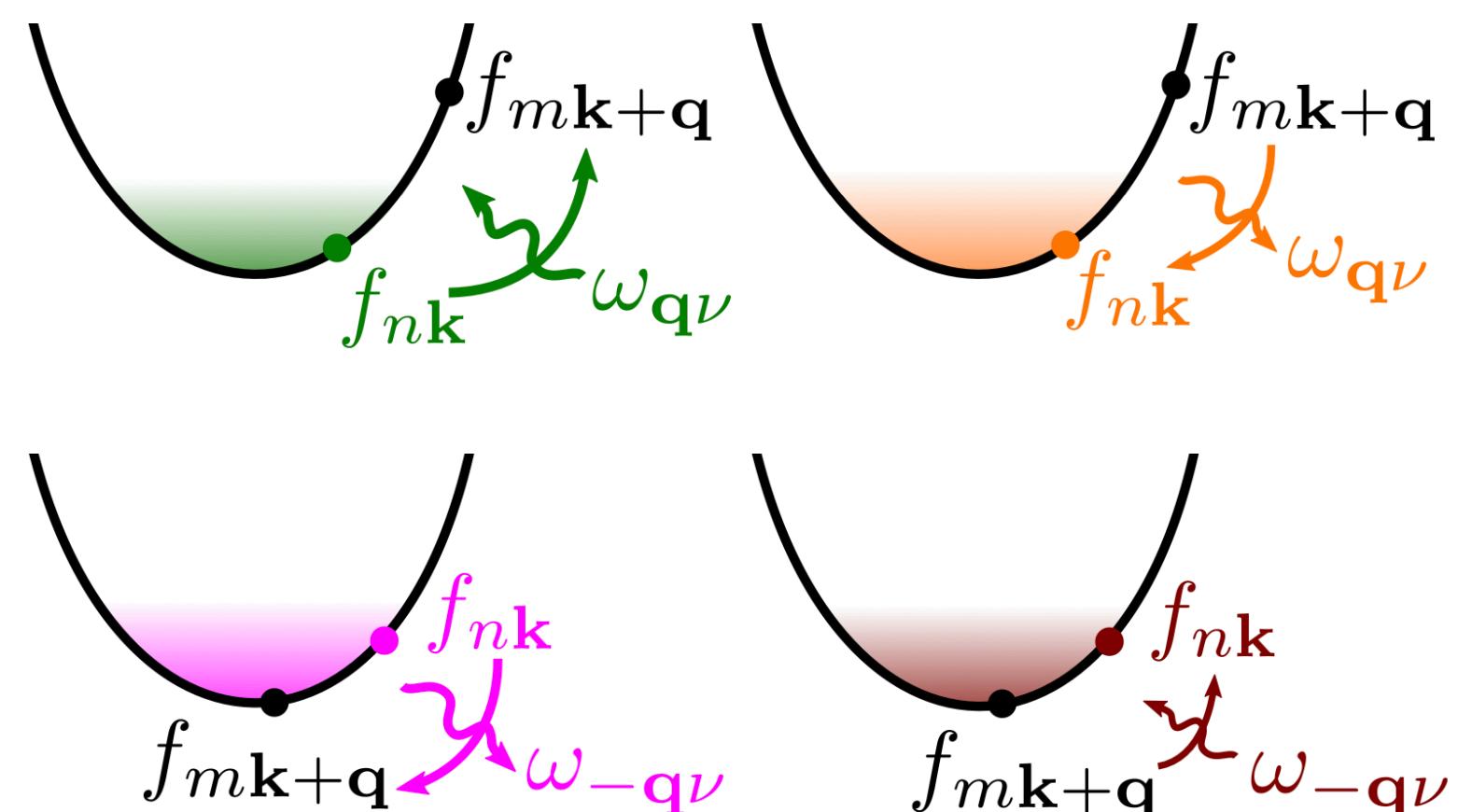
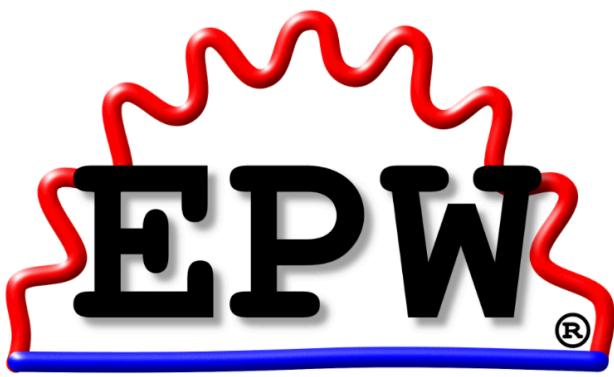
# PSEUDOPOTENTIALS – SSSP LIBRARY

- Valence wavefunctions are ‘soft and smooth’ in the interstitial region, they strongly oscillate in the core region;
  - Bonds are mainly determined by  $\Psi_{km}(\mathbf{r})$  in the interstitial region;
  - Core electrons are very localized;
  - Approximation to reduce computational cost: freeze the core electrons & replace the real ionic potential with a ‘pseudopotential’.



# INTERACTIONS: BROADENING OF BANDS

Electron-phonon interaction

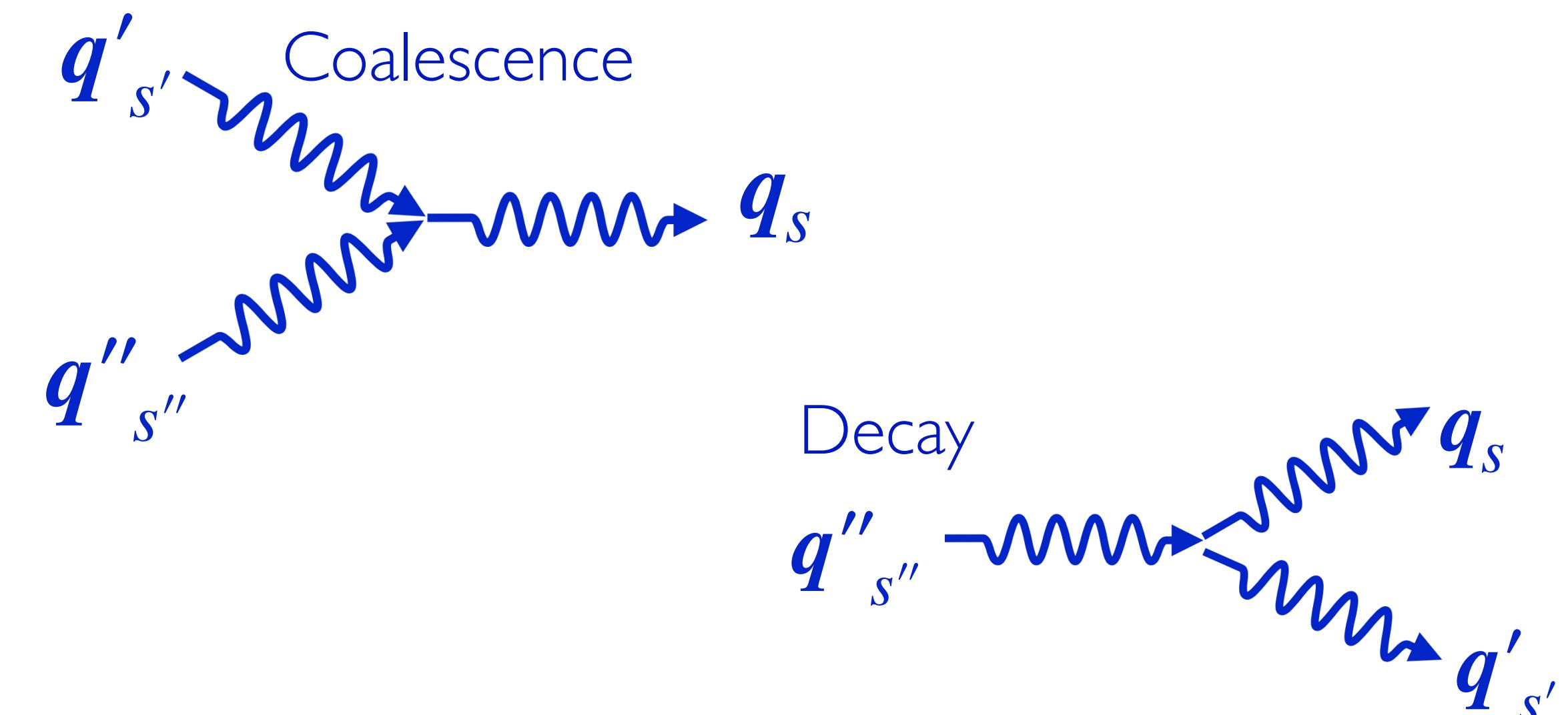


$$\text{Electron-phonon matrix element } g_{m,m',s}(\mathbf{k}, \mathbf{k}', \mathbf{q}) = \sqrt{\frac{\hbar}{2M_0\omega_{qs}}} \left\langle \psi_{k'm'} | \partial_{qs} V | \psi_{km} \right\rangle$$

Self-consistent potential associated with phonon  $\mathbf{q}_s$

Poncé et al. Computer Phys. Commun, 209 (2016)  
 Poncé et al. Rep. Prog. Phys. 83 036501 (2020)

Phonon-phonon interaction



phonon-phonon matrix element

$$| V^{(3)}(\mathbf{q}_s, -\mathbf{q}'_{s'}, -\mathbf{q}''_{s''}) |^2$$

Third derivative of the Born-Oppenheimer potential

Paulatto et al. PRB 87 (2013)  
 Fugallo et al. PRB 88 (2013)

# 'BROADENED' BAND STRUCTURE FROM DFT

Electrons

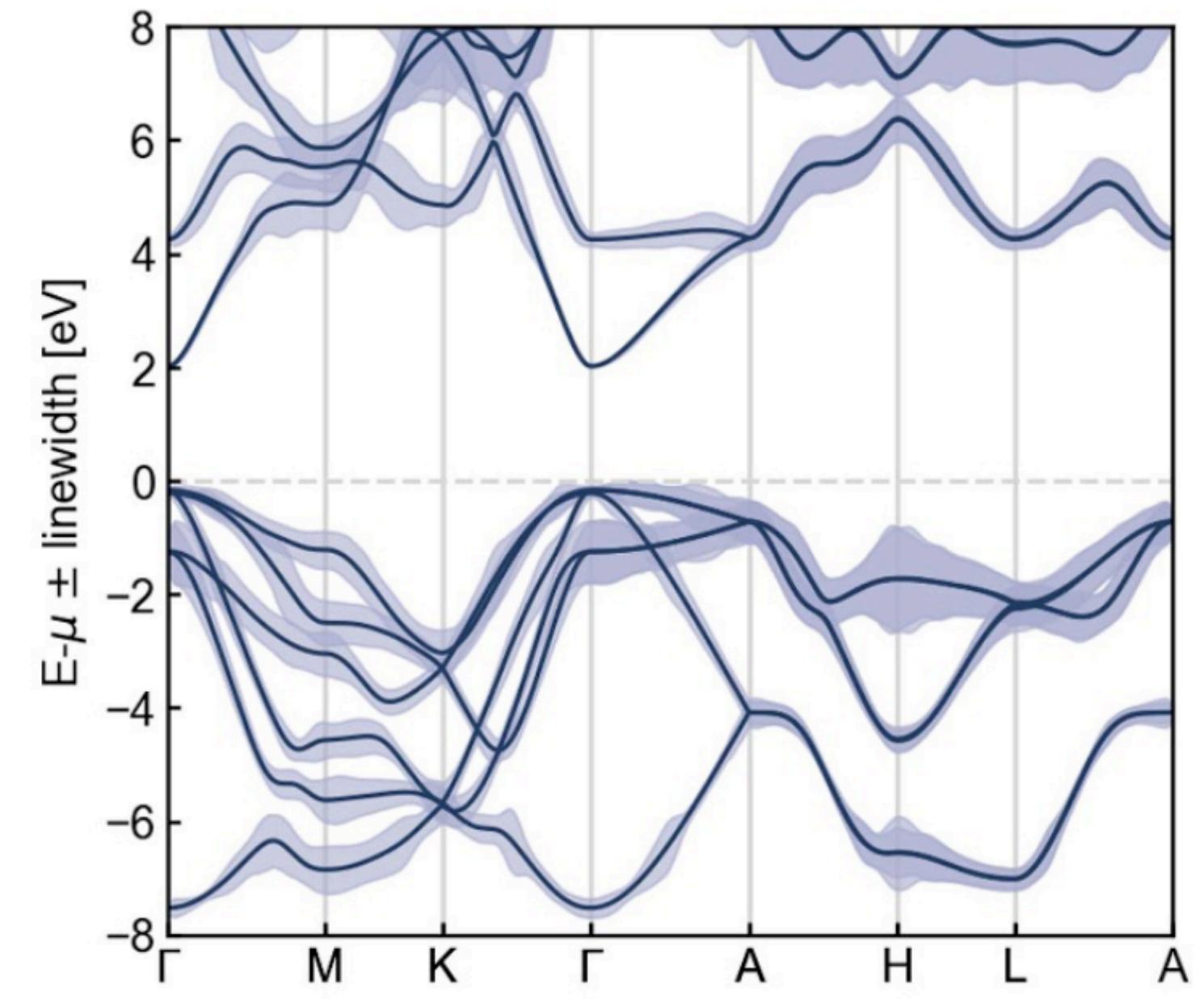
—  $\epsilon(\mathbf{k})_m$

$$\Gamma(\mathbf{k})_m = \frac{1}{\mathcal{N}_k \mathcal{V}} \sum_{\mathbf{k}'' m'', \mathbf{q}s} \frac{2\pi}{\hbar} |g_{m, m'', s}(\mathbf{k}, \mathbf{k}'', \mathbf{q})|^2 \delta_{\mathbf{k}'' - \mathbf{k} - \mathbf{q}, \mathbf{G}} \left[ (\bar{N}(\mathbf{q})_s + \bar{F}(\mathbf{k}'')_{m''}) \right. \\ \times \delta[\epsilon(\mathbf{k}'')_{m''} - \epsilon(\mathbf{k})_m - \hbar\omega(\mathbf{q})_s] + (1 - \bar{F}(\mathbf{k}'')_{m''} + \bar{N}(\mathbf{q})_s) \delta[\epsilon(\mathbf{k}'')_{m''} - \epsilon(\mathbf{k})_m + \hbar\omega(\mathbf{q})_s] \left. \right]$$

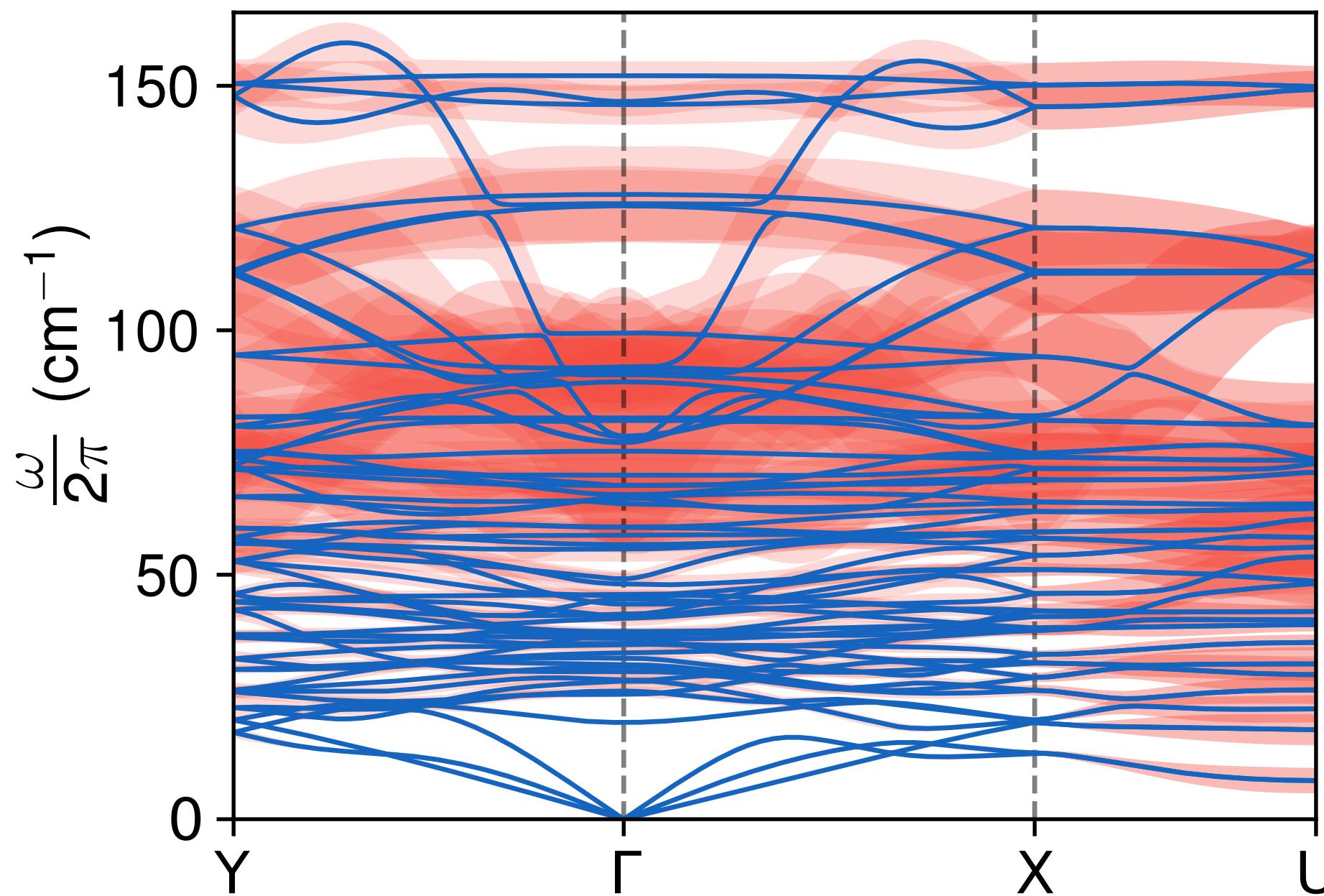
Phonons

—  $\omega(\mathbf{q})_s$

$$\Gamma(\mathbf{q})_s = \frac{36\pi}{\hbar N_q} \sum_{\mathbf{q}, \mathbf{q}', s, s'} |V^{(3)}(\mathbf{q}s, -\mathbf{q}'s', -\mathbf{q}''s'')|^2 \delta_{\mathbf{q} - \mathbf{q}' - \mathbf{q}'', \mathbf{G}} \left[ (\bar{N}_{\mathbf{q}'s'} + \bar{N}_{\mathbf{q}''s''} + 1) \right. \\ \times \delta(\hbar\omega_{qs} - \hbar\omega_{q's'} - \hbar\omega_{q''s''}) + (\bar{N}_{\mathbf{q}'s'} - \bar{N}_{\mathbf{q}''s''}) [\delta(\hbar\omega_{qs} + \hbar\omega_{q's'} - \hbar\omega_{q''s''}) - \delta(\hbar\omega_{qs} - \hbar\omega_{q's'} + \hbar\omega_{q''s''})] \left. \right]$$



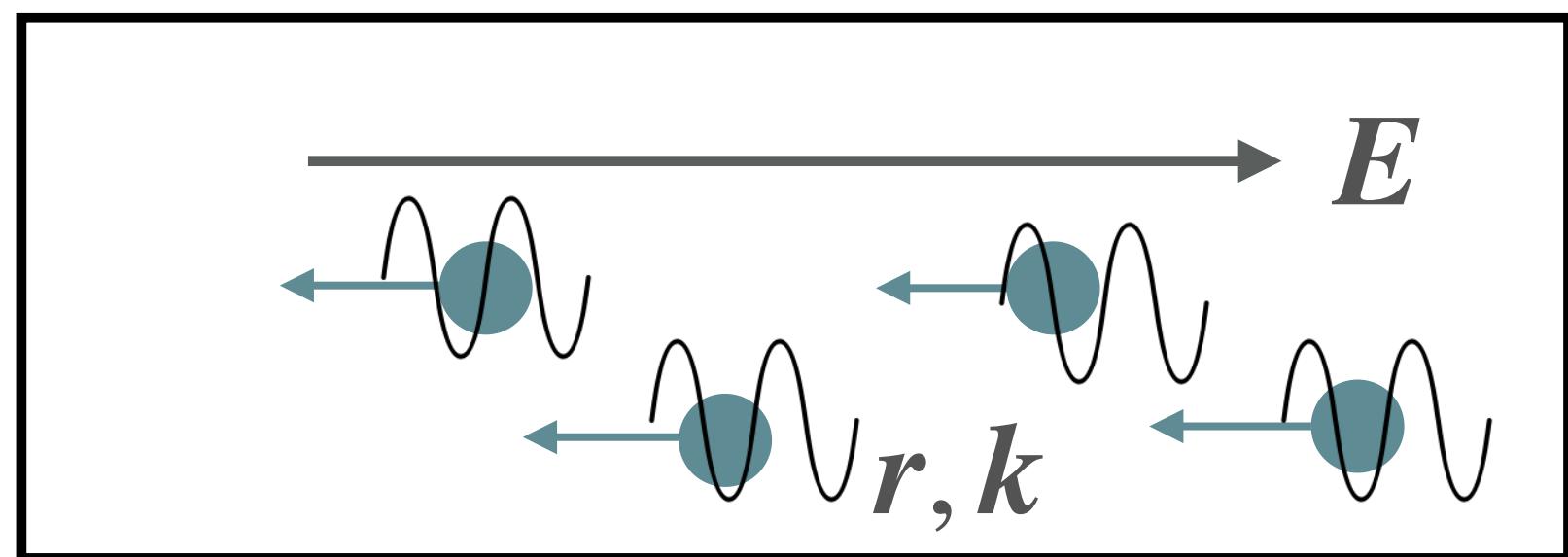
GaN, from Cepellotti et al, J. Phys. Mater. 5 (2022)



$\text{CsPbBr}_3$ , from Simoncelli, Marzari, Mauri, Nat. Phys. 15 (2019)

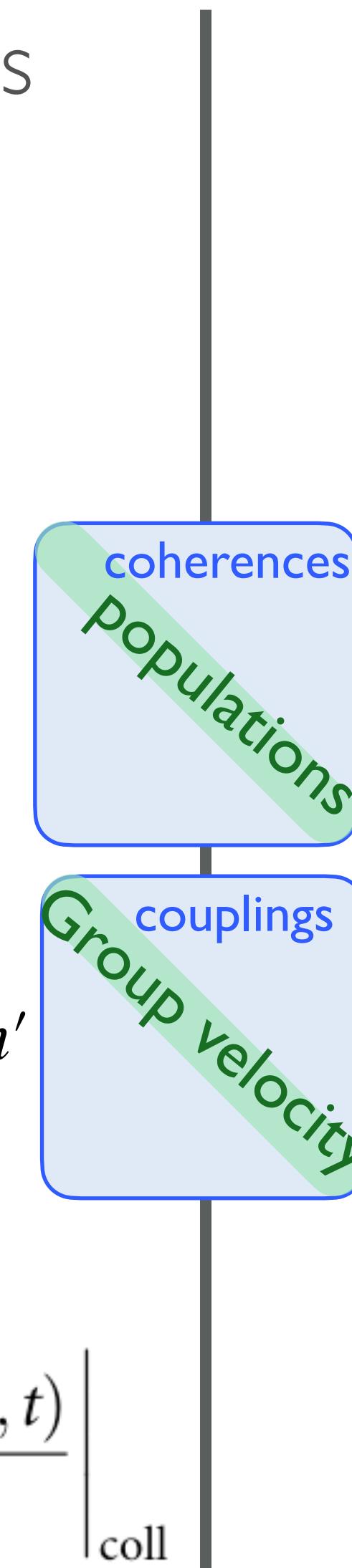
# FROM BAND STRUCTURE TO TRANSPORT COEFFICIENTS

Wigner transport equation for electrons

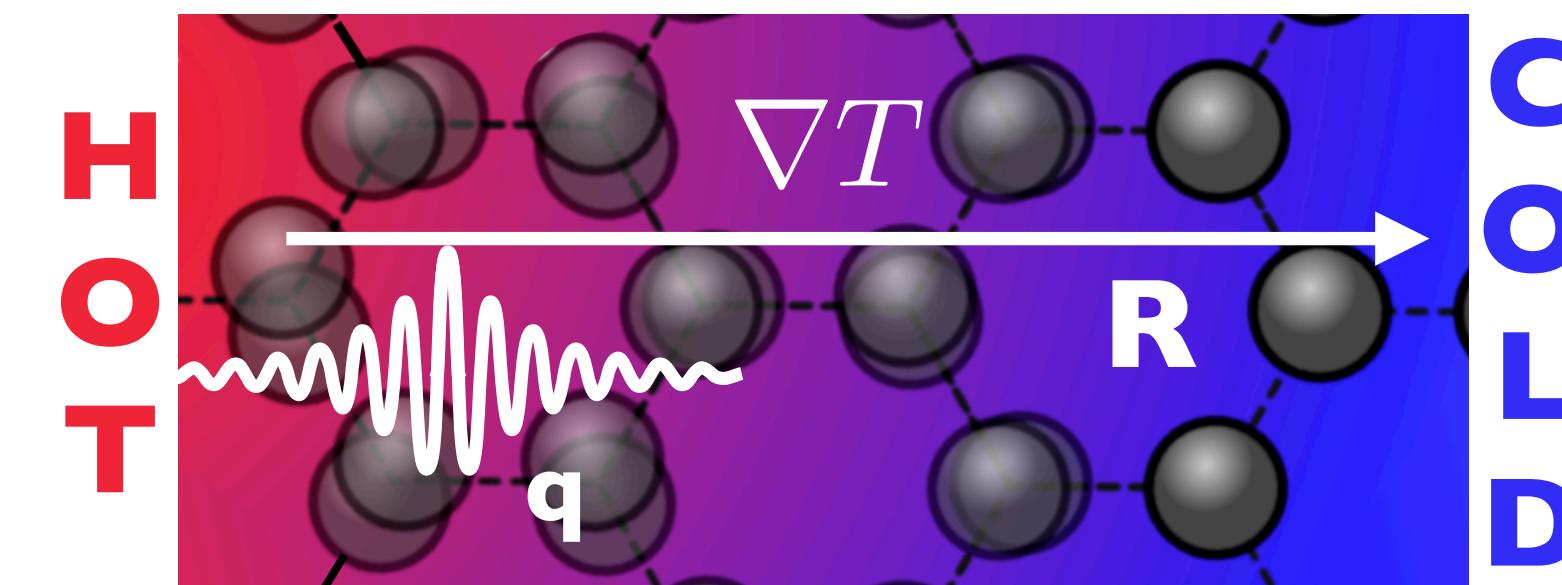


electron Wigner distribution  $F(\mathbf{r}, \mathbf{k}, t)_{m,m'}$

At equilibrium, diagonal elements = Fermi-Dirac



Wigner transport equation for phonons



$N(\mathbf{R}, \mathbf{q}, t)_{s,s'}$  phonon Wigner distribution

At equilibrium, diagonal elements = Bose-Einstein

$\mathbf{V}(\mathbf{q})_{s,s'}$  Phonon velocity operator (diagonal  $\frac{\partial \omega(\mathbf{q})_s}{\partial \mathbf{q}}$ )

$$\frac{\partial}{\partial t} \mathbf{N}(\mathbf{R}, \mathbf{q}, t) + i [\Omega(\mathbf{q}), \mathbf{N}(\mathbf{R}, \mathbf{q}, t)] +$$

$$+ \frac{1}{2} \left\{ \vec{\mathbf{V}}(\mathbf{q}), \cdot \vec{\nabla}_{\mathbf{R}} \mathbf{N}(\mathbf{R}, \mathbf{q}, t) \right\} = \frac{\partial}{\partial t} \mathbf{N}(\mathbf{R}, \mathbf{q}, t) \Big|_{\text{H}^{\text{col}}}$$

Iafrate, Sokolov, Krieger, Phys. Rev. B 96, 144303 (2017);  
Cepellotti & Kozinsky, Materials Today Physics 19 (2021) 100412

Simoncelli, Marzari and Mauri, Nat. Phys. 15 (2019)  
Simoncelli, Marzari and Mauri, Phys. Rev. X 12 (2022)

# WIGNER CONDUCTIVITIES FOR ELECTRONS AND PHONONS

linear response in  $\nabla T$  of phonon Wigner equation yields the heat flux  $\mathbf{Q}$ , thus thermal conductivity ( $\mathbf{Q} = -\kappa \nabla T$ )

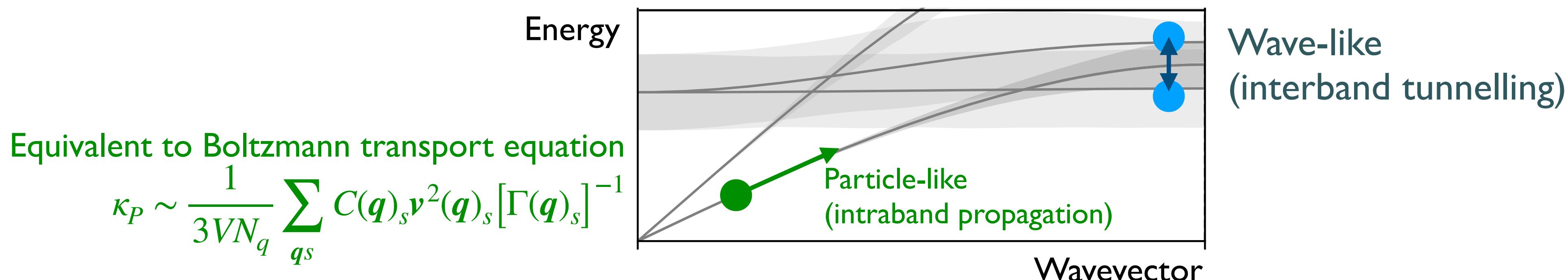
$$\kappa^{\alpha\beta} = \kappa_P^{\alpha\beta} + \frac{1}{VN_q} \sum_{q,s \neq s'} \frac{\omega(\mathbf{q})_s + \omega(\mathbf{q})_{s'}}{4} \left[ \frac{C(\mathbf{q})_s}{\omega(\mathbf{q})_s} + \frac{C(\mathbf{q})_{s'}}{\omega(\mathbf{q})_{s'}} \right] v^\alpha(\mathbf{q})_{s,s'} v^\beta(\mathbf{q})_{s',s} \frac{\frac{1}{2} [\Gamma(\mathbf{q})_s + \Gamma(\mathbf{q})_{s'}]}{[\omega(\mathbf{q})_{s'} - \omega(\mathbf{q})_s]^2 + \frac{1}{4} [\Gamma(\mathbf{q})_s + \Gamma(\mathbf{q})_{s'}]^2}$$

*Simoncelli, Marzari and Mauri, Nat. Phys. 15 (2019)*

linear response in  $\mathbf{E}$  of electron Wigner equation yields the charge current  $\mathbf{J}$ , thus electrical conductivity  $\mathbf{J} = -\sigma \mathbf{E}$

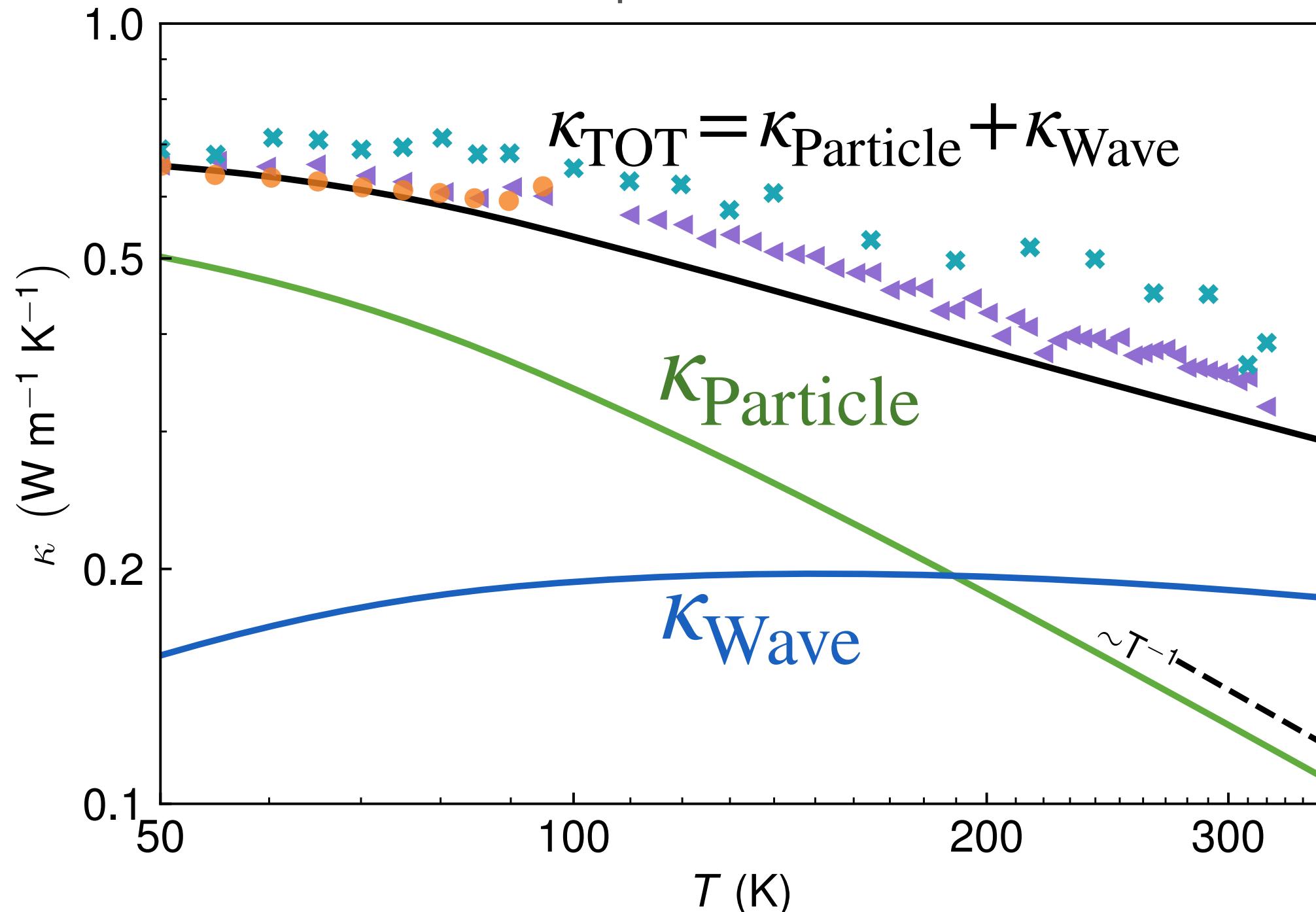
$$\sigma^{\alpha\beta} = \sigma_P^{\alpha\beta} + \frac{g_s}{VN_k} \sum_{k,m \neq m'} \frac{f(\mathbf{k}')_{m'} - f(\mathbf{k})_m}{\epsilon(\mathbf{k}')_{m'} - \epsilon(\mathbf{k})_m} v^\alpha(\mathbf{k})_{m,m'} v^\beta(\mathbf{k})_{m',m} \frac{\frac{1}{2} [\Gamma(\mathbf{k})_m + \Gamma(\mathbf{k})_{m'}]}{[\epsilon(\mathbf{k})_{m'} - \epsilon(\mathbf{k})_m]^2 + \frac{1}{4} [\Gamma(\mathbf{k})_m + \Gamma(\mathbf{k})_{m'}]^2}$$

*Cepellotti and Kozinsky, Materials Today Physics 19 (2021)*



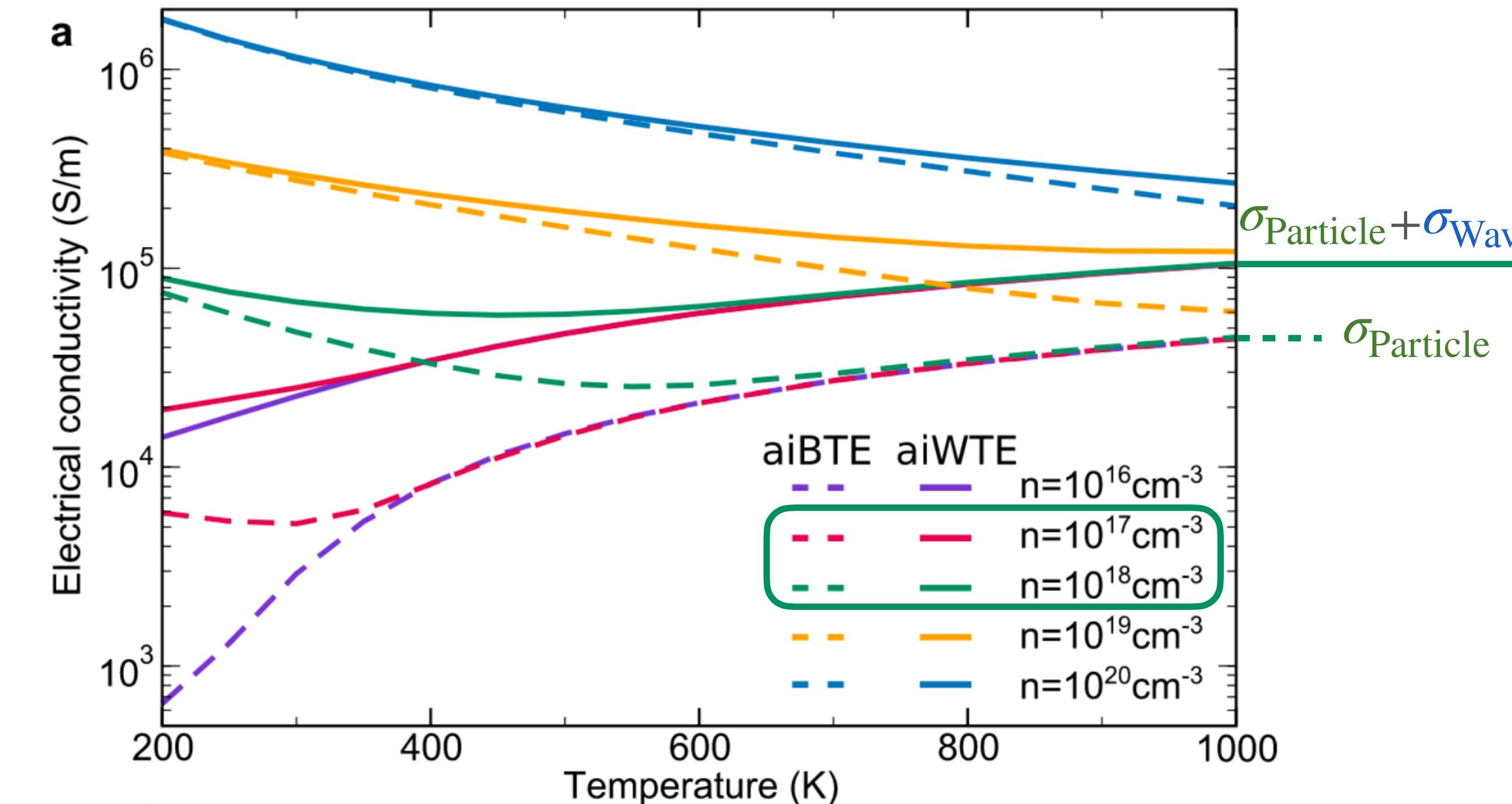
# DUAL WAVE-PARTICLE TRANSPORT

Phonon transport in  $\text{CsPbBr}_3$



*Simoncelli, Marzari, Mauri, Nat. Phys. 15 (2019)*

Electron transport in  $\text{Bi}_2\text{Se}_3$



*Cepellotti and Kozinsky, Materials Today Physics 19 (2021)*

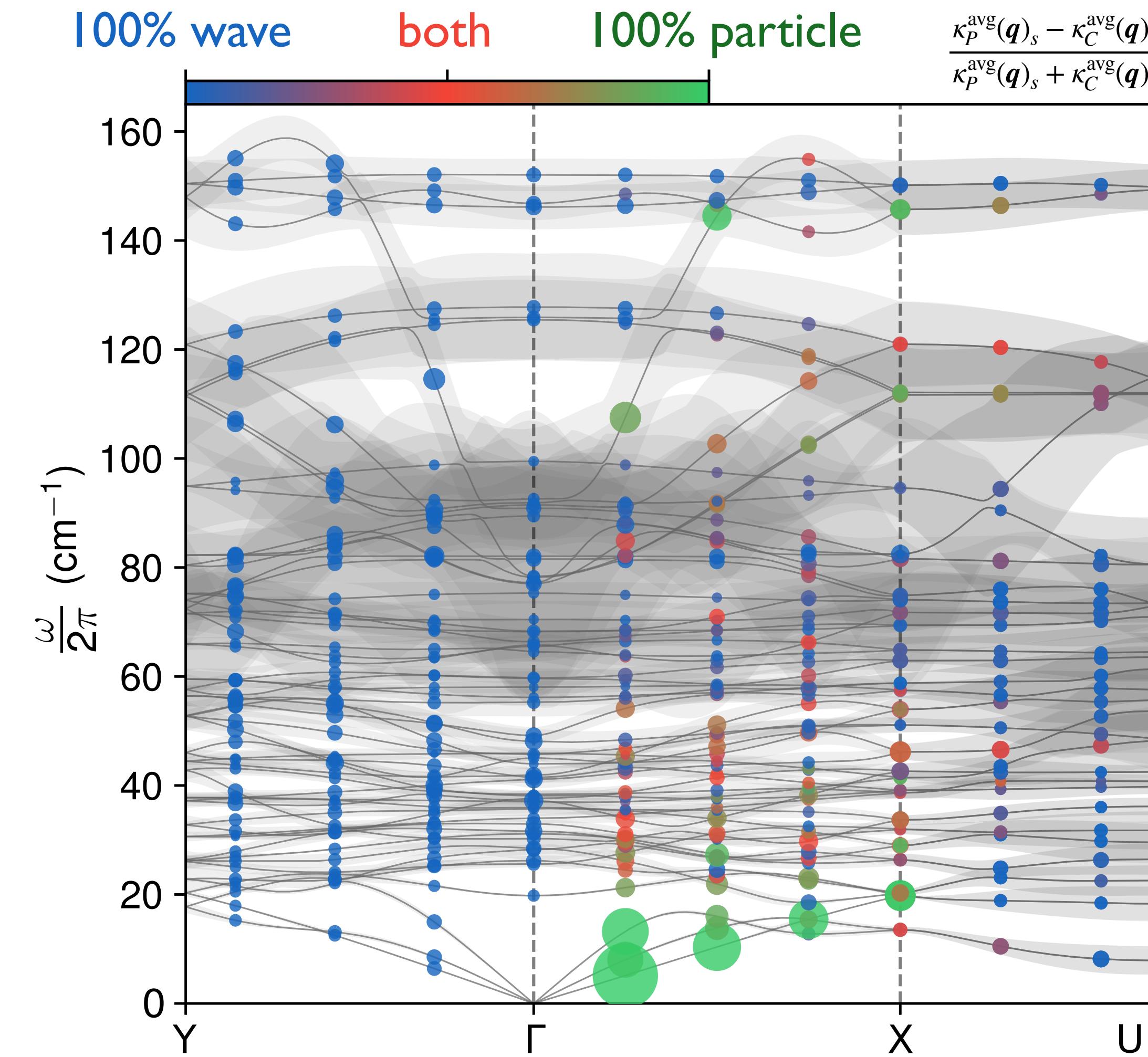


or phono3py  
or ALAMODE  
or Phoebe



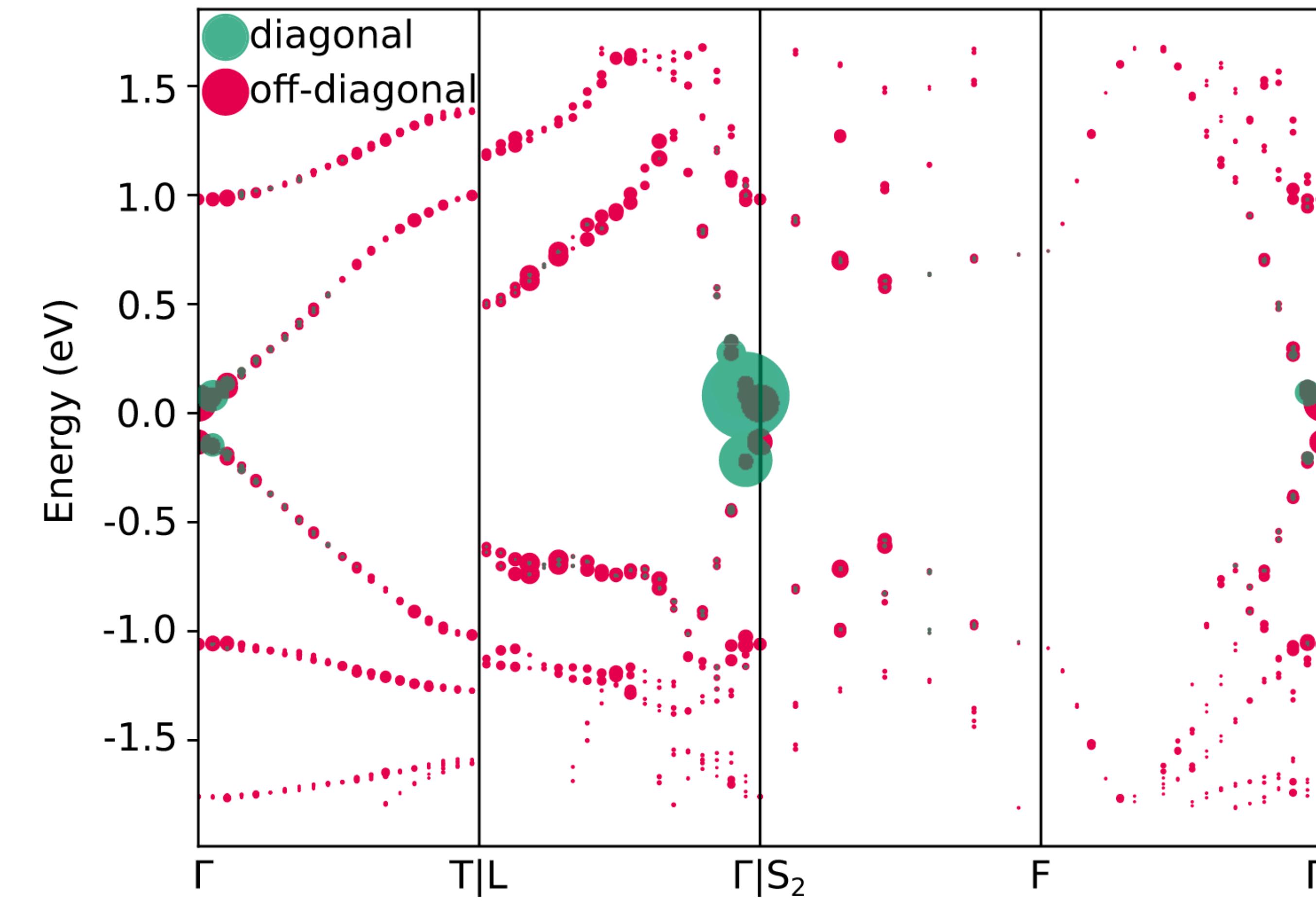
# DUAL WAVE-PARTICLE TRANSPORT

Phonon transport in  $\text{CsPbBr}_3$



Simoncelli, Marzari, Mauri, Nat. Phys. 15 (2019)

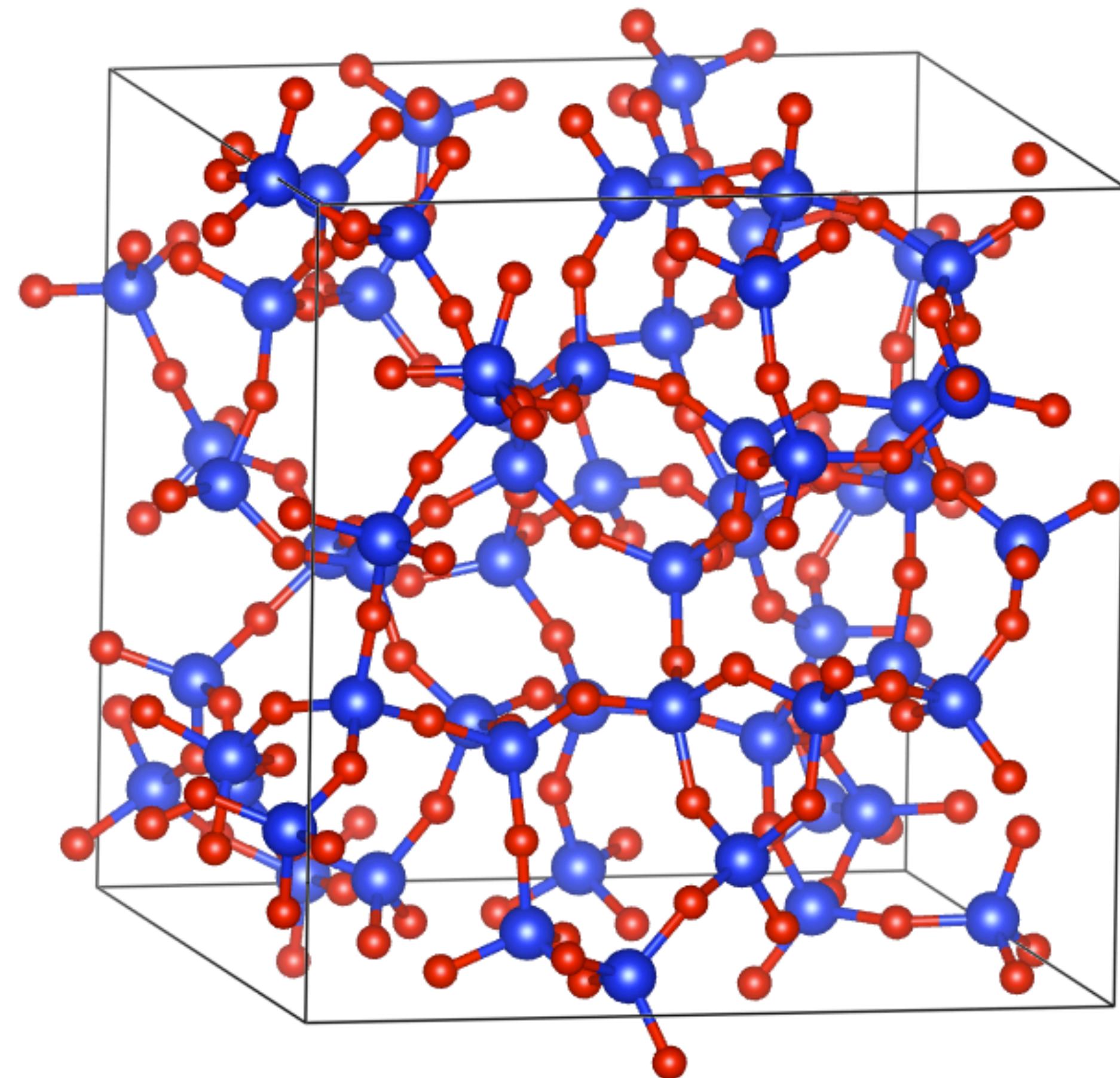
Electron transport in  $\text{Bi}_2\text{Se}_3$



Cepellotti and Kozinsky, Materials Today Physics 19 (2021)

# BEYOND BAND TRANSPORT

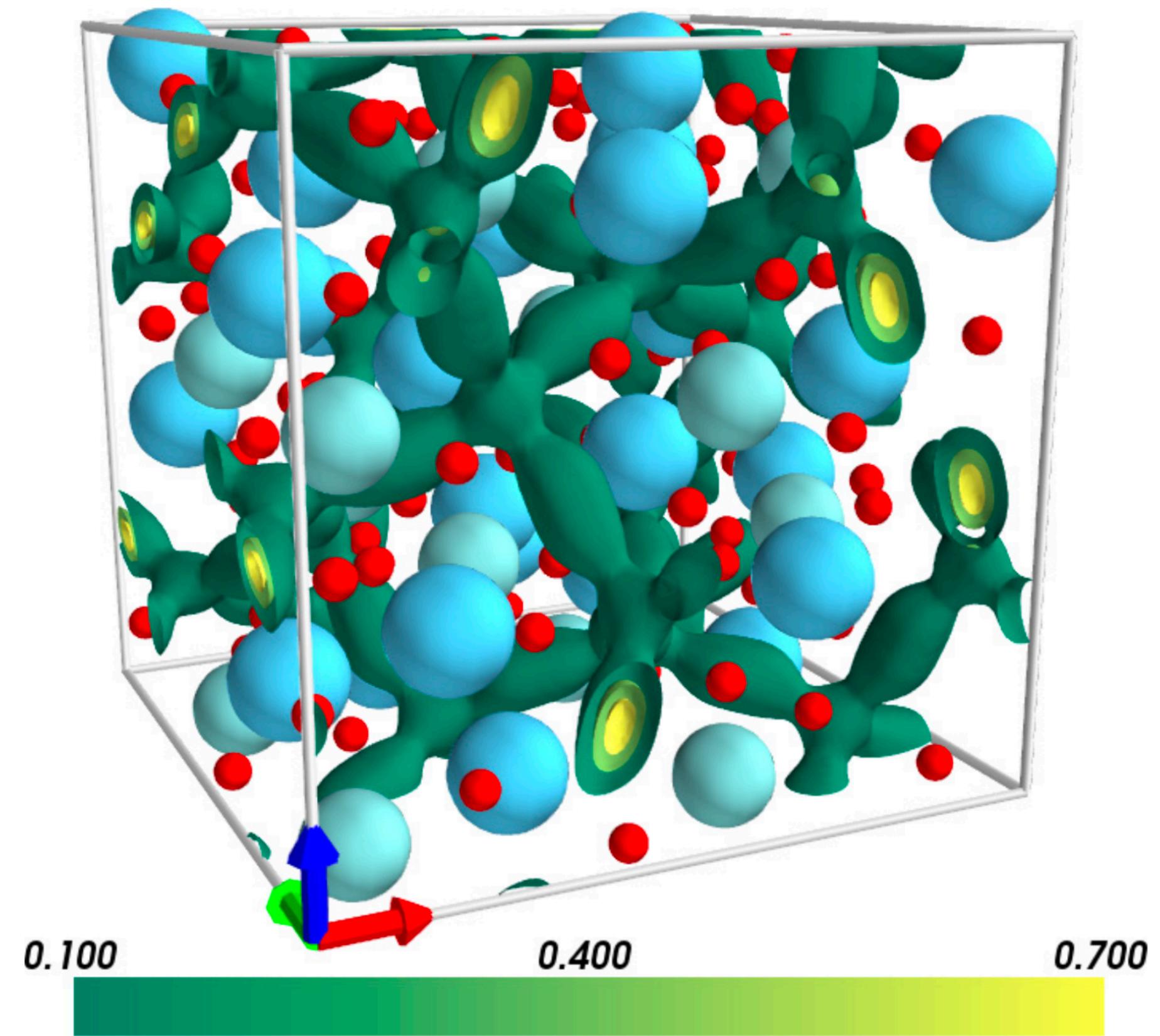
Heat transfer in amorphous solids



Atomistic model of SiO<sub>2</sub> generated from first principles

*Simoncelli, Mauri, Marzari, npj Comput. Mater. 9 (2023);*

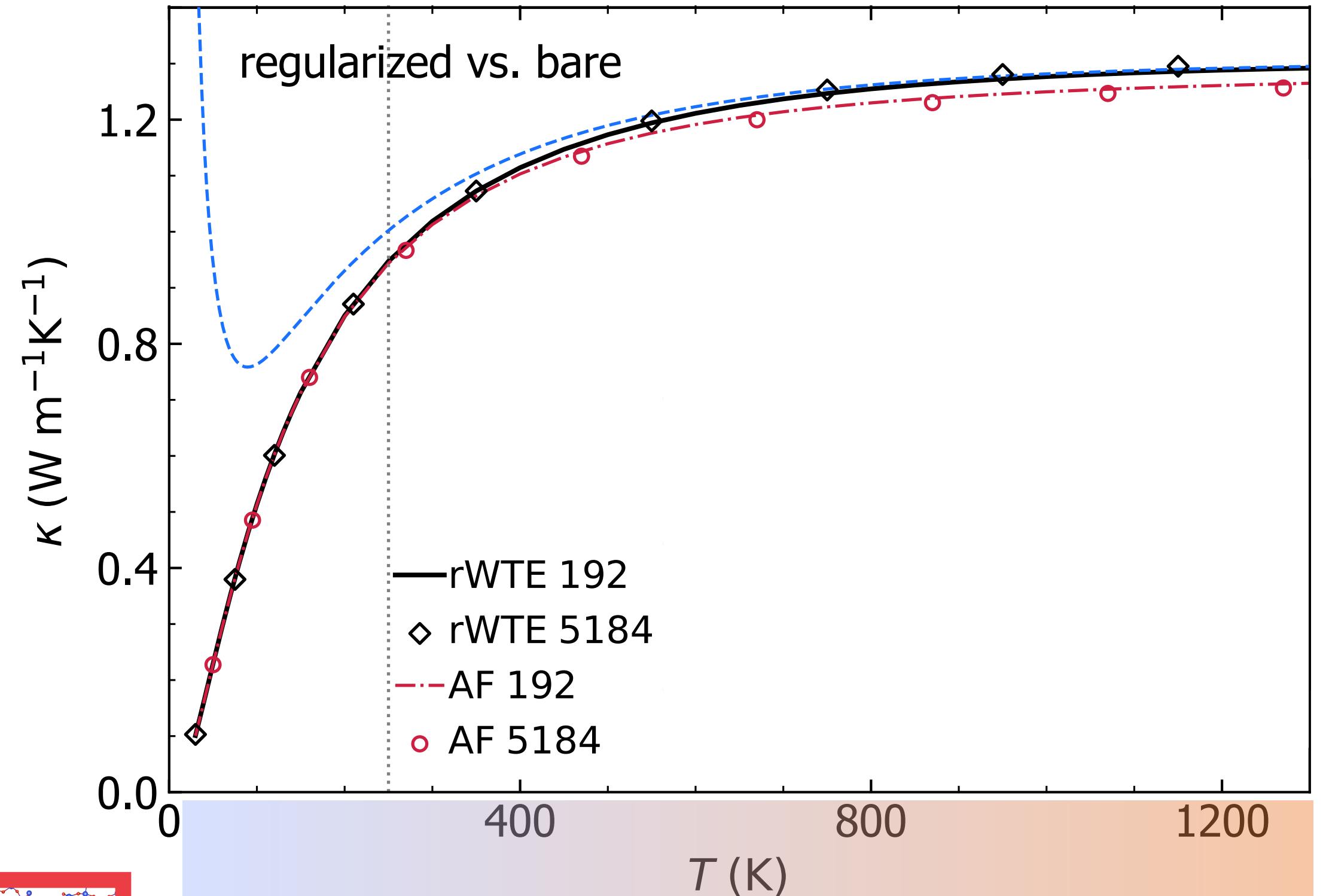
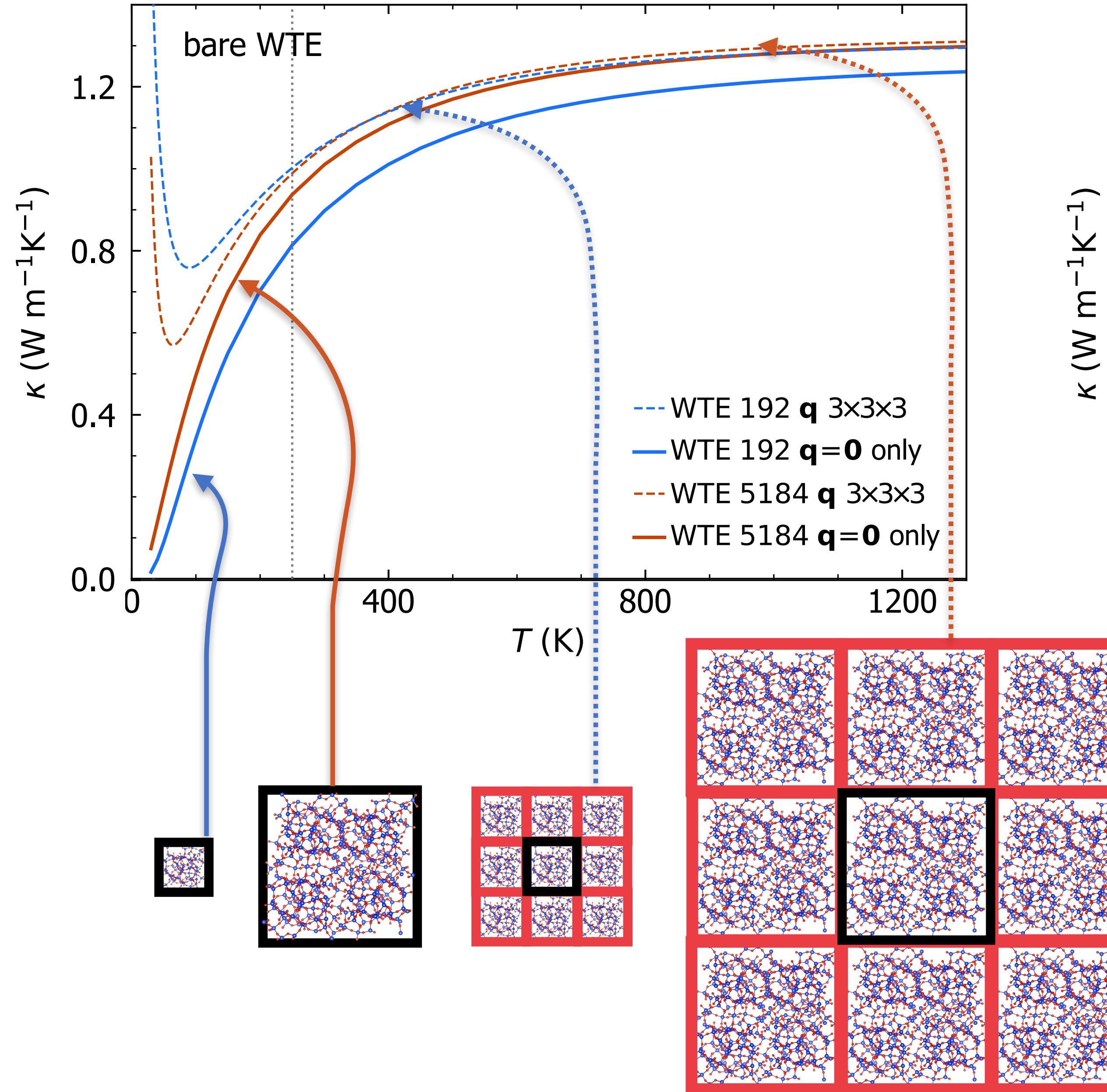
Charge transfer in solid-state ionic conductors



Li-Ion percolation pathways in Li<sub>7</sub>La<sub>3</sub>Zr<sub>2</sub>O<sub>12</sub>

Kahle et al., Phys. Rev. Materials 3, 055404 (2019)

# PROTOCOL FOR HEAT TRANSPORT IN GLASSES



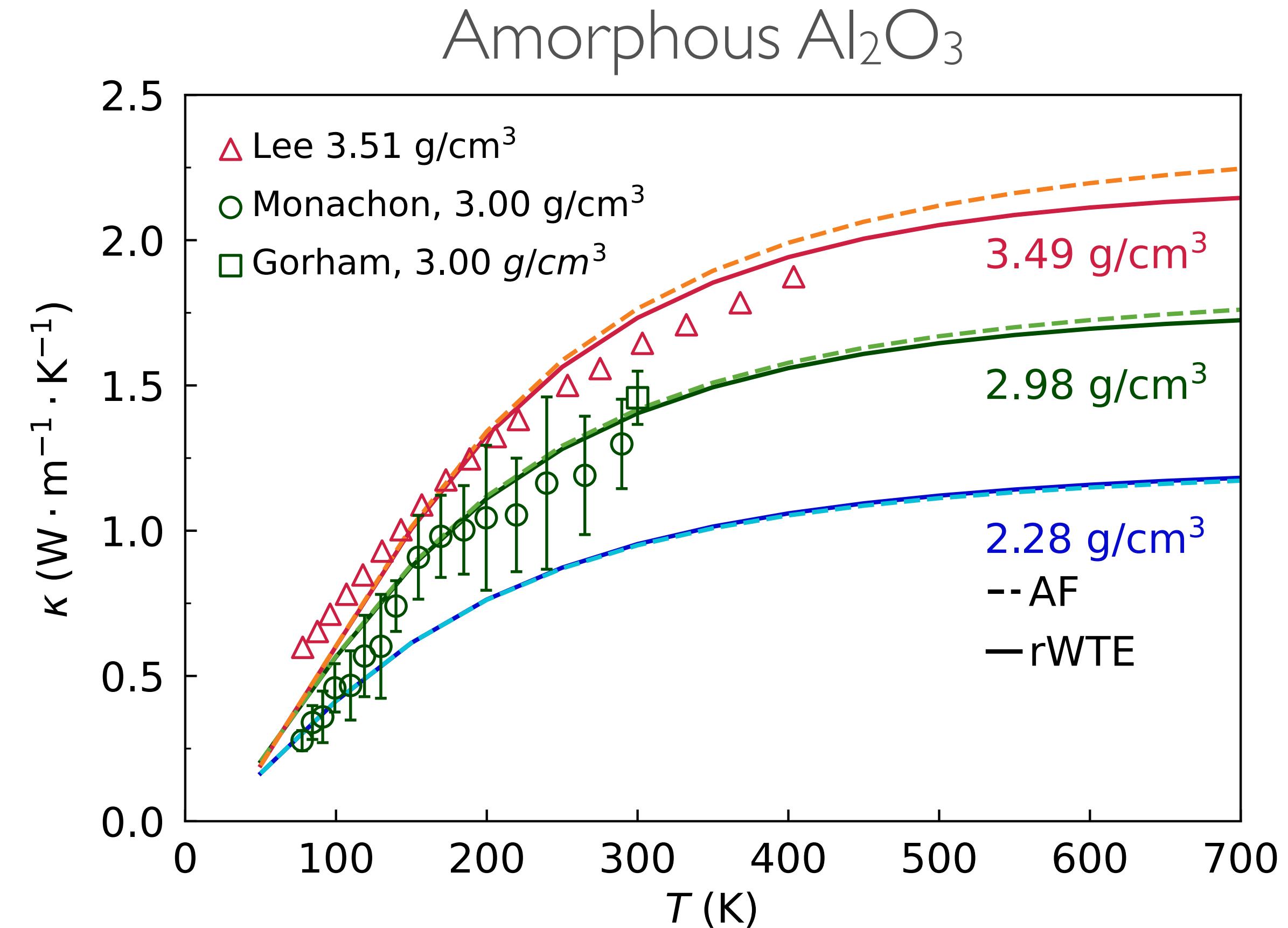
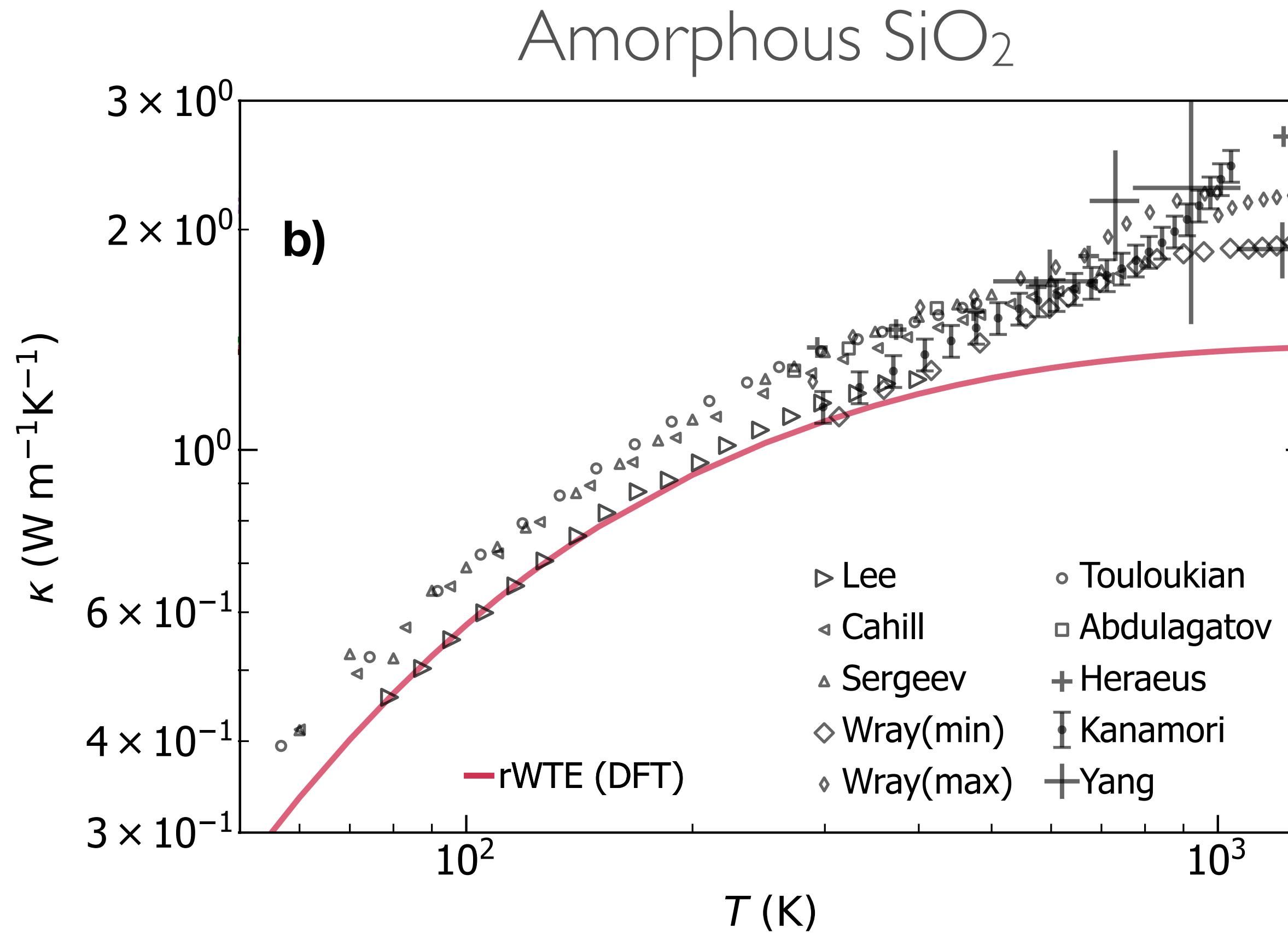
$$\frac{1}{\sqrt{2\pi}\eta} e^{-\frac{(\omega(\mathbf{q})_s - \omega(\mathbf{q})_{s'})^2}{2\eta^2}}$$

$$\frac{1}{\pi} \frac{\frac{1}{2}(\Gamma(\mathbf{q})_s + \Gamma(\mathbf{q})_{s'})}{(\omega(\mathbf{q})_s - \omega(\mathbf{q})_{s'})^2 + \frac{1}{4}(\Gamma(\mathbf{q})_s + \Gamma(\mathbf{q})_{s'})^2}$$

Voigt profile  $\mathcal{F}_{[\eta; \Gamma(\mathbf{q})_s + \Gamma(\mathbf{q})_{s'}]}(\omega(\mathbf{q})_s - \omega(\mathbf{q})_{s'})$

Arrows indicate the components of the Voigt profile:  $\Gamma(\mathbf{q})_s \nearrow \eta$  and  $\Gamma(\mathbf{q})_{s'} \nearrow \eta$ .

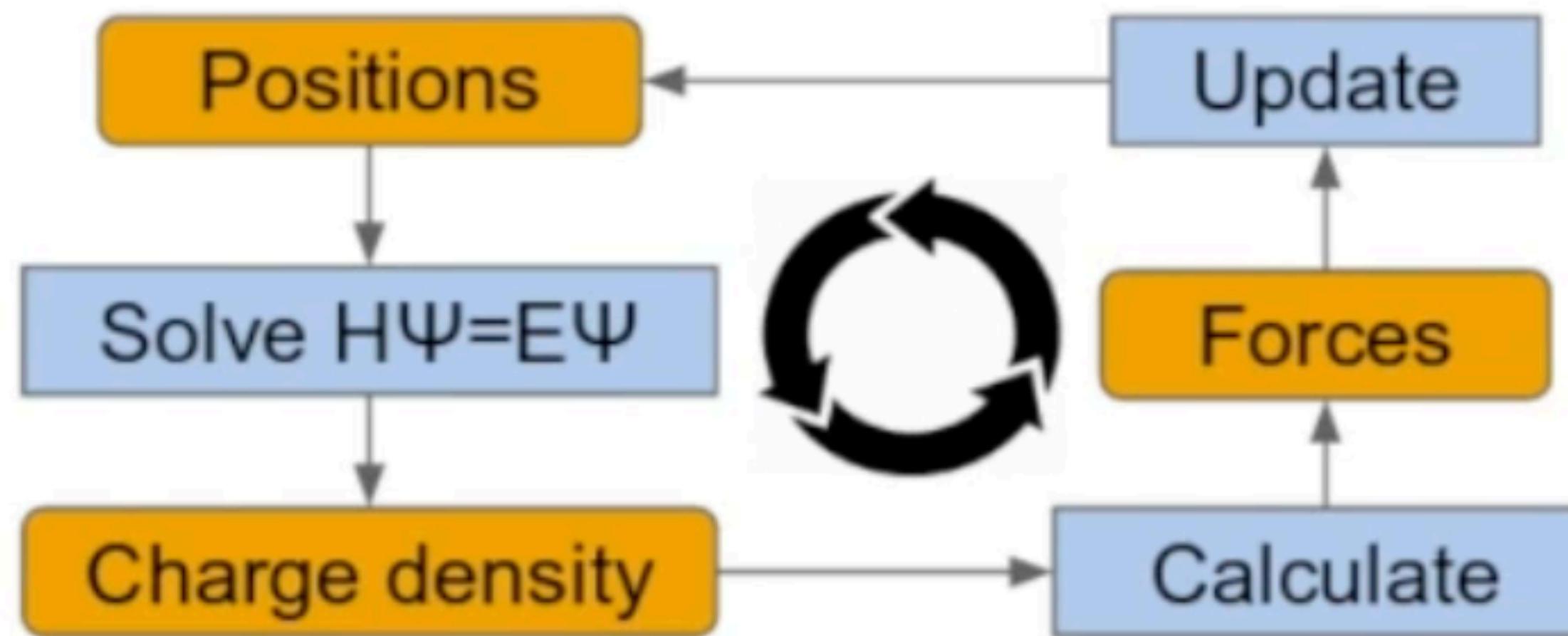
# CONDUCTIVITY OF GLASSES FROM FIRST PRINCIPLES



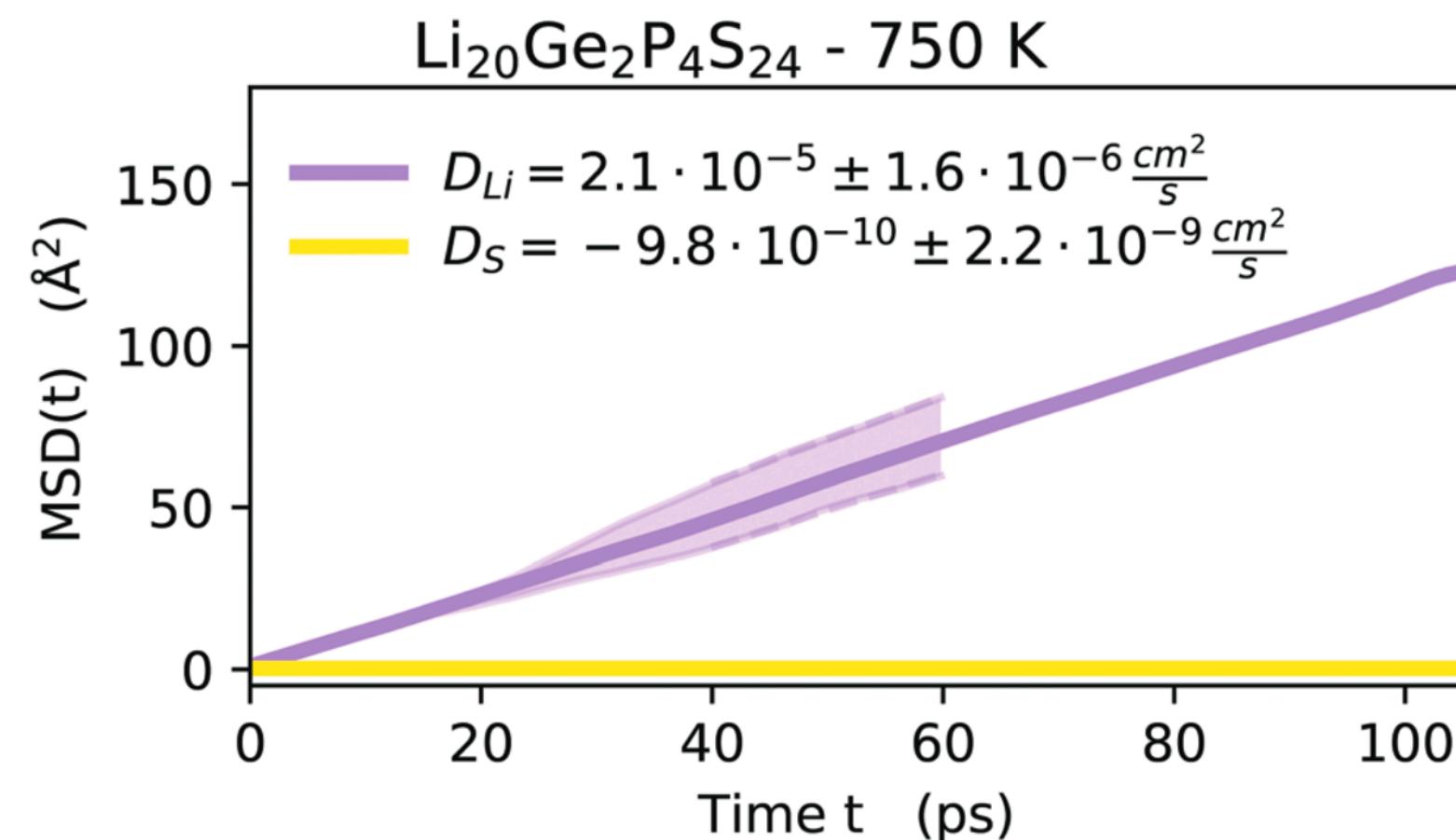
Simoncelli, Mauri, Marzari, *npj Comput. Mater.* 9 (2023)

Harper, Iwanowski, Payne, Simoncelli *arXiv* 2303.08637 (2023)

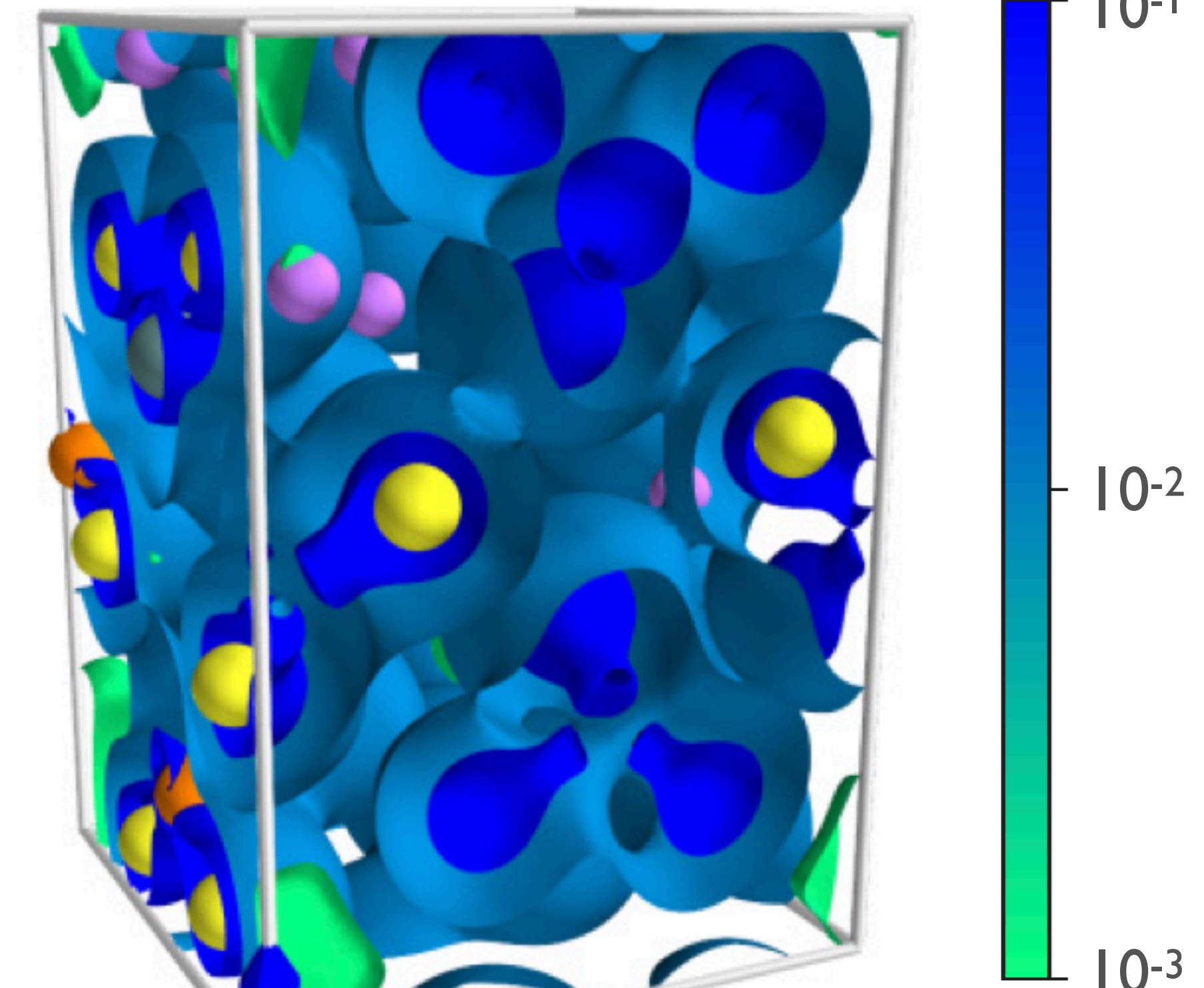
# IONIC DIFFUSIVITY FROM AB INITIO MOLECULAR DYNAMICS

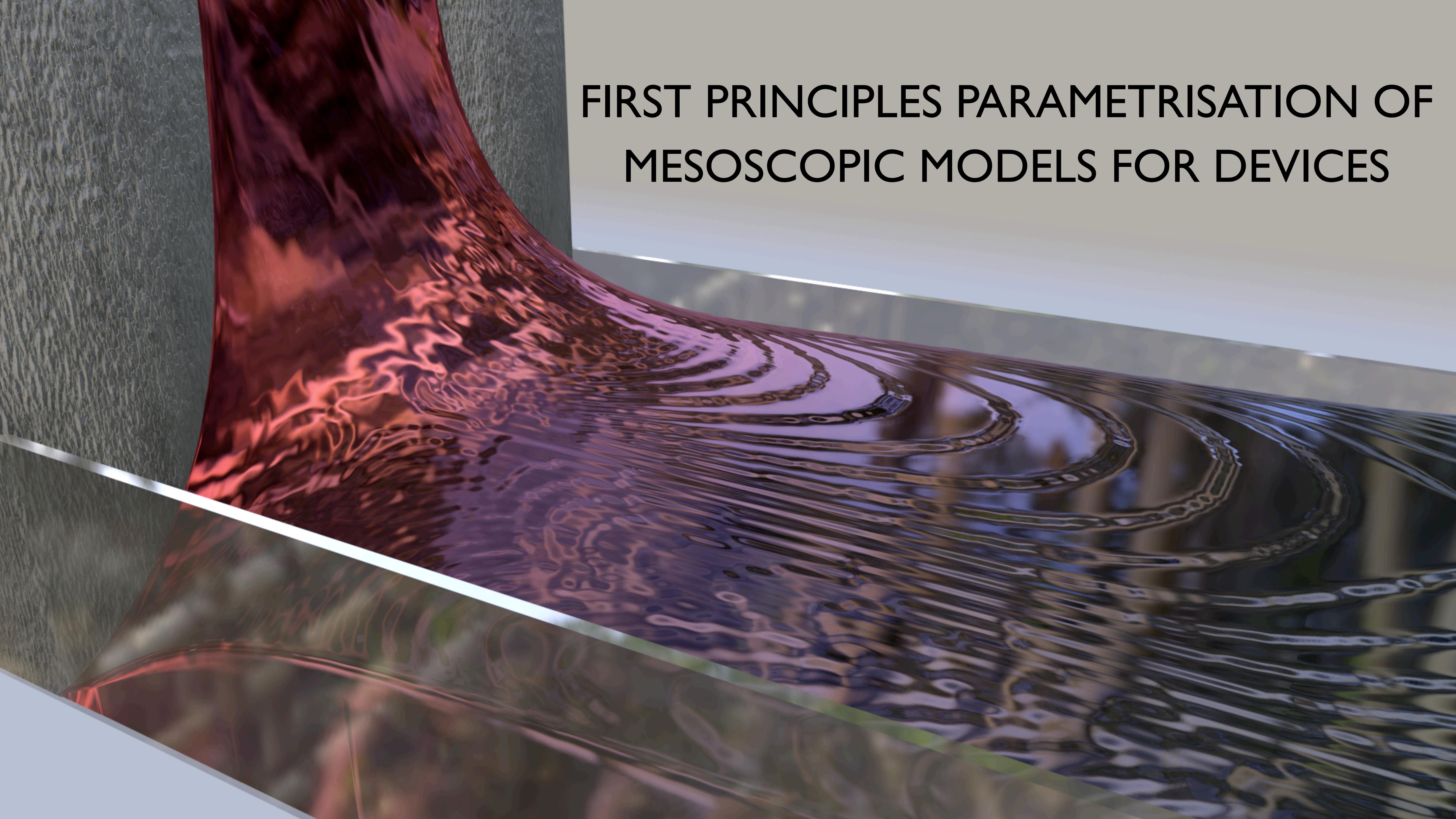


Ionic conductors:  $D_{\text{tr}}^{\text{Li}} = \lim_{t \rightarrow \infty} \frac{1}{6t} \frac{1}{N_{\text{Li}}} \sum_l \left\langle |\mathbf{R}_l(t + \tau) - \mathbf{R}_l(\tau)|^2 \right\rangle_\tau$



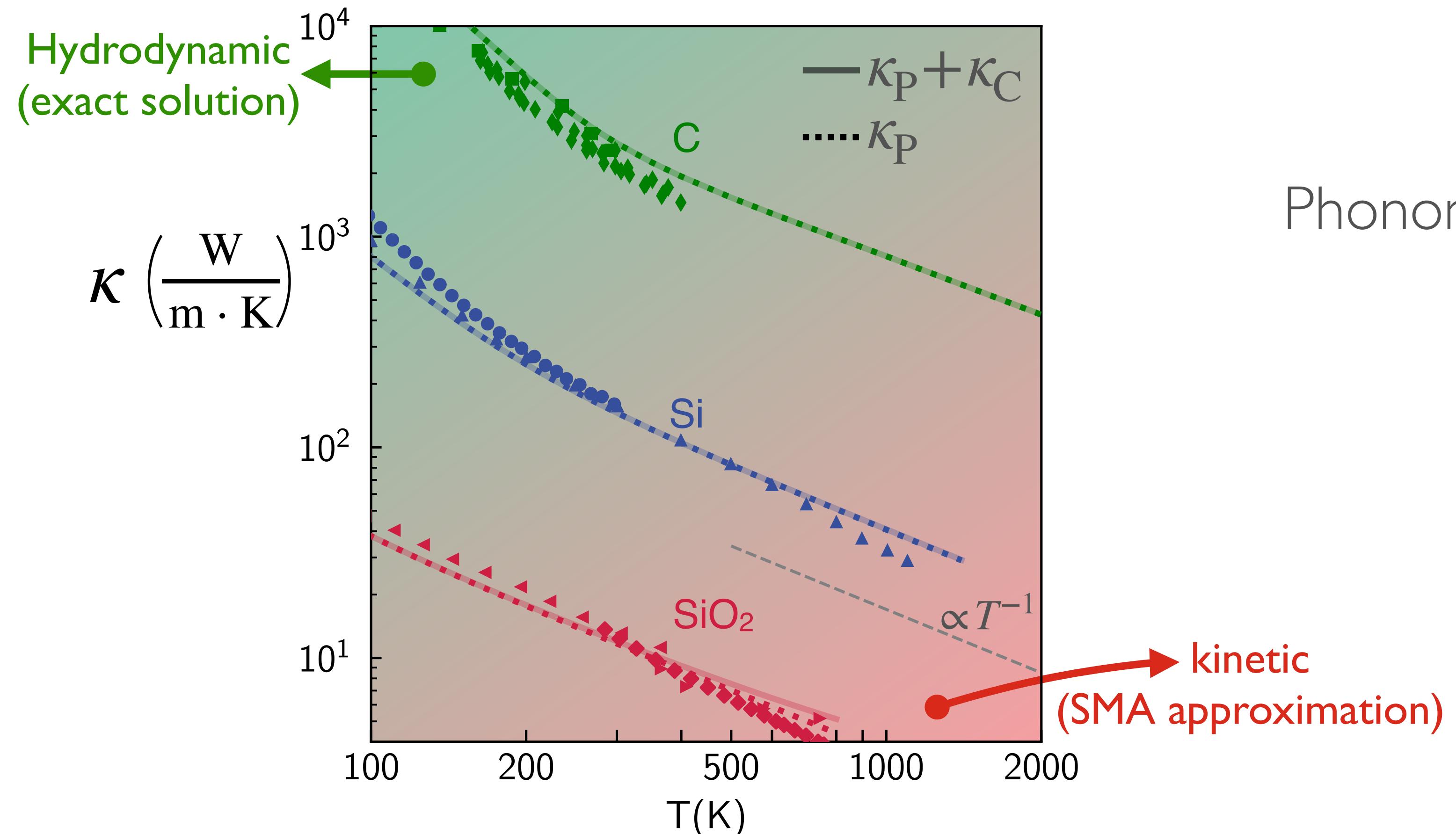
Isosurfaces of valence electronic charge density



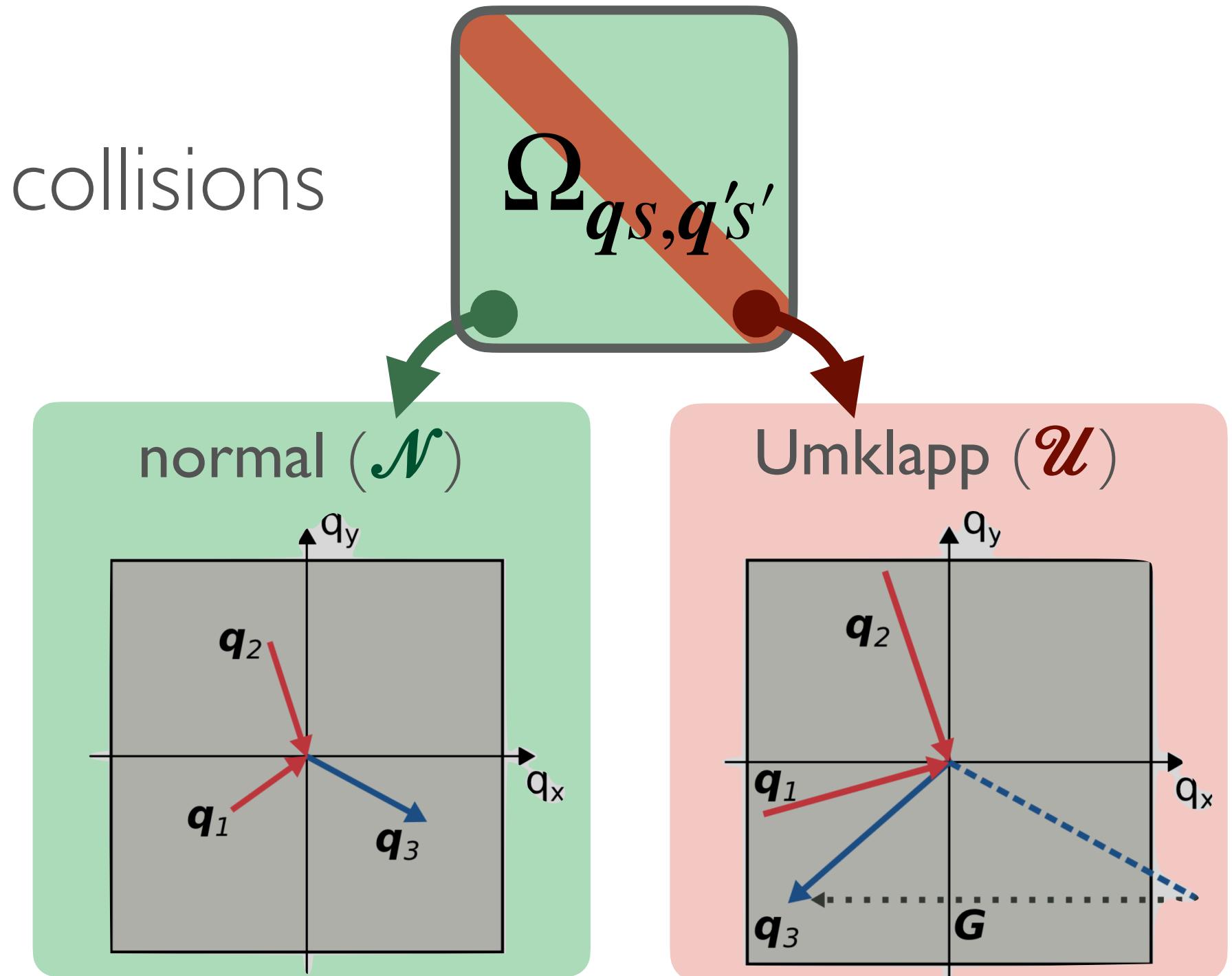


# FIRST PRINCIPLES PARAMETRISATION OF MESOSCOPIC MODELS FOR DEVICES

# HEAT HYDRODYNAMICS IN SIMPLE CRYSTALS WITH $\kappa_P \gg \kappa_C$



Phonon collisions



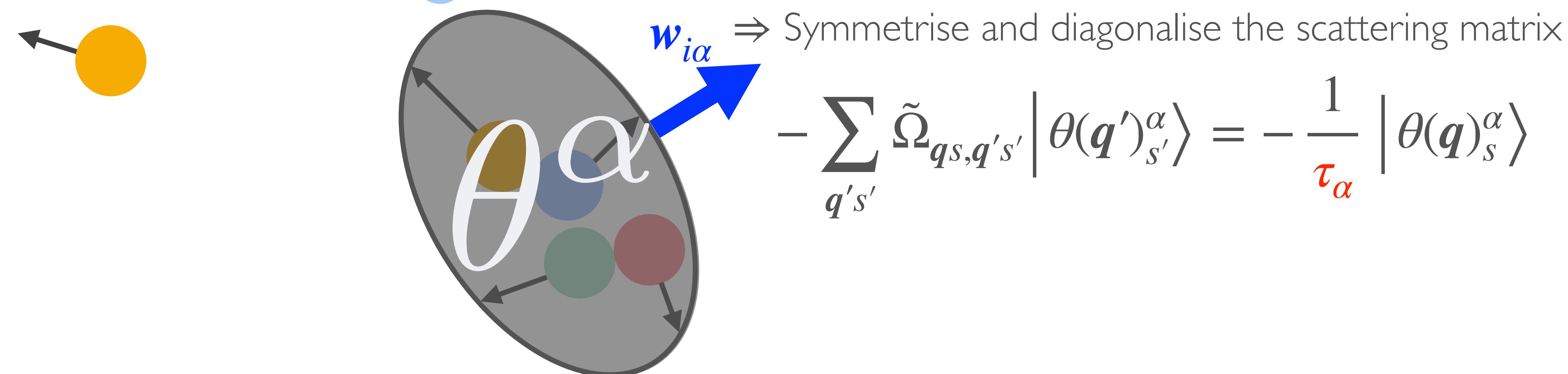
Particle-like conduction dominates, Peierls-Boltzmann equation is accurate

$$\frac{\partial N(x, \mathbf{q}, t)_s}{\partial t} + \vec{V}(\mathbf{q})_s \cdot \nabla_x N(x, \mathbf{q}, t)_s = - \sum_{\mathbf{q}' s'} \Omega_{\mathbf{q}_s, \mathbf{q}' s'} [N(x, \mathbf{q}', t)_{s'} - \bar{N}(\mathbf{q}')_{s'}]$$

# RELAXONS: EXACT SOLUTION & MICROSCOPIC INSIGHTS

How to define heat carriers and relaxation time in the hydrodynamic regime?

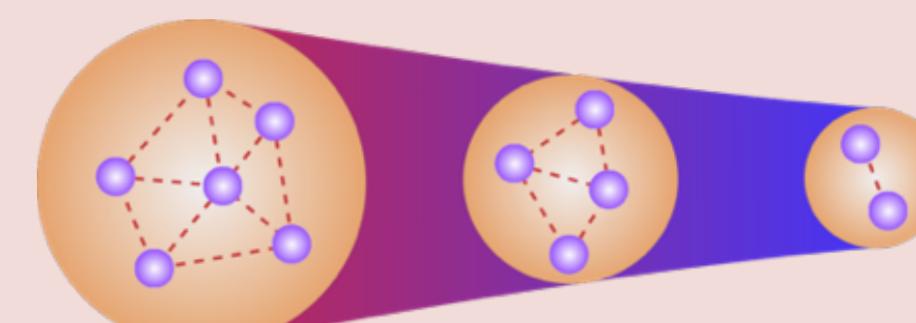
$$\frac{\partial N(x, \mathbf{q}, t)_s}{\partial t} + \vec{V}(\mathbf{q})_s \cdot \nabla_x N(x, \mathbf{q}, t)_s = - \sum_{\mathbf{q}' s'} \Omega_{qs, q's'} [N(x, \mathbf{q}', t)_{s'} - \bar{N}(\mathbf{q}')_{s'}]$$



Relaxon  $|\theta(\mathbf{q})_s^{\alpha}\rangle$  = cloud of interacting phonons having:

1) Exact lifetime:  $\tau_{\alpha}$

relaxon  
phonon

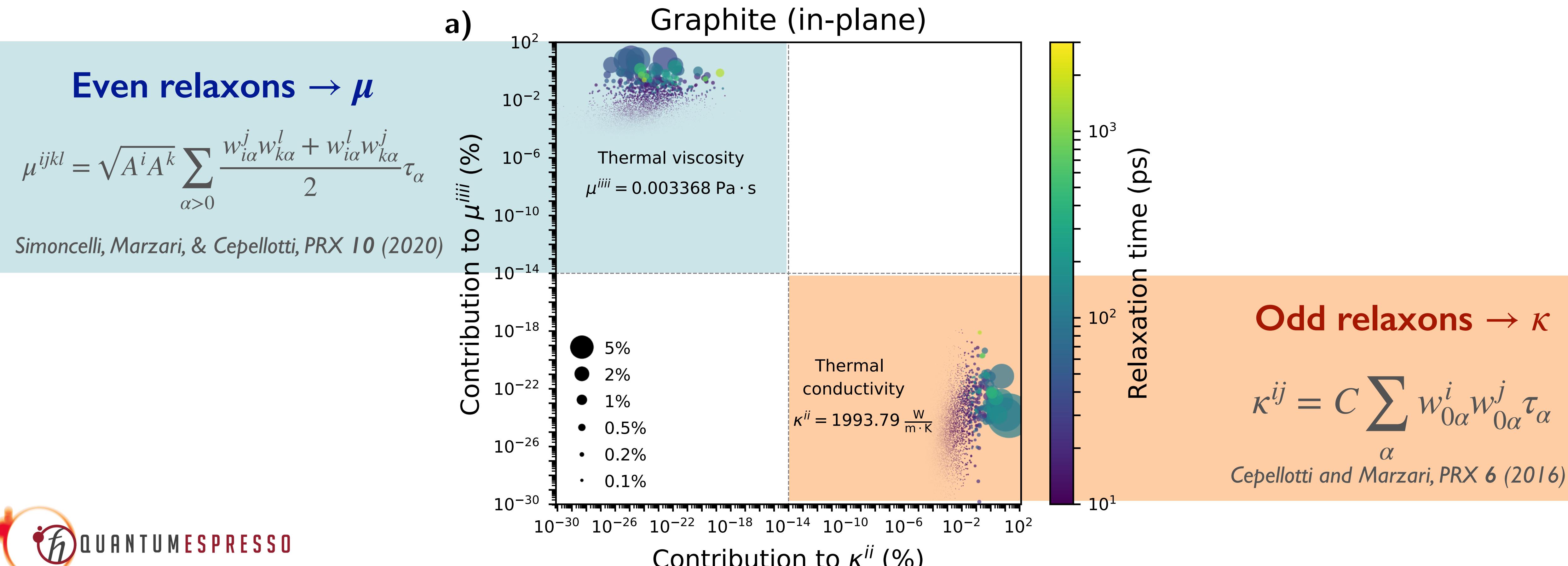


2) Velocity:

$$\mathbf{w}_{i\alpha} = \frac{1}{V} \sum_{\mathbf{q}, s} \langle \phi(\mathbf{q})_s^i | V(\mathbf{q})_s | \theta(\mathbf{q})_s^{\alpha} \rangle$$

# ODD & EVEN RELAXONS: CONDUCTIVITY & VISCOSITY

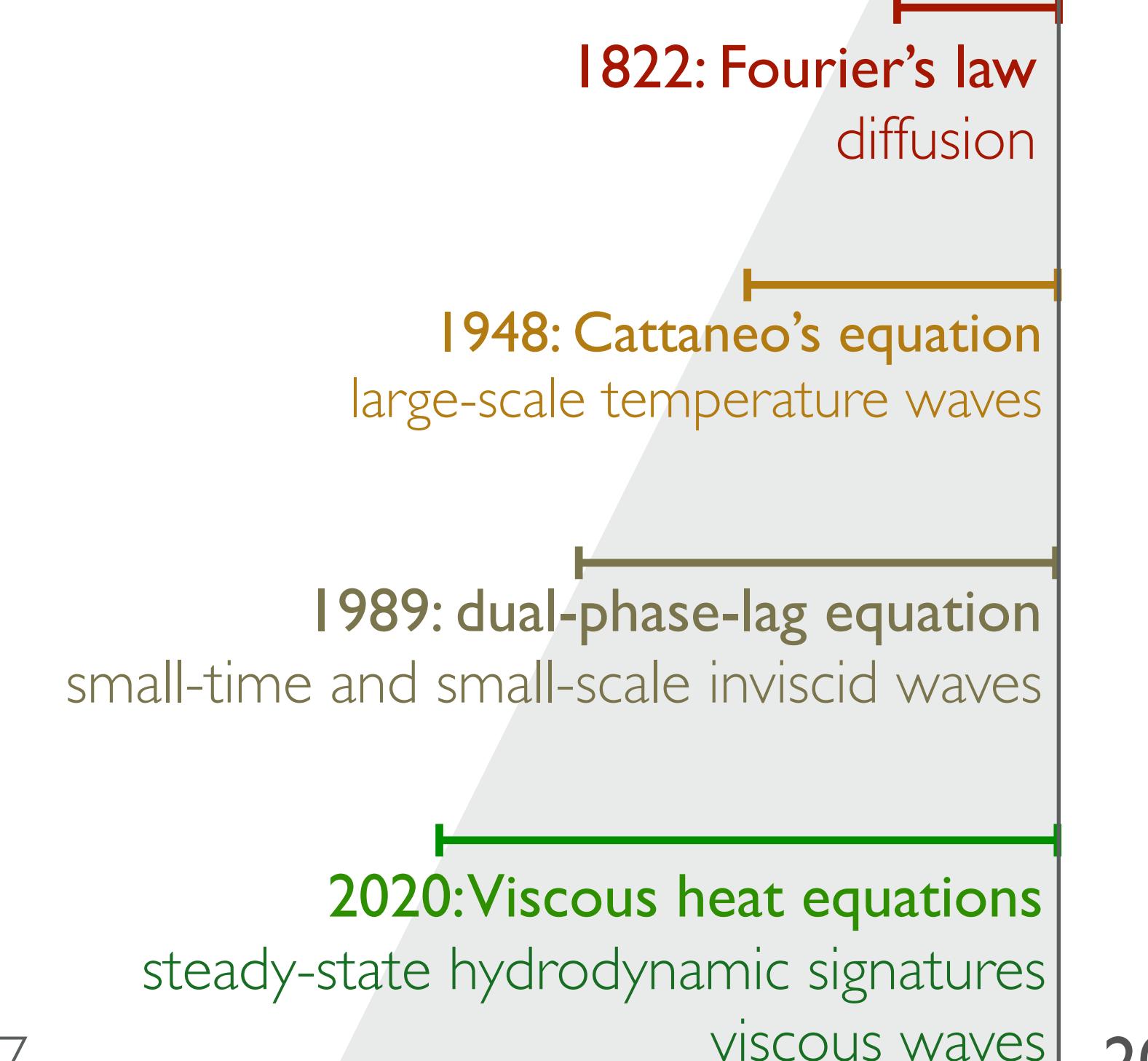
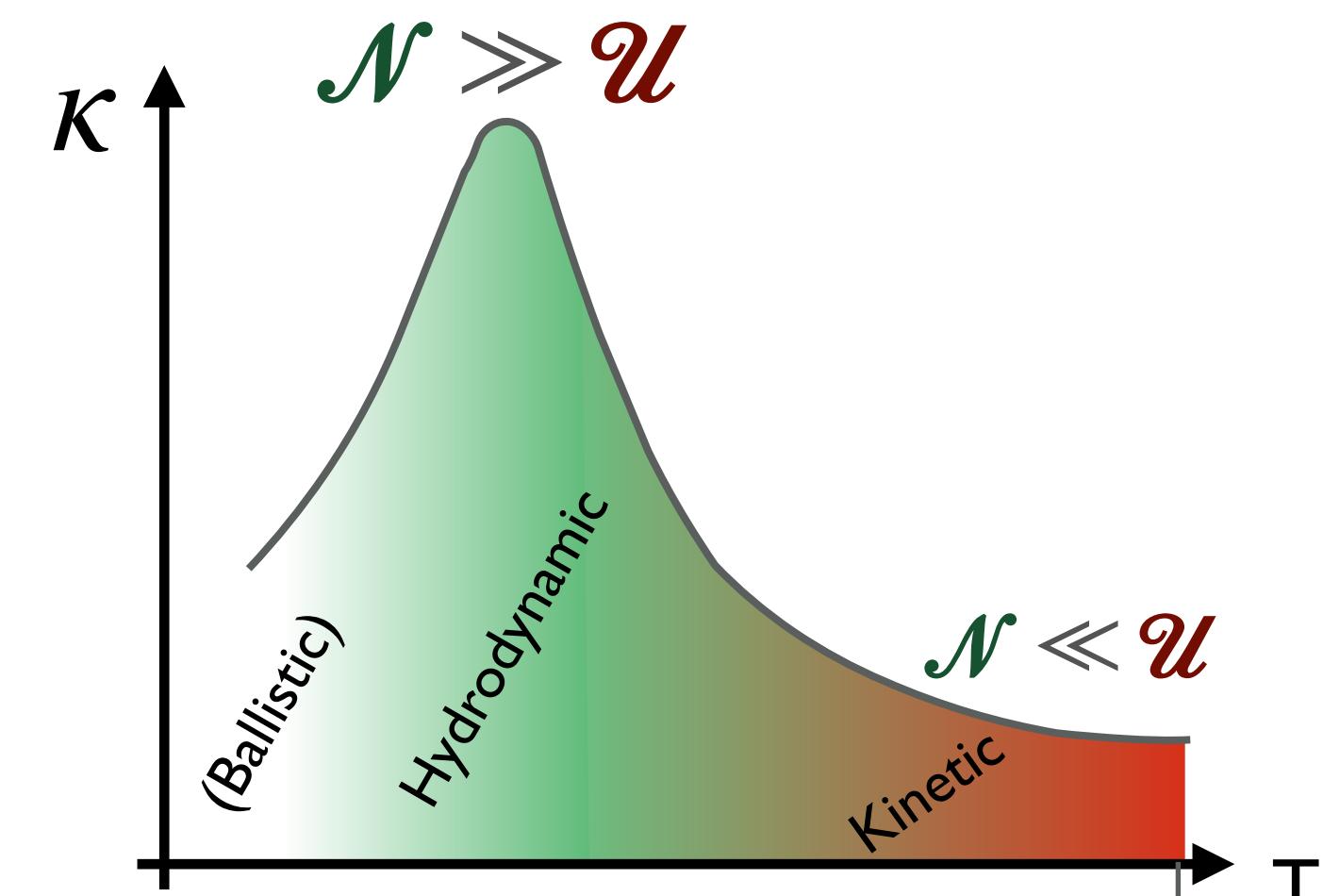
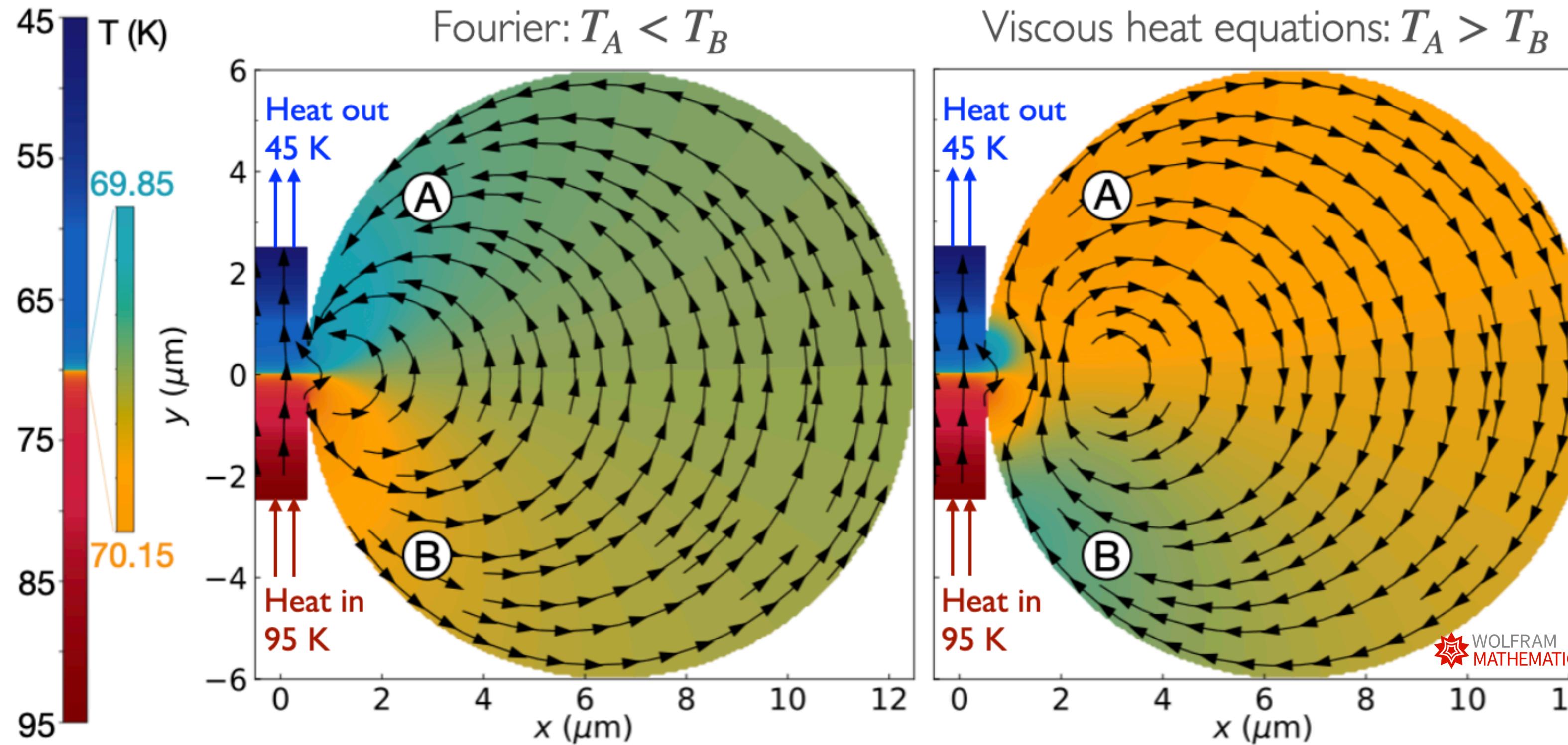
Relaxons have parity: even  $|\theta(-\mathbf{q})_s^\alpha\rangle = + |\theta(\mathbf{q})_s^\alpha\rangle$  or odd  $|\theta(-\mathbf{q})_s^\beta\rangle = - |\theta(\mathbf{q})_s^\beta\rangle$



# VISCOUS HEAT EQUATIONS GENERALISE FOURIER'S LAW

$$\partial_t T + \vec{A} \otimes \nabla_x u - \vec{\kappa} \otimes \nabla_x^2 T = 0$$

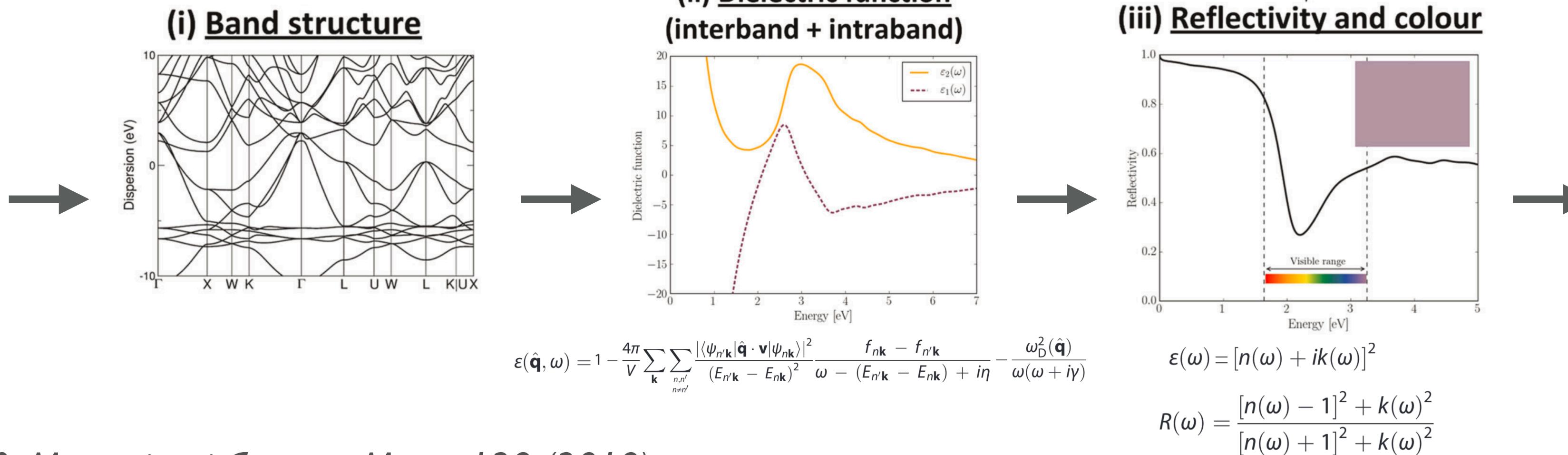
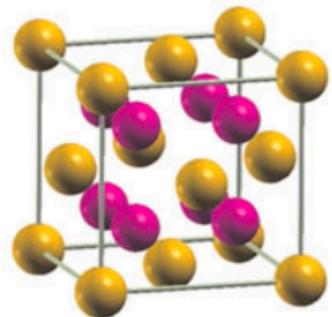
$$\partial_t u + \vec{B} \otimes \nabla_x T - \vec{\mu} \otimes \nabla_x^2 u = -\vec{D} \otimes u$$



# PREDICTING REFLECTIVITY AND COLOUR OF METALS

## Colour Workflow

### Crystal structure



Prandini, Rignanese, & Marzari, *npj Comput. Mater.* 129 (2019)

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Article | Published: 08 March 2023

**Evidence of near-ambient superconductivity in a N-doped lutetium hydride**

Nathan Dasenbrook-Gammon, Elliot Snider, Raymond McBride, Hiranya Pasan, Dylan Durkee, Nugzar Khavashi-Sutter, Sasanka Munasinghe, Sachith E. Dissanayake, Keith V. Lawler, Ashkan Salamat & Ranga P. Dias

**nature**

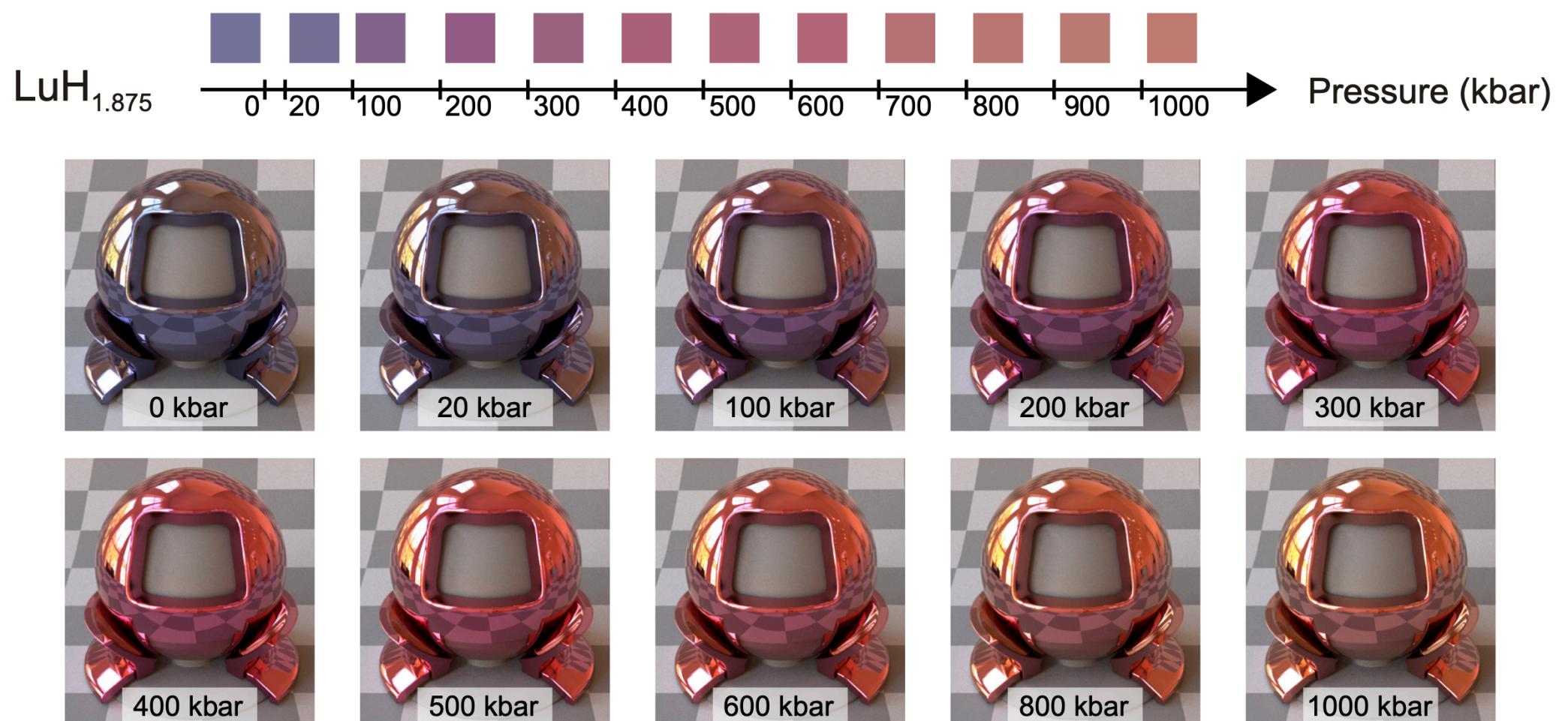
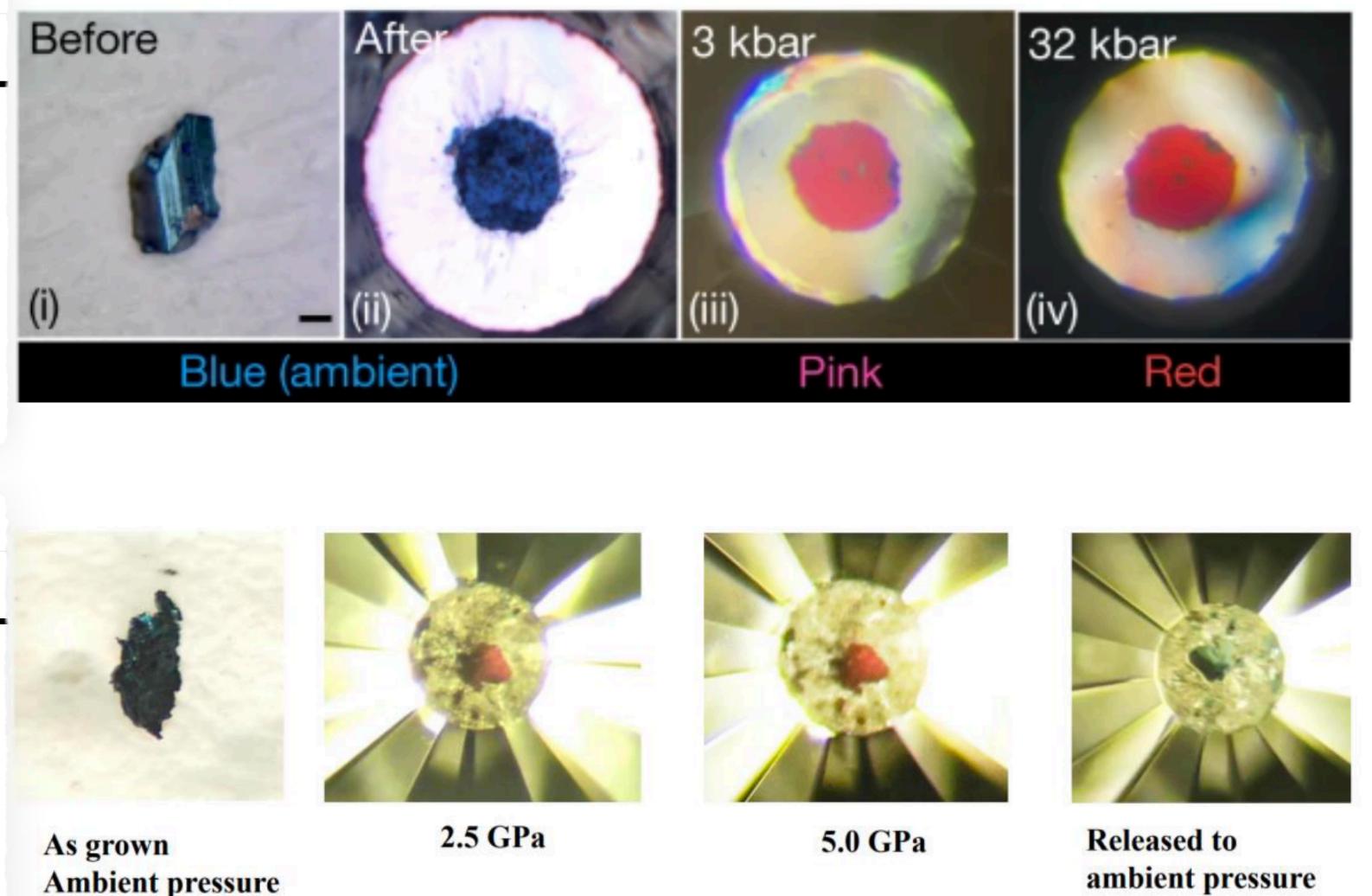
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Article | Published: 11 May 2023

**Absence of near-ambient superconductivity in LuH<sub>2+x</sub>N<sub>y</sub>**

Xue Ming, Ying-Jie Zhang, Xiyu Zhu, Qing Li, Chengping He, Yuecong Liu, Tianheng Huang, Gan Liu, Bo Zheng, Huan Yang, Jian Sun, Xiaoxiang Xi & Hai-Hu Wen



Ab-initio theory predicts color change but no superconductivity

Kim, Conway, Pickard, Pascut, & Monserrat, arXiv:2304.07326

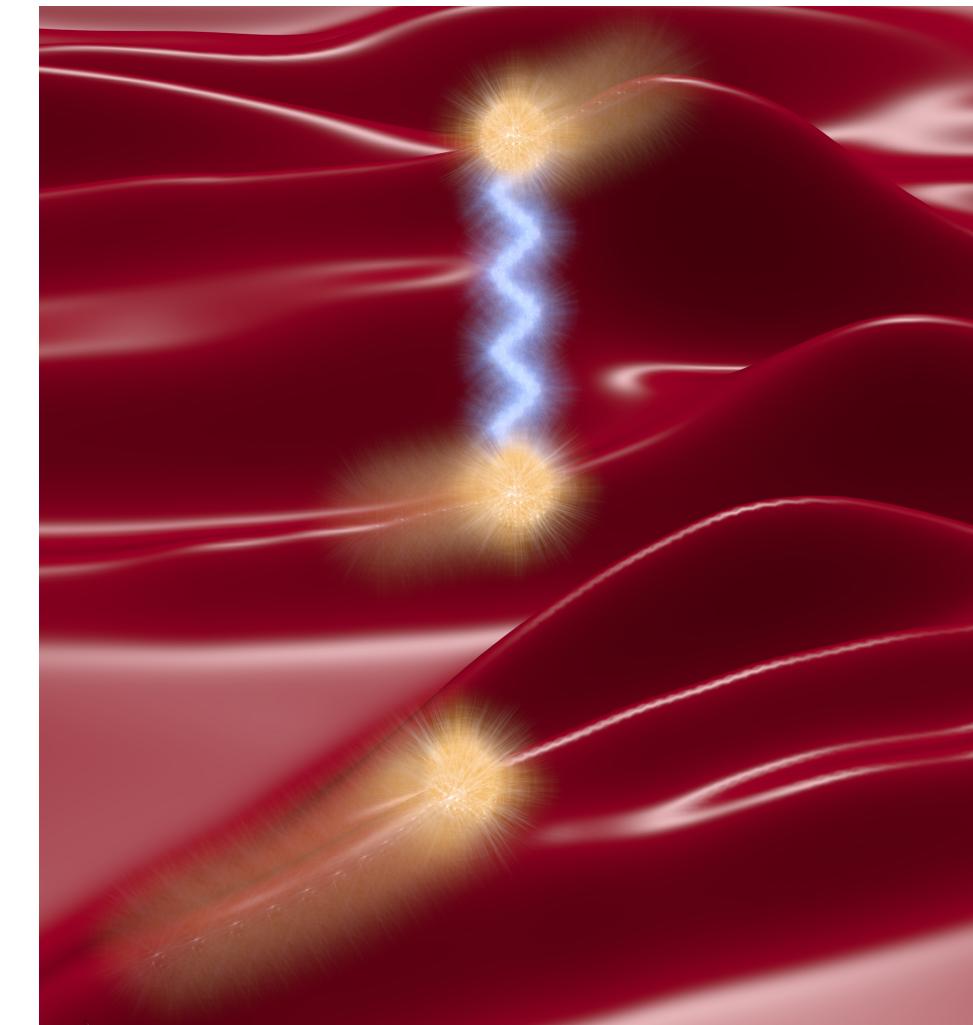
# CONCLUSIONS



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allows to predict from first principles:

- Å - **Bands** for electrons and phonons, and **broadening** due to interactions;
- **electrical and thermal conductivity** beyond semiclassical theory;
- nm - Ionic diffusion or heat transport in **disordered materials**;
- μm - **Raman spectra**, useful to characterise structural properties;
- mm - parameters for **mesoscopic models** for devices.



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