

# MS-DFT: Quantum Transport from a Multi-Space Excitation Viewpoint

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## I. Background information

- DFT-NEGF: Difficulties → Beyond DFT-NEGF?
- DFT vs NEGF
- NEGF ≠ Landauer

## II. MS-DFT: development & its applications

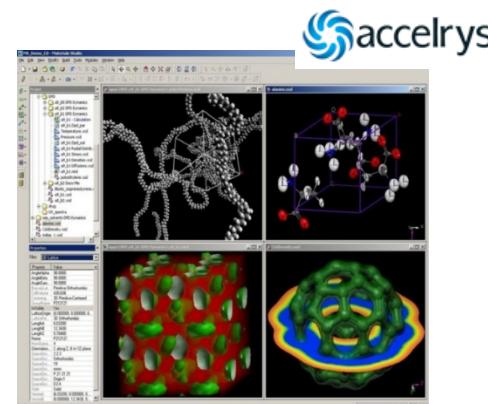
## III. Summary

# Beyond DFT: Equilibrium → Non-Equilibrium

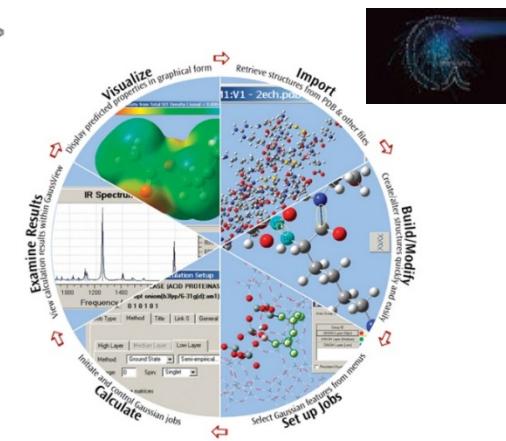
## ❑ Density Functional Theory (DFT)

- VASP
- SIESTA
- Gaussian
- etc. etc.

Energy, structure, ...



@ Equilibrium



## ❑ GW+BSE & time-dependent DFT

Optical excitation, ...

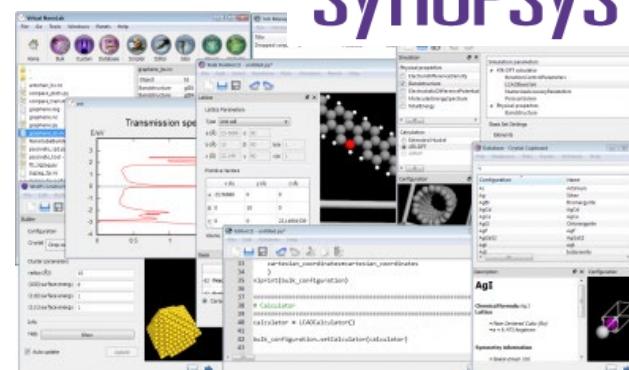
@ Non-equilibrium

## ❑ Non-Equilibrium Green's function (NEGF)

Quantum transport, ...

@ Non-equilibrium

- TranSIESTA
- QuantumATK
- etc.



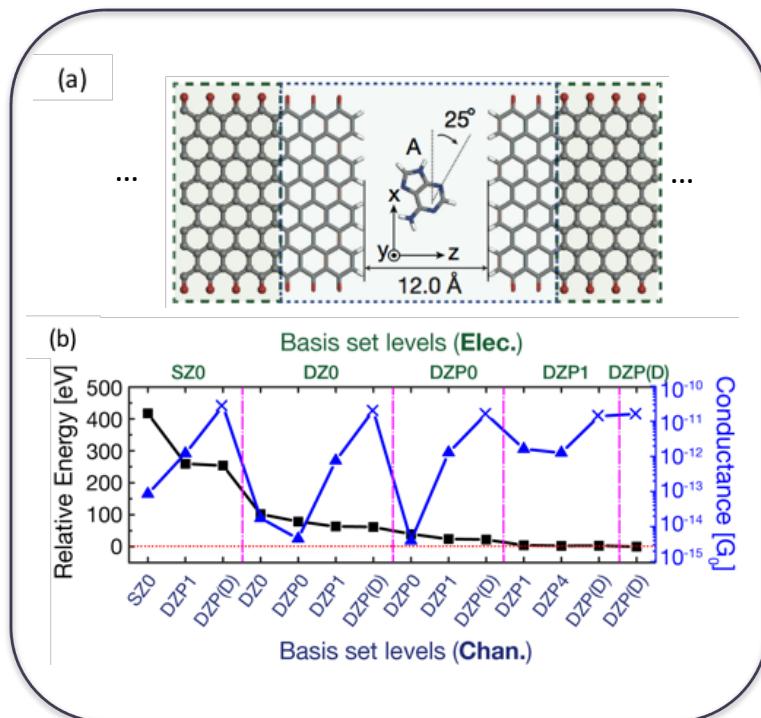
SYNOPSYS®

SEMICON®  
West2007

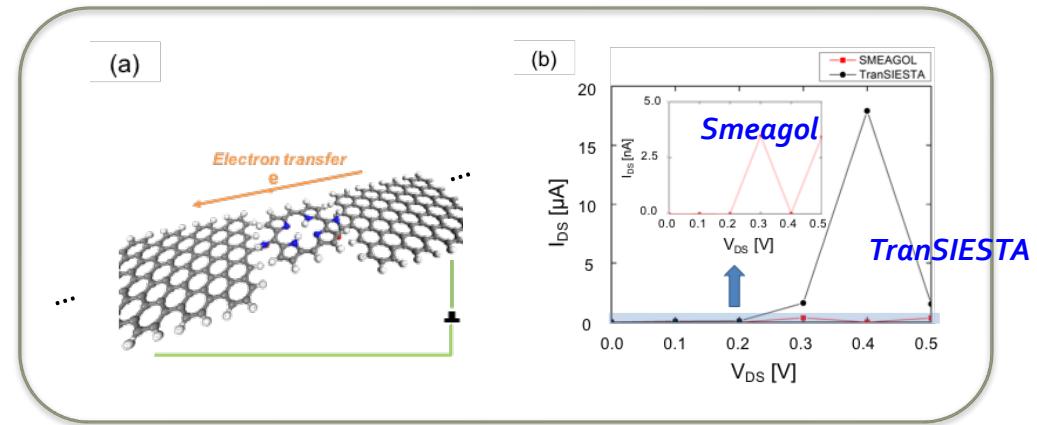
"Technology Innovation  
Showcase Winner"

# Difficulties with NEGF (beyond-DFT methods in general)

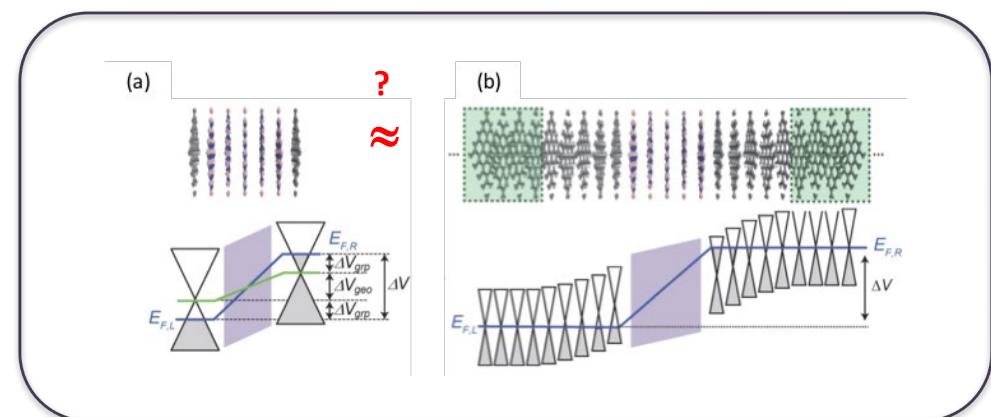
## Various difficulties from NEGF



Nonvariational nature of "Landauer" current ( $V_b = 0$  V)



Inequivalence between different codes ( $V_b \neq 0$  V)



Restrictions from the requirement of semi-infinite electrodes ( $V_b \neq 0$  V)

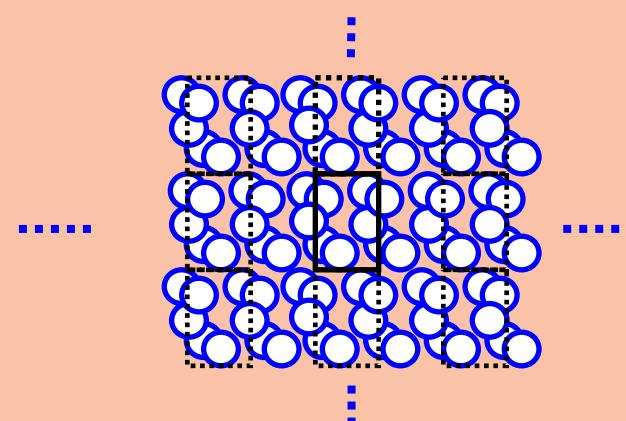
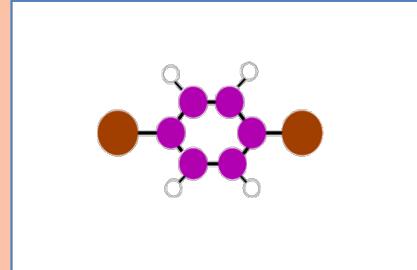
# DFT vs NEGF: Closed vs Open B.C.

## DFT (Equilibrium)

*Closed or Periodic B. C.*

$$H\psi_i = \varepsilon_i\psi_i$$

$$f_{FD}(E - \mu)$$

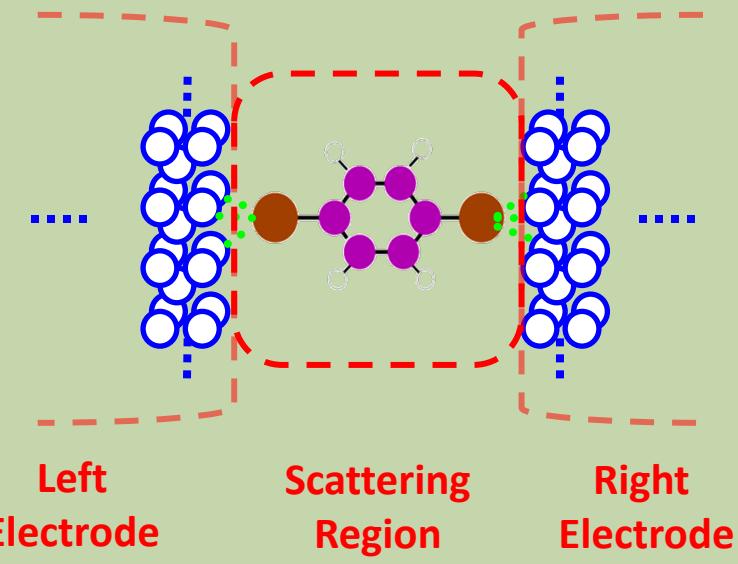


## NEGF (Non-equilibrium)

*Open B. C.*

$$G^R = (E_1 - H - \Sigma_1 - \Sigma_2)^{-1}$$

$$G^n(E) \approx f_1 A_1(E) + f_2 A_2(E)$$



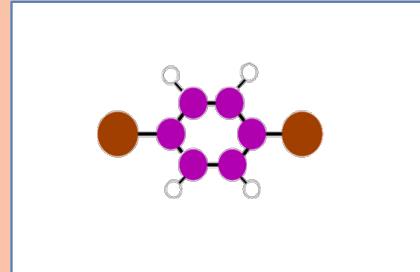
$$\Sigma = \tau g_s \tau^+$$

## DFT (Equilibrium)

*Closed or Periodic B. C.*

$$H\psi_i = \varepsilon_i\psi_i$$

$$f_{FD}(E - \mu)$$



😊 High-reliability of simulations!!

$$E[\chi] = \frac{\langle \chi | H | \chi \rangle}{\langle \chi | \chi \rangle} \rightarrow E[\chi] \geq E_{GS} = \langle \psi_{GS} | H | \psi_{GS} \rangle$$

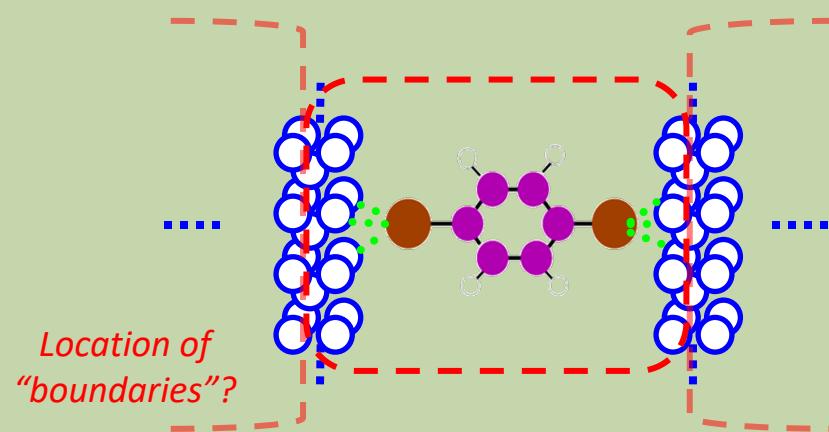
- Total energy ← Variational principle

## NEGF (Non-equilibrium)

*Open B. C.*

$$G^R = (E1 - H - \Sigma_1 - \Sigma_2)^{-1}$$

$$G^n(E) \approx f_1 A_1(E) + f_2 A_2(E)$$



😢 Ambiguities??

$$I(V) \approx \frac{e}{h} \int dE \text{Tr}(\Gamma_1 \mathbf{G} \Gamma_2 \mathbf{G}^+) [f_1 - f_2]$$

- Current: Non-variational quantity

# Remind: NEGF assumptions

Valid for: *time-dependent Schrodinger eq.* & *closed* quantum system

- Retarded Green's function ( $\sim$  DOS):

$$\mathbf{G}^R(E) = [(E + i0^+) \mathbf{1} - \mathbf{H}]^{-1}$$

- Spectral function ( $\sim$ "DOS")

$$\mathbf{A}(E) = i[\mathbf{G}(E) - \mathbf{G}^+(E)]$$



Leonid Keldysh  
(1931~2016)



Gordon Baym  
(1935~)



Leo Kadanoff  
(1937~2015)

- Correlation function ( $\sim$  density):

$$\mathbf{G}^n = \mathbf{G}^R \Sigma^{\text{in}} \mathbf{G}^A \quad \text{"Keldysh eq."}$$

$$\psi\psi^+ \quad ss^+$$

- Density matrix

$$\mathbf{D} = \frac{1}{2\pi} \int_{-\infty}^{+\infty} dE \mathbf{G}^n(E)$$

or Density

$$n(\vec{r}) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} dE \mathbf{G}^n(\vec{r}, E)$$

- *Closed quantum systems*
- *Initial global equilibrium*
- *Adiabatic approach to non-equilibrium state*

*"Electronic Transport in Mesoscopic Systems"*  
by S. Datta (1997)

*"Electrical Transport in Nanoscale Systems"*  
by M. Di Ventra (2008)

# DFT-NEGF: NEGF + Landauer (Landauer $\neq$ NEGF!)

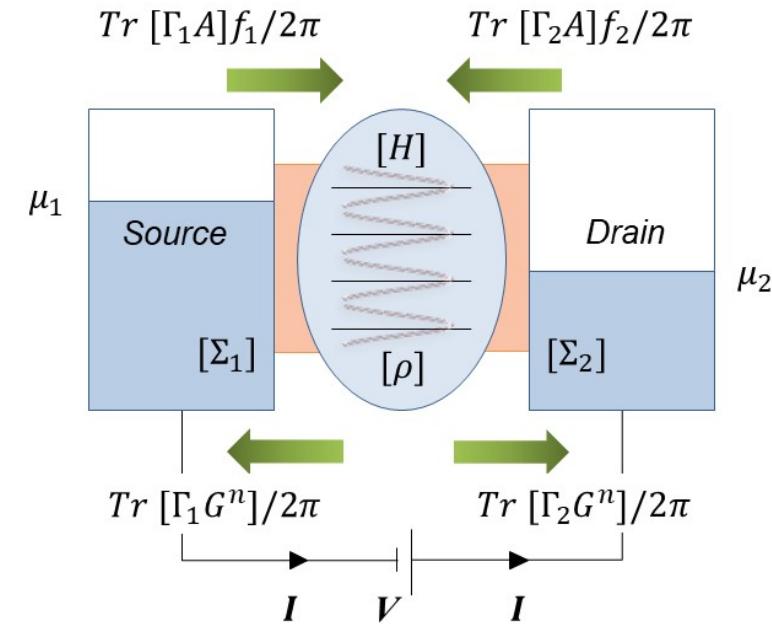
$$i\hbar \frac{\partial \psi(t)}{\partial t} = H(t)\psi(t) + \int_0^t dt' \Sigma(t, t')\psi(t') + s(t)$$

- Self-energy:
$$\mathbf{G}^R(E) = [E\mathbb{I} - \mathbf{H} - \boldsymbol{\Sigma}_1(E) - \boldsymbol{\Sigma}_2(E)]^{-1}$$
- “Landauer condition”:
$$\boldsymbol{\Sigma}^{in} \approx \boldsymbol{\Gamma}_1 f_1 + \boldsymbol{\Gamma}_2 f_2$$

$$\rightarrow n(\vec{r}) \approx \frac{1}{2\pi} \int_{-\infty}^{+\infty} dE [\mathbf{f}_1 \mathbf{A}_1 + \mathbf{f}_2 \mathbf{A}_2]$$
- Terminal current:

$$I = \frac{e}{h} \int dE \{ Tr[\boldsymbol{\Gamma}_\alpha \mathbf{A}] f_\alpha - Tr[\boldsymbol{\Gamma}_\alpha \mathbf{G}^n] \}$$

$$\approx \frac{e}{h} \int dE \underbrace{Tr(\boldsymbol{\Gamma}_1 \mathbf{G} \boldsymbol{\Gamma}_2 \mathbf{G}^+)}_{Transmission} [f_1(E) - f_2(E)]$$



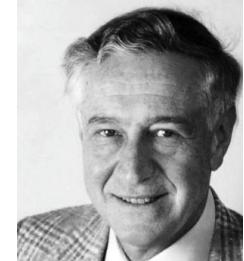
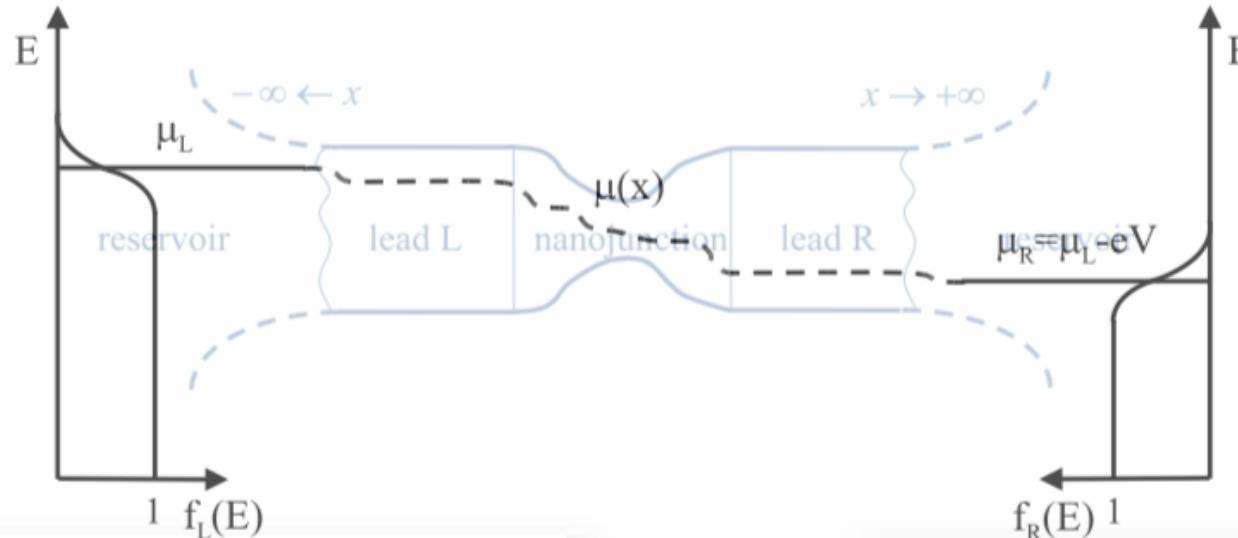
- Time-dependent  $\rightarrow$  Steady state transport
- Closed  $\rightarrow$  Open quantum system via BC

“Electronic Transport in Mesoscopic Systems”  
by S. Datta (1997)

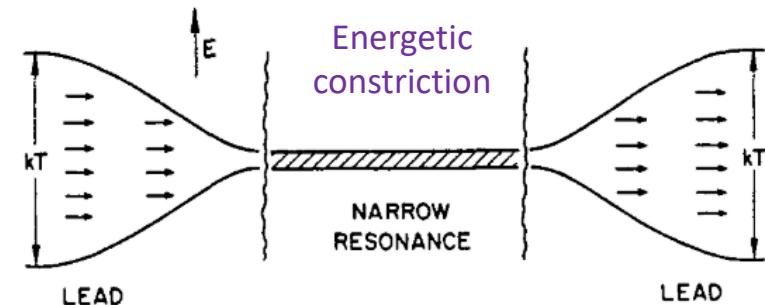
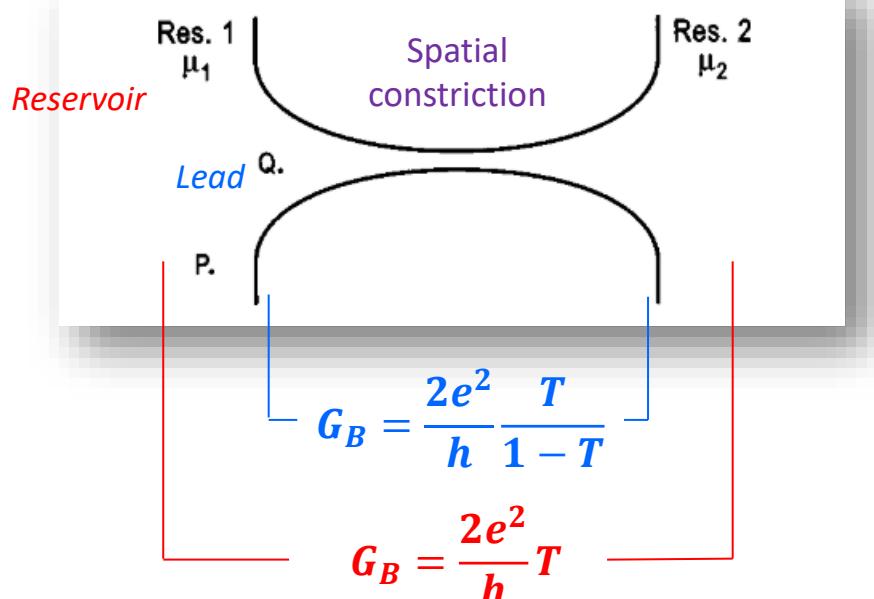
“Electrical Transport in Nanoscale Systems”  
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# Landauer “picture” for quantum transport

“... it is a **viewpoint**, not a specific equation.”



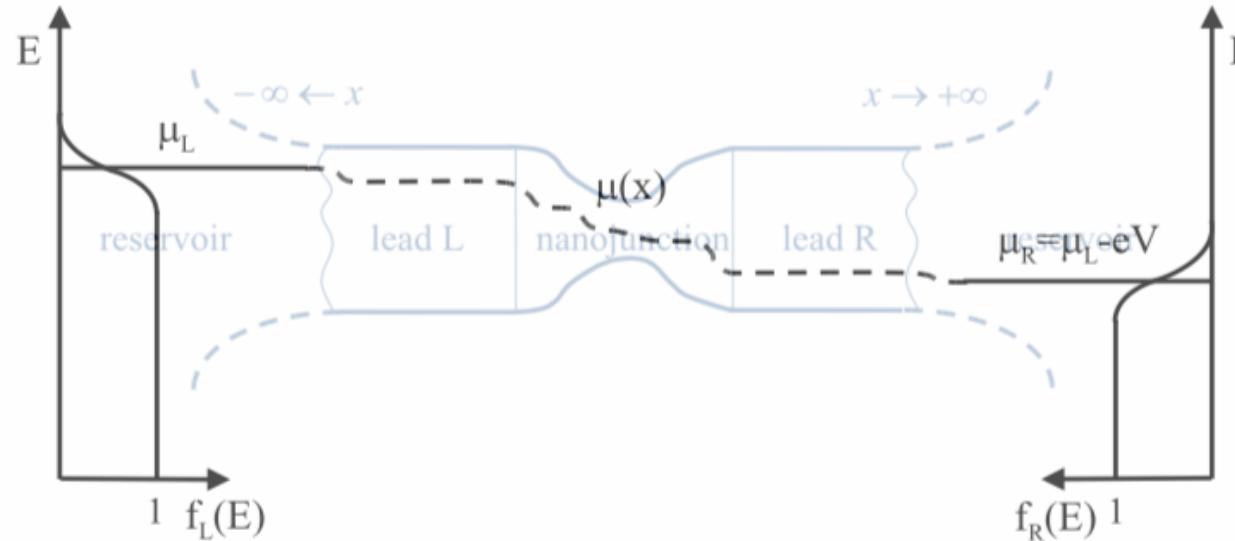
Rolf William Landauer  
(1927~1999)



- R. Landauer, *Z. Phys. B* **68**, 217 (1987)  
R. Landauer, *J. Phys. Condens. Matter* **43**, 8099 (1989)  
R. Landauer, *Phys. Scr.* **T42**, 110 (1992)  
Y. Imry & R. Landauer, *Rev.Mod. Phys.* **71**, S306 (1999)

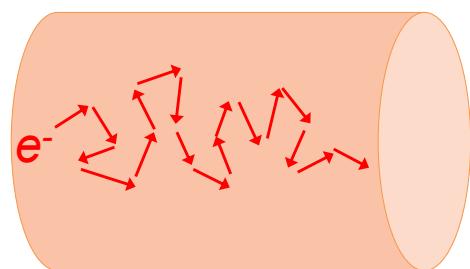
# Objective of this work

**Q. Beyond DFT-NEGF? ← Alternative to the Landauer picture?**



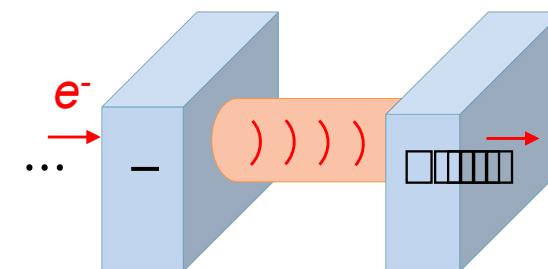
Rolf William Landauer  
(1927~1999)

## Classical transport

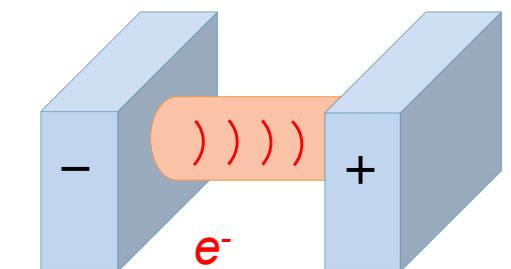


## Quantum transport

Landauer (1957)



This work (2020)



## I. Background information: DFT, NEGF, & Landauer

## II. MS-DFT: development & its applications

- Formulation → Total energy
- Voltage drop: Quasi-Fermi level splitting & Landauer resistivity dipole
- Graphene vertical vdW tunneling transistor & NDR
- *Electric enthalpy & Interfacial water*

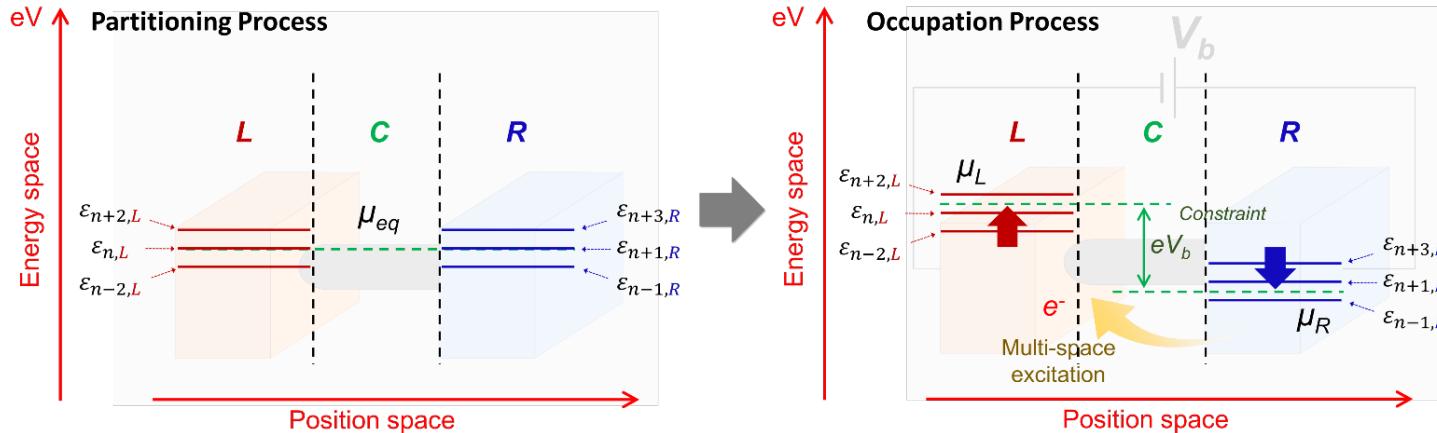
## III. Summary

## Multi-Space constrained-search DFT (MS-DFT)

### 1. Steady-state *quantum transport*

= Time-independent *multi-space optical excitation*

*cf. Landauer viewpoint*



### 2. Micro-canonical → Variational (constrained-search) DFT quantum transport calculation

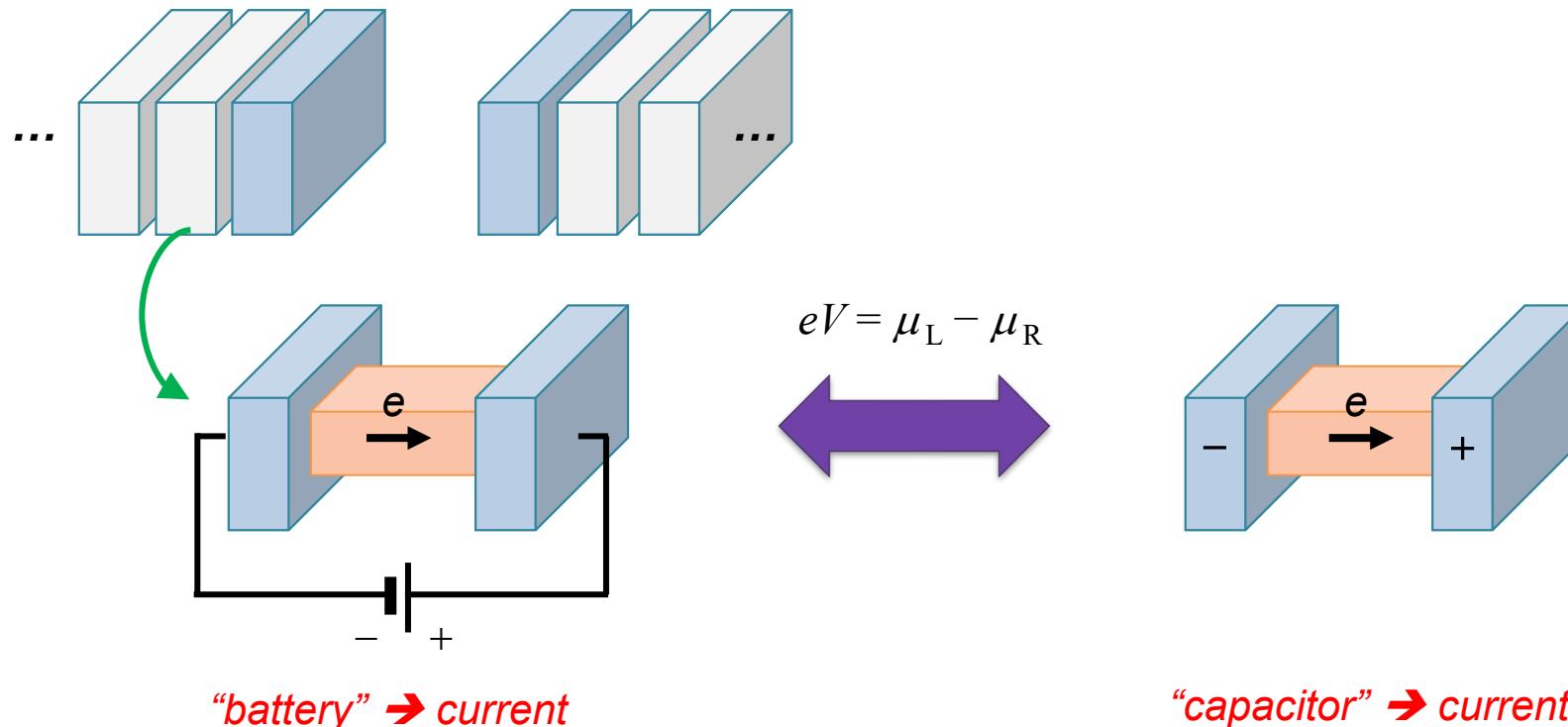
*cf. DFT-NEGF*

- H.S. Kim & YHK, arXiv [cond-mat.mes-hall], 1808.03608 (2018)
- J. Lee, H. Yeo, & YHK, PNAS **117**, 10142 (2020)
- T.H. Kim, J. Lee, R.-G. Lee, & YHK, Adv. Sci. **7**, 2001038 (2020)

**Quantum transport = Multi-space (space-discriminating) excitation**  
→ **Variational DFT calculation of steady-state current**

Step 1. Viewpoint: Grand-canonical (“Landauer”)  $\Leftrightarrow$  Micro-canonical

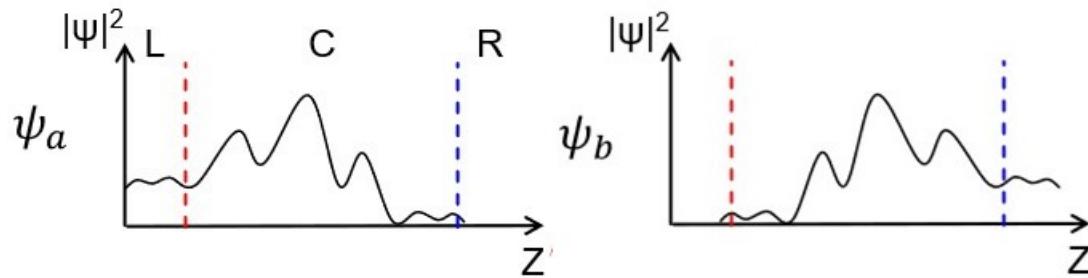
Di Ventra & Todorov, J. Phys. Cond. Matt. **16**, 8025 (2004).



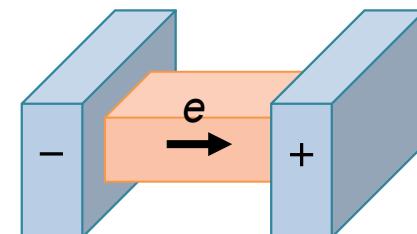
**Quantum transport = Multi-space (space-discriminating) excitation**  
 → **Variational DFT calculation of steady-state current**

Step 2. Assign  $\Psi$  to  $L$ ,  $C$ , &  $R$  regions

“locality” or “near-sightness” in C (semi-conductors)  
 (W. Kohn)



$$\psi_i(\vec{r}) \in \begin{cases} \psi_i^L & \text{if } \int_L |\psi_i(\vec{r})|^2 d^3r > \int_{C/R} |\psi_i(\vec{r})|^2 d^3r, \\ \psi_i^C & \text{if } \int_C |\psi_i(\vec{r})|^2 d^3r > \int_{L/R} |\psi_i(\vec{r})|^2 d^3r, \\ \psi_i^R & \text{if } \int_R |\psi_i(\vec{r})|^2 d^3r > \int_{L/C} |\psi_i(\vec{r})|^2 d^3r \end{cases}$$



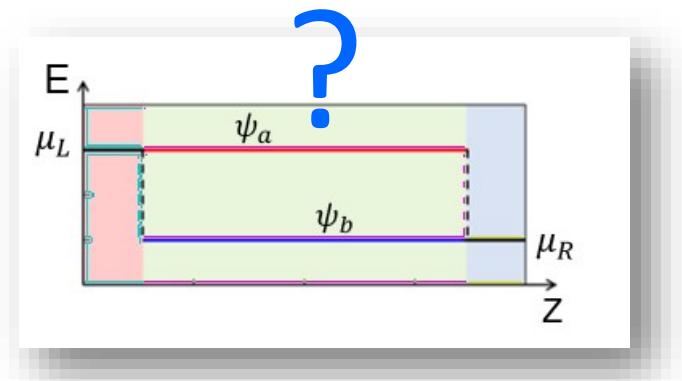
- $V = 0 : \rho_0(\vec{r}) = \rho_0^L(\vec{r}) + \rho_0^C(\vec{r}) + \rho_0^R(\vec{r})$
- $V \neq 0 : \rho_k(\vec{r}) = \rho_k^L(\vec{r}) + \rho_k^C(\vec{r}) + \rho_k^R(\vec{r})$

**Quantum transport = Multi-space (space-discriminating) excitation**  
 → **Variational DFT calculation of steady-state current**

Step 3. quantum **transport** ⇔ Multi-electrode (*drain* → *source*) **excitation**

cf. **Variational time-independent excited-state DFT**

- M. Levy & Á. Nagy, *Phys. Rev. Lett.* **83**, 4361 (1999).
- A. Görling, *Phys. Rev. A* **59**, 3359 (1999).



For the “excited” state  $k$ ;

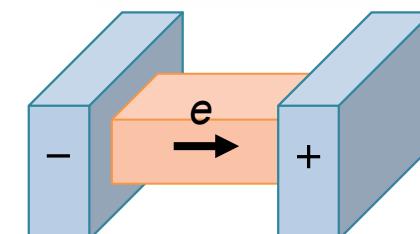
$$\begin{aligned} E_k &= \min_{\rho} \left\{ \int v(\vec{r}) \rho(\vec{r}) d^3 \vec{r} + F[\rho_k^L, \rho_k^C, \rho_k^R, \rho_0] \right\} \\ &= \int v(\vec{r}) \rho(\vec{r}) d^3 \vec{r} + F[\rho_k, \rho_0] \end{aligned}$$

with

*orthogonal*

$$F[\rho_k, \rho_0] = \min_{\Psi^{L/C/R} \rightarrow \rho_k} \langle \Psi_{L/C/R} | \hat{T} + \hat{V}_{ee} | \Psi_{L/C/R} \rangle$$

→ **Constrained Search** (constraint:  $eV = \mu_R - \mu_L$ )



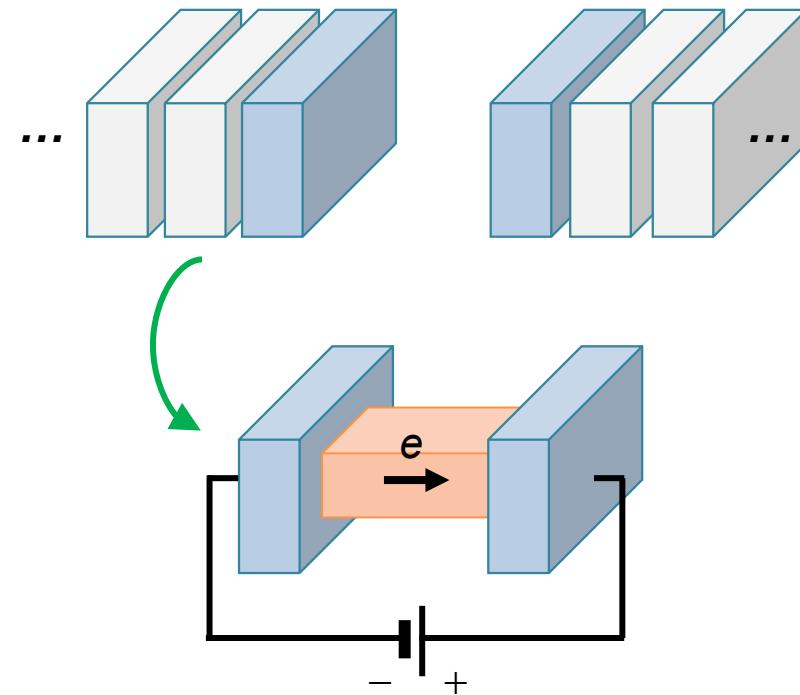
$$\rho_k(\vec{r}) = \rho_k^L(\vec{r}) + \rho_k^C(\vec{r}) + \rho_k^R(\vec{r})$$

**Quantum transport = Multi-space (space-discriminating) excitation**  
 → **Variational DFT calculation of steady-state current**

Step 4. Transmission & current as **post-processing processes**

- Semi-infinite electrodes (recover Landauer):

$$T(E; V) = \text{Tr}[\Gamma_L G \Gamma_R G^\dagger]$$



- Finite electrodes:

$$T(E; V) = \text{Tr}[A_L M A_R M^\dagger] \quad \text{with} \quad M = \tau_L^+ G \tau_R$$

- I-V:

$$I(V) = \frac{e}{h} \int_{-\infty}^{\infty} dE \ T(E; V) [f_1(E) - f_2(E)]$$

*N.B. "Current" is not our simulation target any more.*  
→ Instead, minimizing "energy" within the "constraint  $eV = \mu_1 - \mu_2$ "

0. Applied bias as a constraint:  $eV = \mu_1 - \mu_2$
1. Assign  $\psi_i$  to L/C/R (multi-space) regions
2. Minimize energy functional via constrained search :

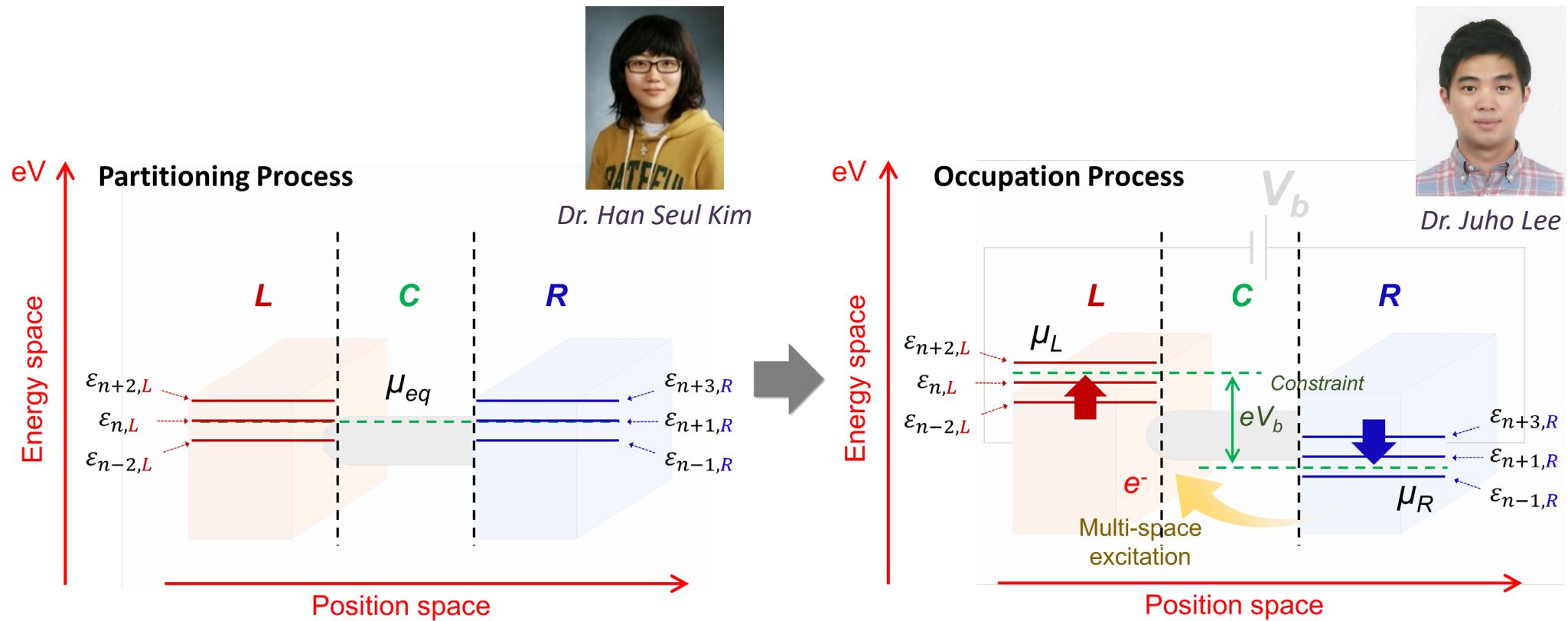
$$E_k = \min_{\rho} \left\{ \int v(\vec{r}) \rho(\vec{r}) d^3\vec{r} + F[\rho_k^L, \rho_k^C, \rho_k^R, \rho_0] \right\} \quad (\text{total energy})$$

$$F[\rho_k, \rho_0] = \min_{\Psi^{L/C/R} \rightarrow \rho_k} \langle \Psi_{L/C/R} | \hat{T} + \hat{V}_{ee} | \Psi_{L/C/R} \rangle \quad (\text{universal functional})$$

⇒ Solve (non-equilibrium) Kohn-Sham (KS) equations

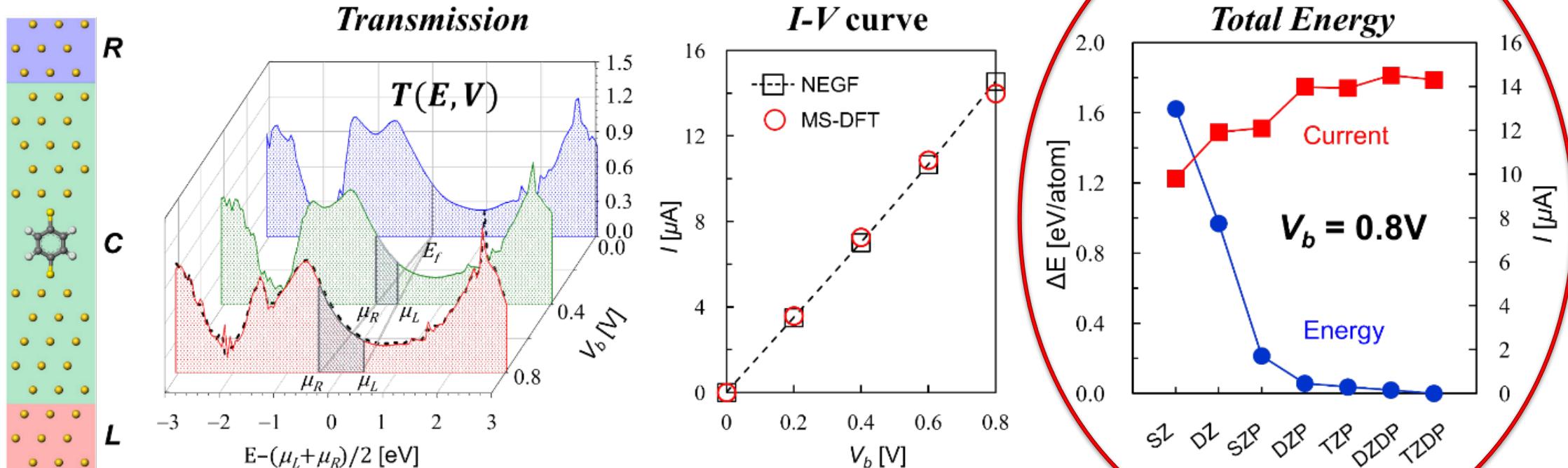
$$[\hat{h}_{KS}^0 + \Delta v_{Hxc}(\vec{r})] \psi_i(\vec{r}) = \varepsilon_i \psi_i(\vec{r})$$

**Quantum transport = Multi-space (space discriminating) excitation**  
**→ Variational constrained-search DFT calculation of quantum transport**



# MS-DFT advantage 1. “Non-equilibrium” total energy

- MS-DFT (microcanonical) vs NEGF (grand-canonical) → Key implication:



Dr. Han Seul Kim



Dr. Juho Lee

J. Lee, H. Kim, & YHK,  
Adv. Sci. 7, 2001038  
(2020)

## 2. Quasi-Fermi levels (Electrochemical potential drop)

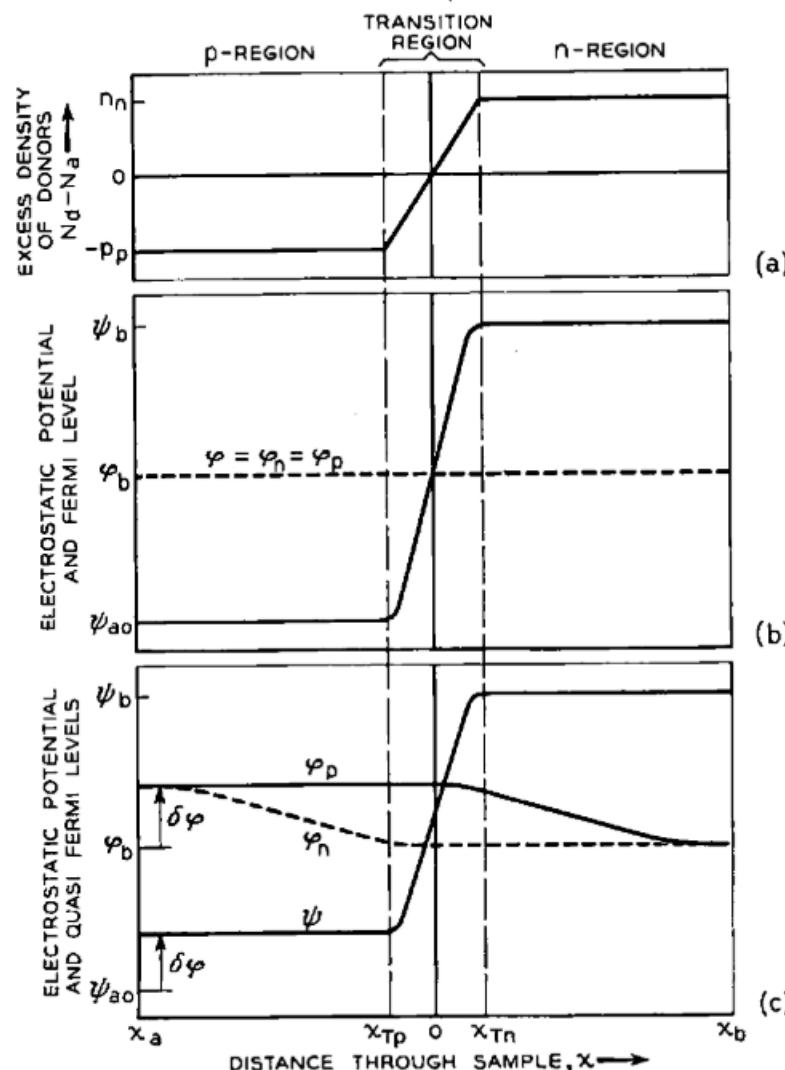
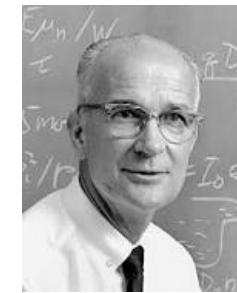


Fig. 6—Simplified model of a  $p-n$  junction.



Nobel Prize in  
Physics 1956

William Shockley  
(1910~1989)

- **$p-n$  junction**

Shockley, Bell Sys. Tech. J. **28**, 435 (1949)

- **e-h recombination**

Shockley-Read, Phys. Rev. **87**, 835 (1952)

- **Solar cell**

Shockley-Queisser, J. Appl. Phys. **32**, 510 (1961)

**N.B.**

*After 70 years since its inception,  
NO 1<sup>st</sup>-principles calculations of QFLs*

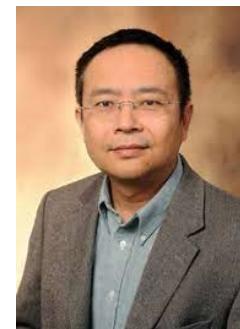
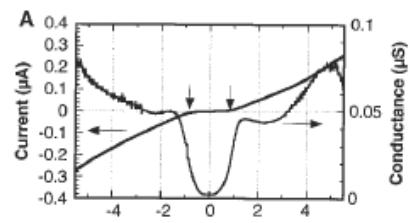
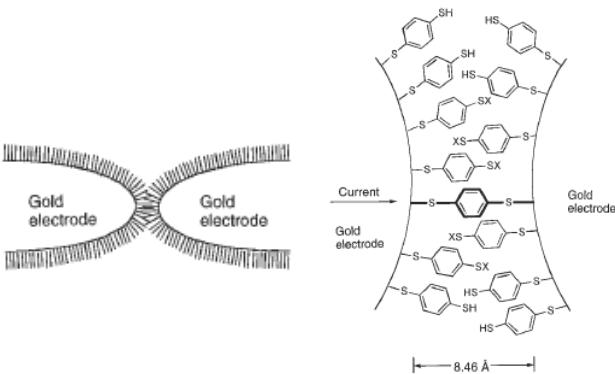
# Explicit (implicit) QFLs within MS-DFT (DFT-NEGF)

IWCN 2023  
June 12, 2023

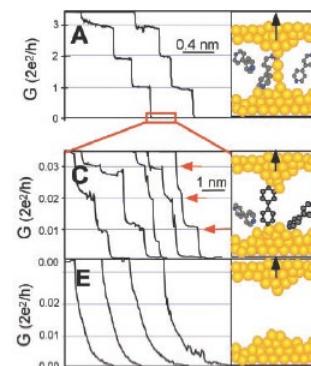
e.g. Molecular electronic devices



Mark Reed  
(1955~2021)



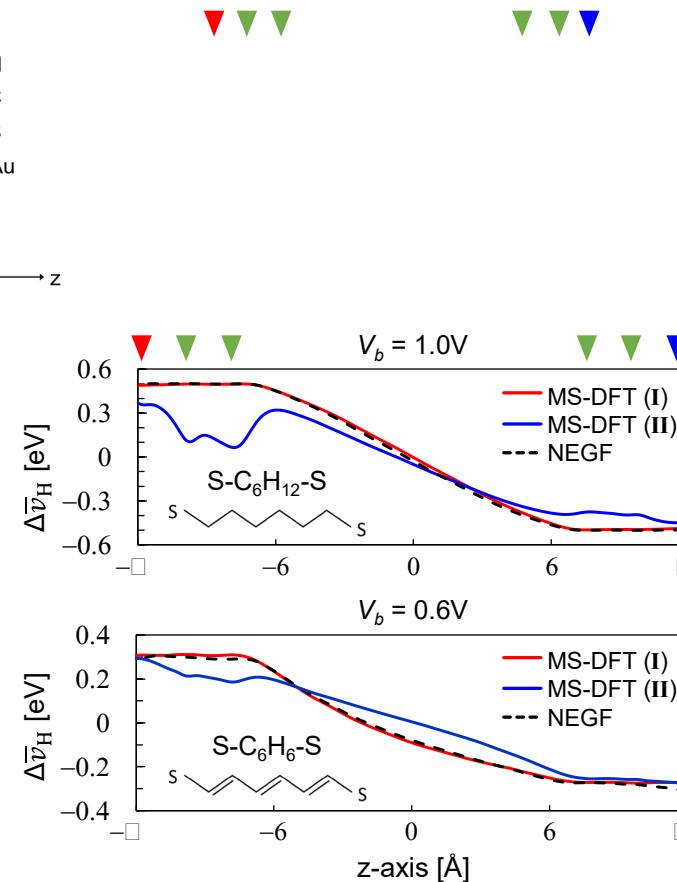
Nongjian Tao  
(1963~2020)



Science (2003)

○ H  
● C  
● S  
● Au

y  
x  
z



# Explicit (implicit) QFLs within MS-DFT (DFT-NEGF)

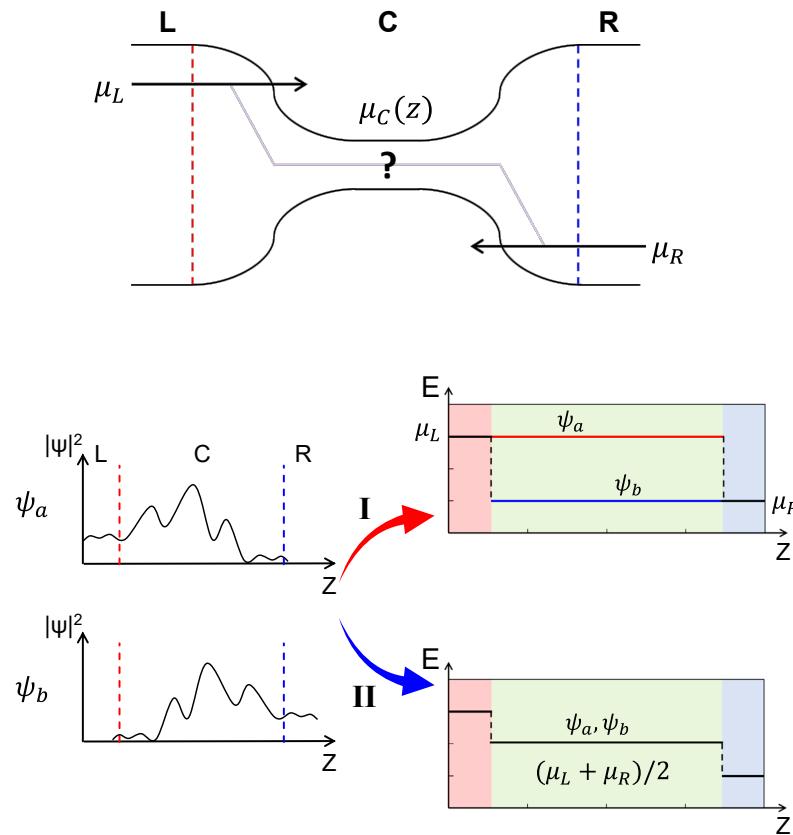
- Occupation rule? → Important to maintain the **separate (non-local) QFLs!**



Juho Lee

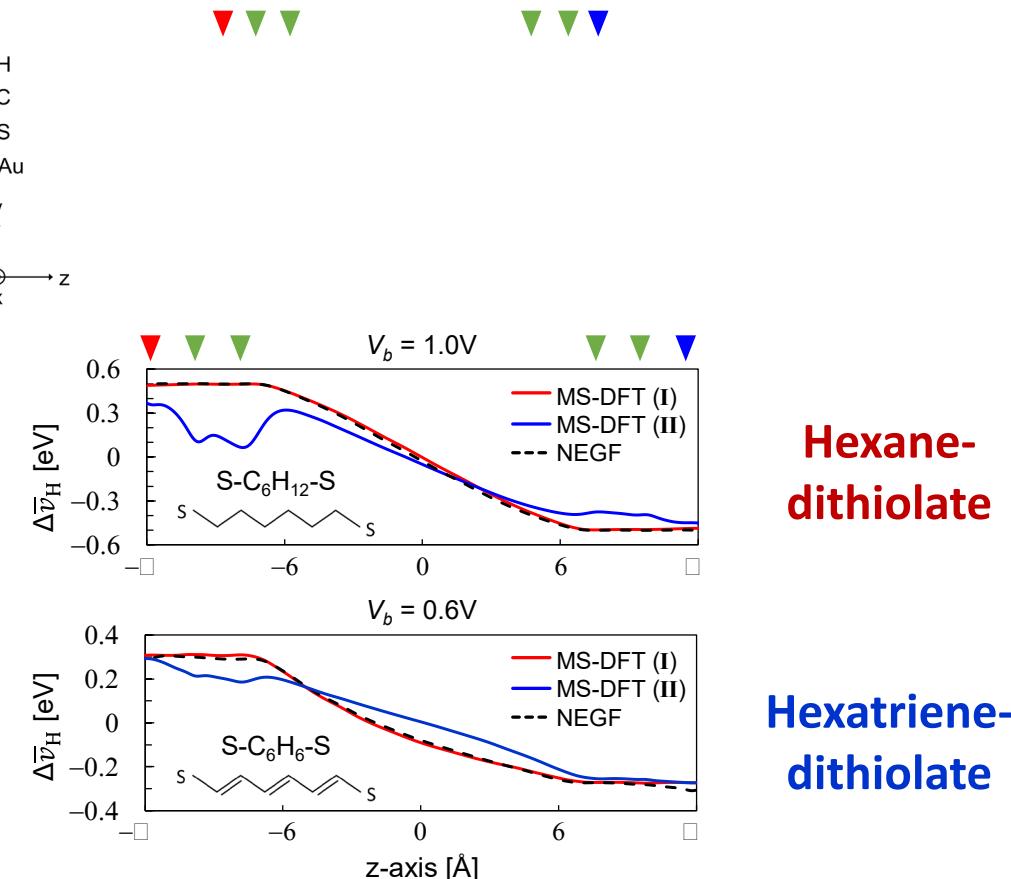


Hyun Woo Yeo



J. Lee, H. Yeo, & YHK,  
PNAS 117, 10142 (2020)

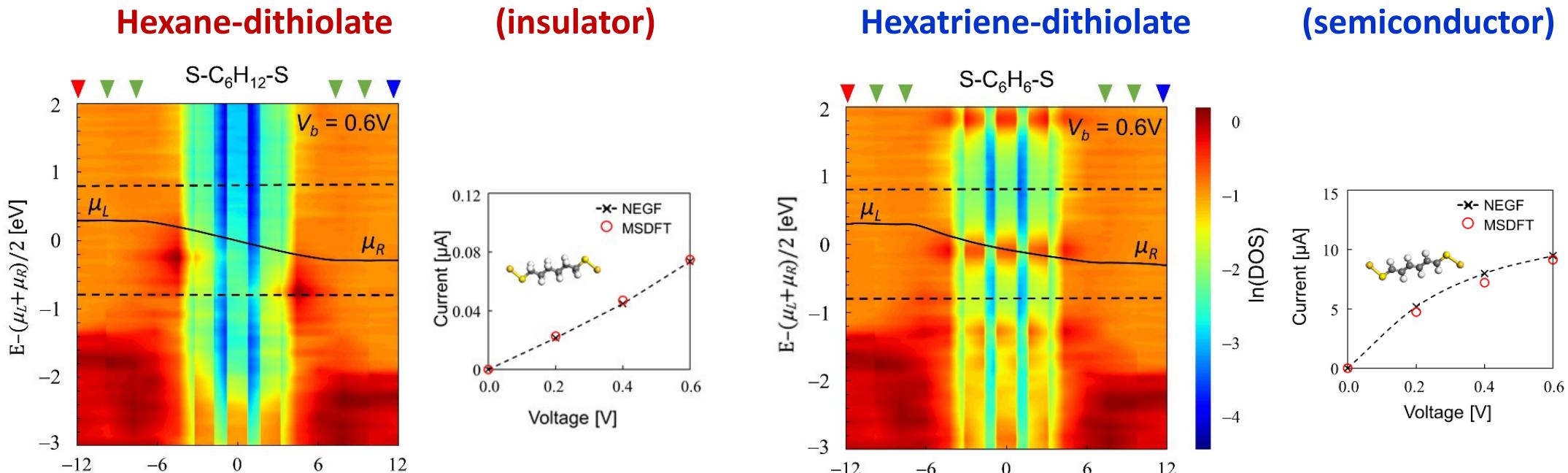
$$cf. n(\vec{r}) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} dE \mathbf{G}^n(\vec{r}, E) \\ \approx \frac{1}{2\pi} \int_{-\infty}^{+\infty} dE [f_1 \mathbf{A}_1 + f_2 \mathbf{A}_2] \\ \mathbf{G}\Gamma_1 \mathbf{G}^+ \quad \mathbf{G}\Gamma_2 \mathbf{G}^+$$



$$\psi_i(\vec{r}) \in \begin{cases} \psi_i^L & \text{if } \int_L |\psi_i(\vec{r})|^2 d^3r > \int_{C/R} |\psi_i(\vec{r})|^2 d^3r, \\ \psi_i^C & \text{if } \int_C |\psi_i(\vec{r})|^2 d^3r > \int_{L/R} |\psi_i(\vec{r})|^2 d^3r, \\ \psi_i^R & \text{if } \int_R |\psi_i(\vec{r})|^2 d^3r > \int_{L/C} |\psi_i(\vec{r})|^2 d^3r \end{cases}$$

# QFL splitting: Where is the “voltage” drop?

- Electrostatic potential drop: Why nonlinear drop @ hexatriene-dithiolate?



*Electrochemical potential drop*

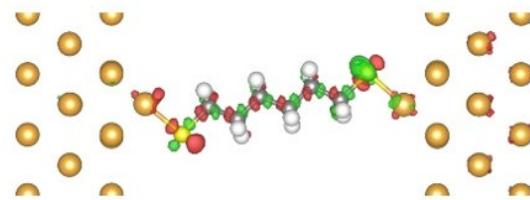
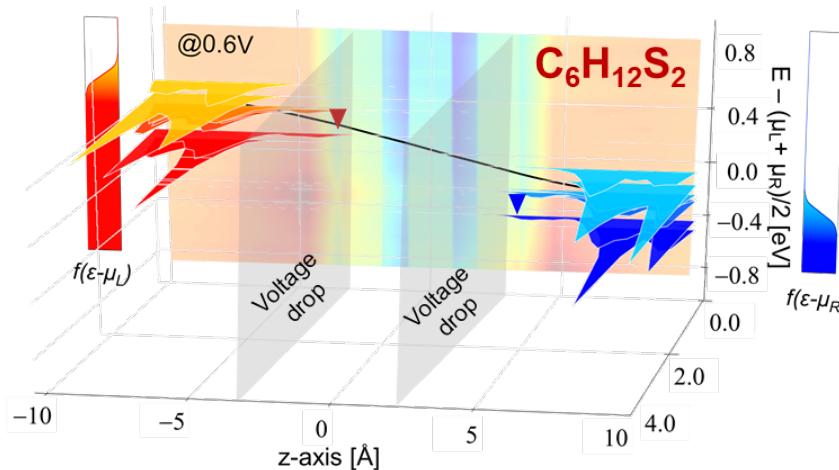
$$V = \frac{\mu_1(\mathbf{r}_2) - \mu_1(\mathbf{r}_1)}{e} = \phi(\mathbf{r}_2) - \phi(\mathbf{r}_1) + \frac{\bar{\mu}(\mathbf{r}_2) - \bar{\mu}(\mathbf{r}_1)}{e}$$

*Electrostatic potential drop*

*Chemical potential drop*

# Electrostatic potential drops

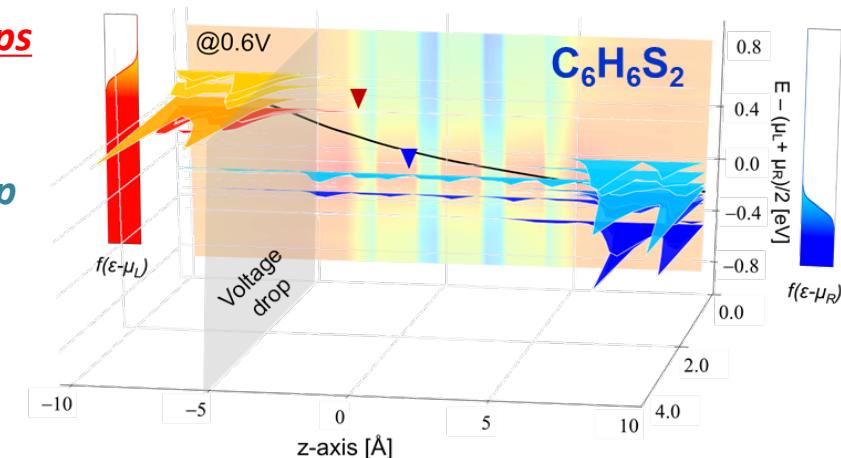
Hexane-dithiolate



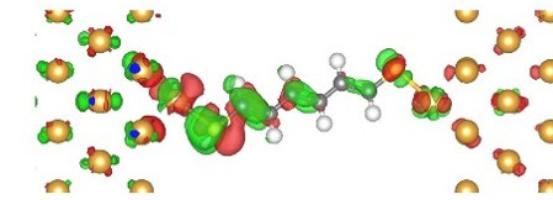
"Voltage" drops

*Electrostatic potential drop*

Hexatriene-dithiolate

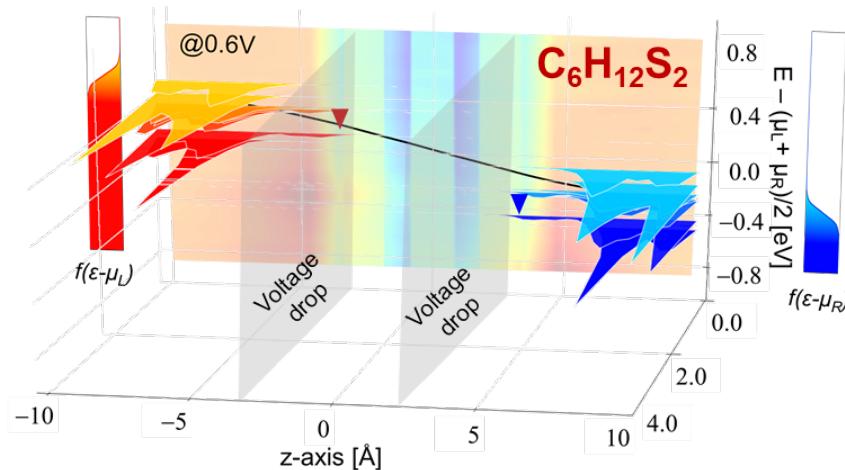


*Landauer residual resistivity dipole*

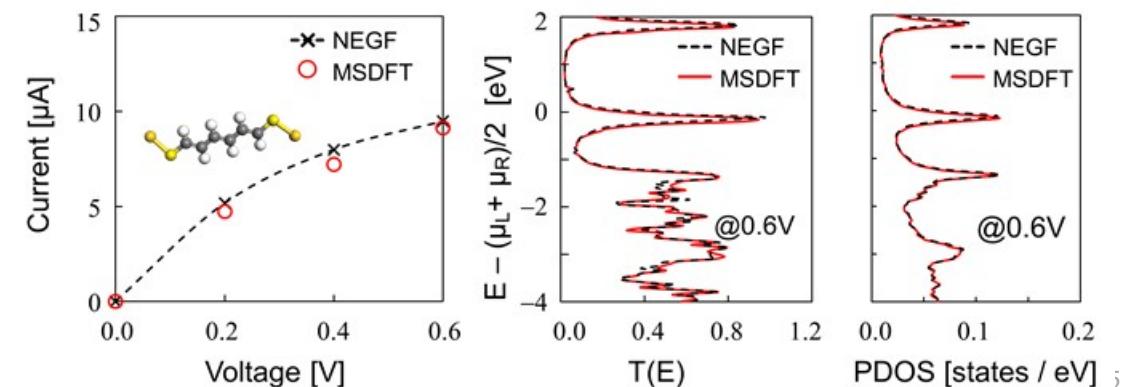
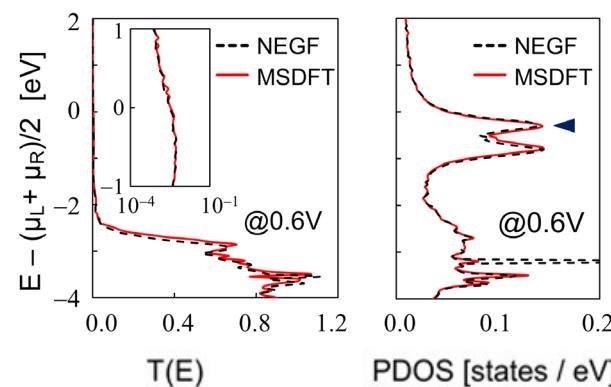
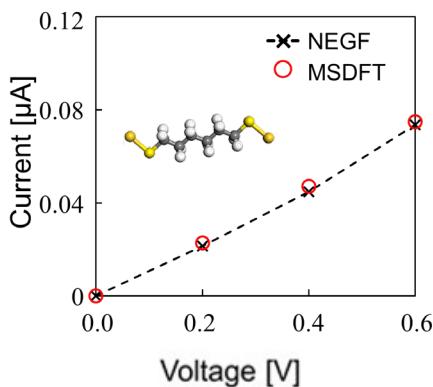
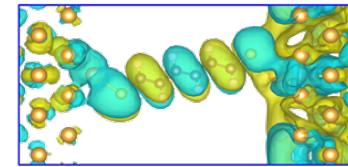
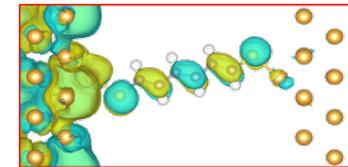
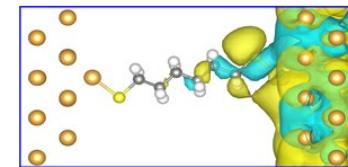
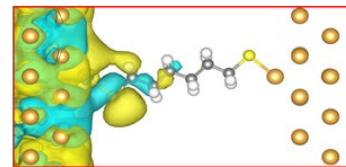
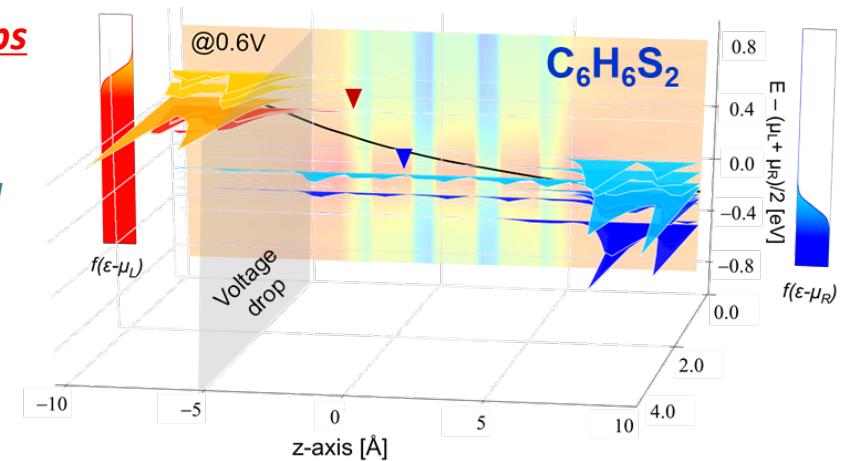


# Electrochemical potential drops (QFLs)

Hexane-dithiolate



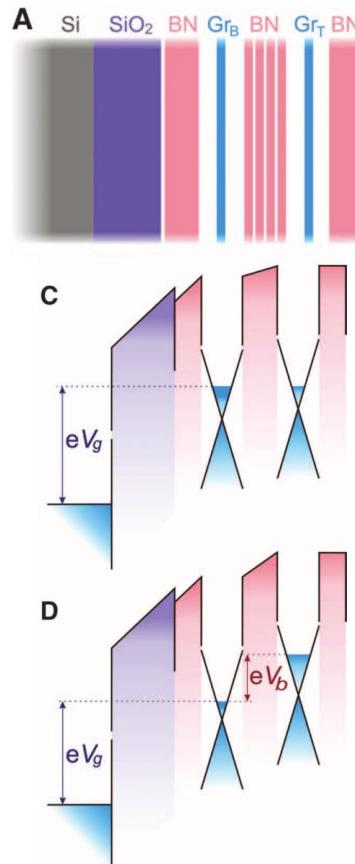
Hexatriene-dithiolate



### 3. 2D vdW devices: e.g. Gr/hBN/Gr heterojunctions

#### Vertical tunneling field effect transistor (FET)

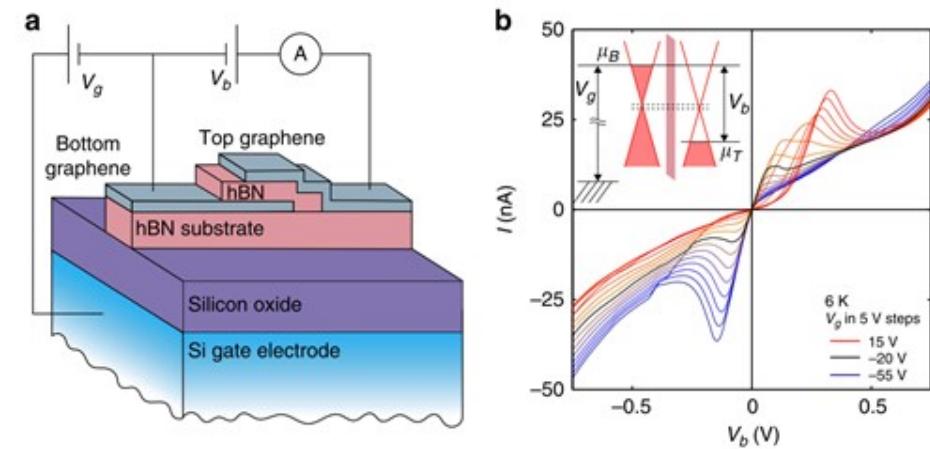
L. Britnell *et al. Science* 335, 947 (2012)



Modulation of **tunneling** currents  
→ On/Off  $\approx 1 \times 10^4$

- *Negative Differential Resistance (NDR)*

L. Britnell *et al. Nat. Commun.* 4, 1794 (2013)



- *High photocurrent*

L. Britnell *et al. Science* 340, 1311 (2013), etc.

- *Chiral quantum states*

J. Wallbank *et al. Science* 353, 6299 (2016), etc.

- *Giant tunneling magnetoresistance*

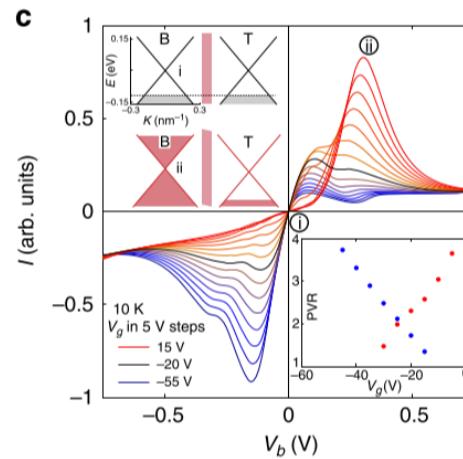
T. Song *et al. Science* 360, 1214 (2018), etc.

- *etc.*

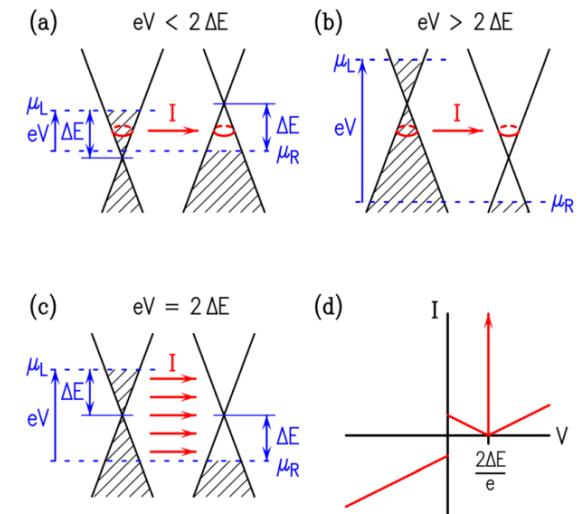
# Only semi-classical theory (not NEGF)

- Semi-classical Bardeen approach

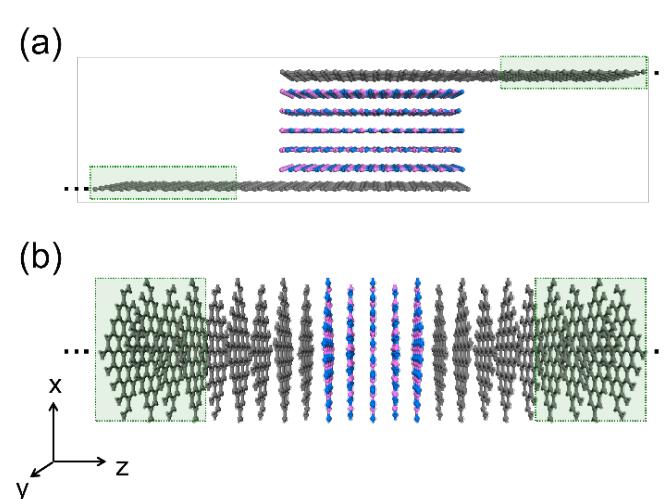
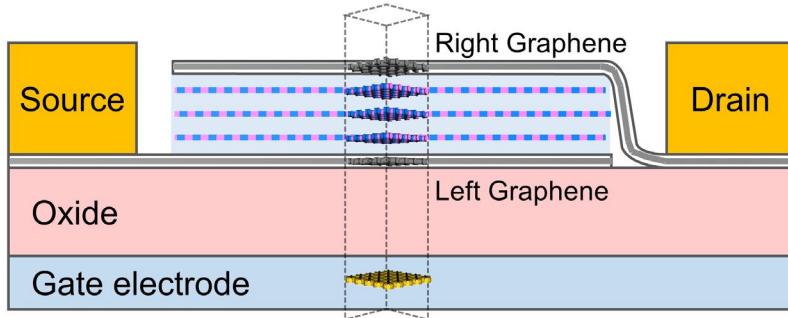
$$I = g_V \frac{4\pi e}{\hbar} \sum_{\alpha, \beta} |M_{\alpha\beta}|^2 [f_L(E_\alpha) - f_R(E_\beta)] \delta(E_\alpha - E_\beta)$$



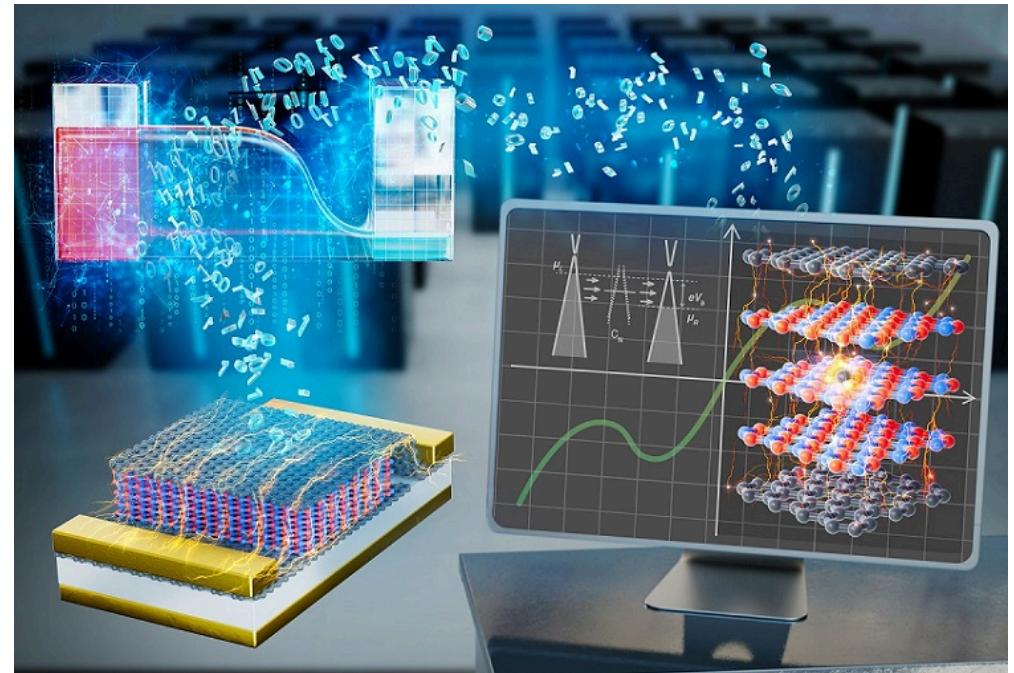
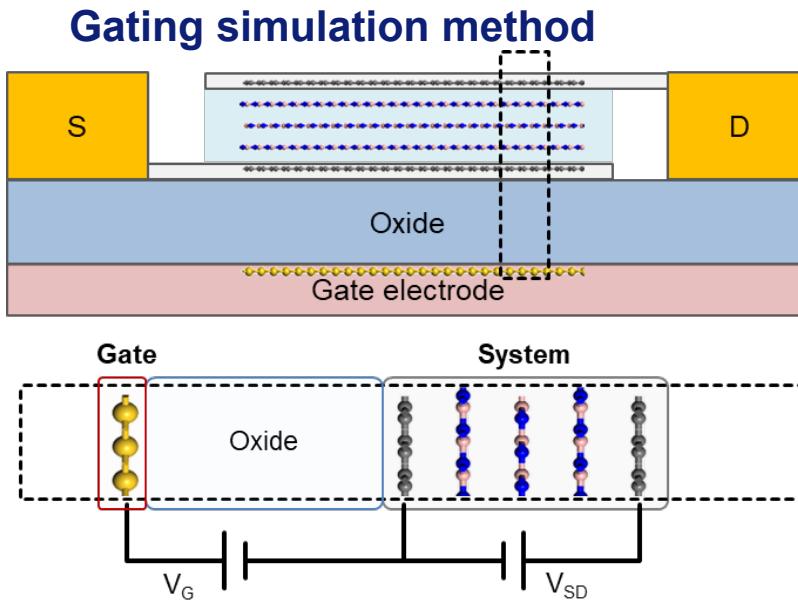
L. Britnell *et al.*  
*Nat. Commun.* **4**, 1794 (2013)



Feenstra *et al.*  
*J. Appl. Phys.* **111**, 4 (2012)



# MS-DFT for graphene tunneling “FET”



1. “Constrained search”:

$V_G$  as a constraint that precedes  $V_{SD}$

2. Transmission:

$$T(E; V_b, V_g) = \text{Tr}[\mathbf{a}_L \mathbf{M} \mathbf{a}_R \mathbf{M}^\dagger]$$

T.H. Kim, J. Lee, R.-G. Lee, & YHK, Npj Comput. Mater. **8**, 50 (2022)

Son *et al.*, Appl. Surf. Sci. **581**, 152396 (2022)

Seo *et al.*, Adv. Mater. **33**, 2102980 (2021)



Taehyung Kim

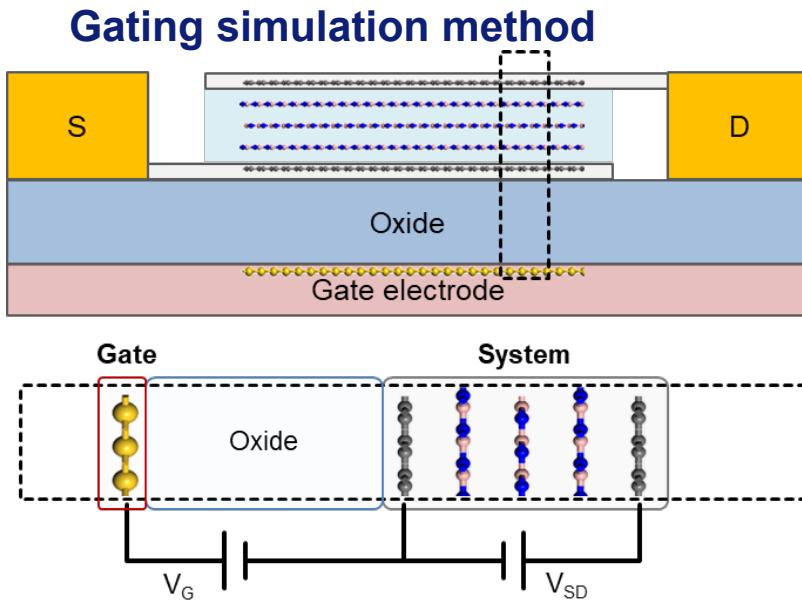


Juho Lee



Ryong Gyu Lee

# MS-DFT for graphene TFET: $V_G = +1V$

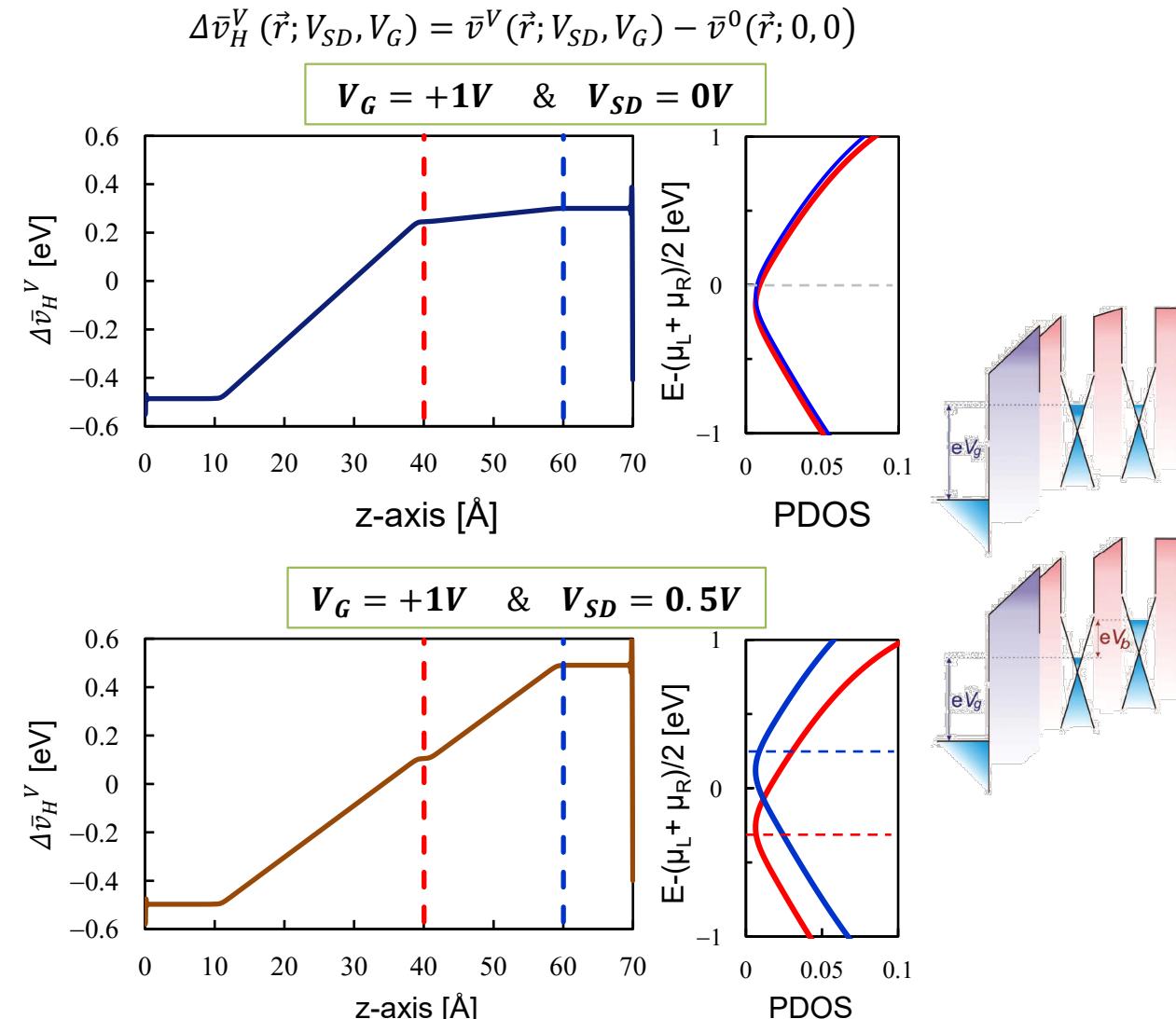


1. “Constrained search”:

$V_G$  as a constraint that precedes  $V_{SD}$

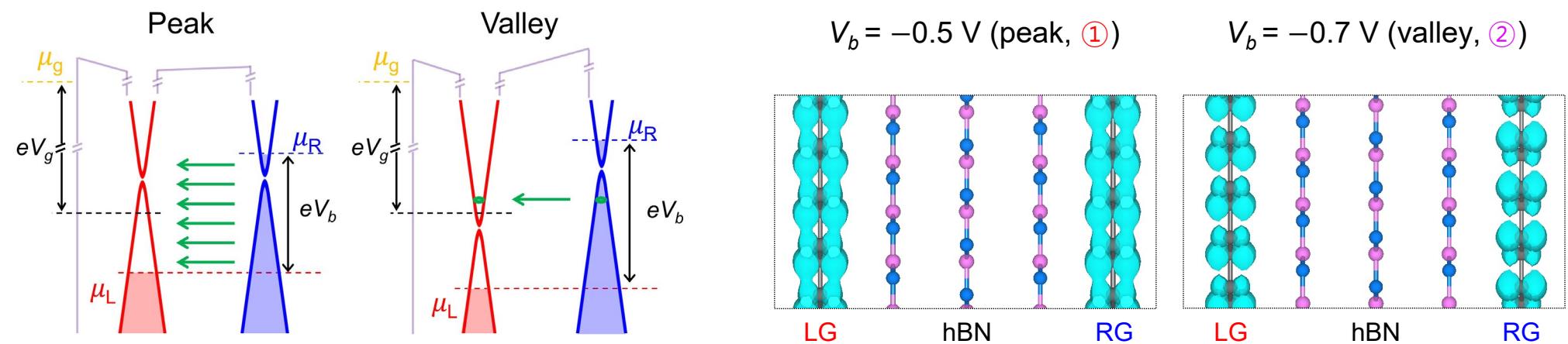
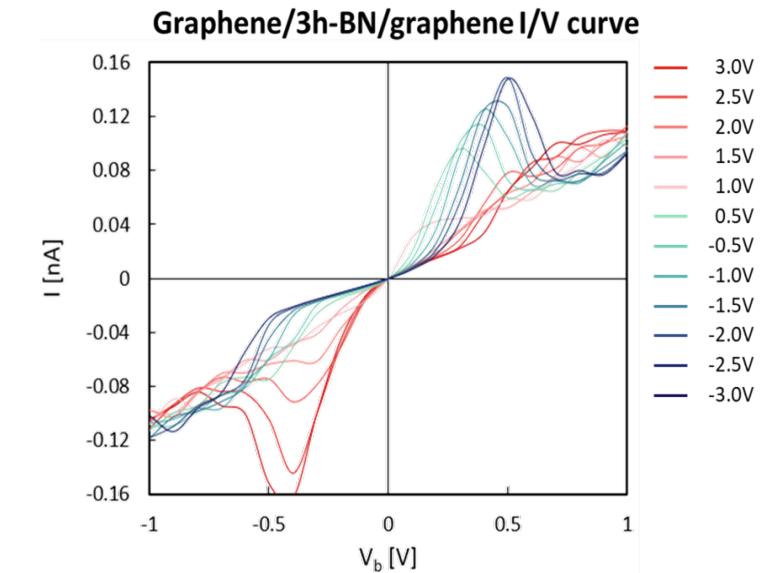
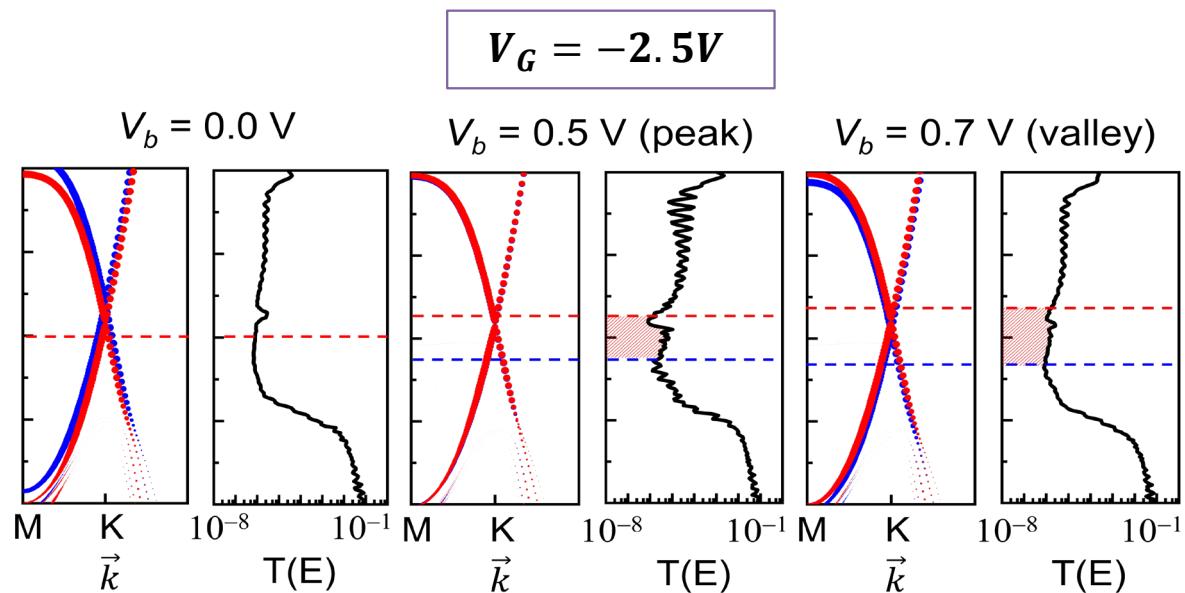
2. Transmission:

$$T(E; V_b, V_g) = \text{Tr}[\mathbf{a}_L \mathbf{M} \mathbf{a}_R \mathbf{M}^\dagger]$$



- Quantum capacitance → Field partial penetration

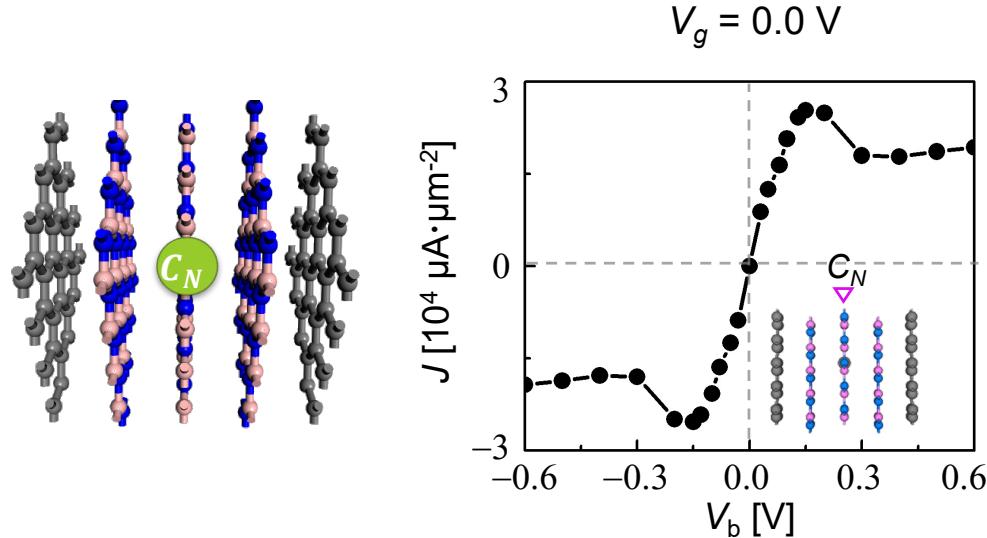
# NDR @ Gr/pristine hBN/Gr TFET ← MS-DFT



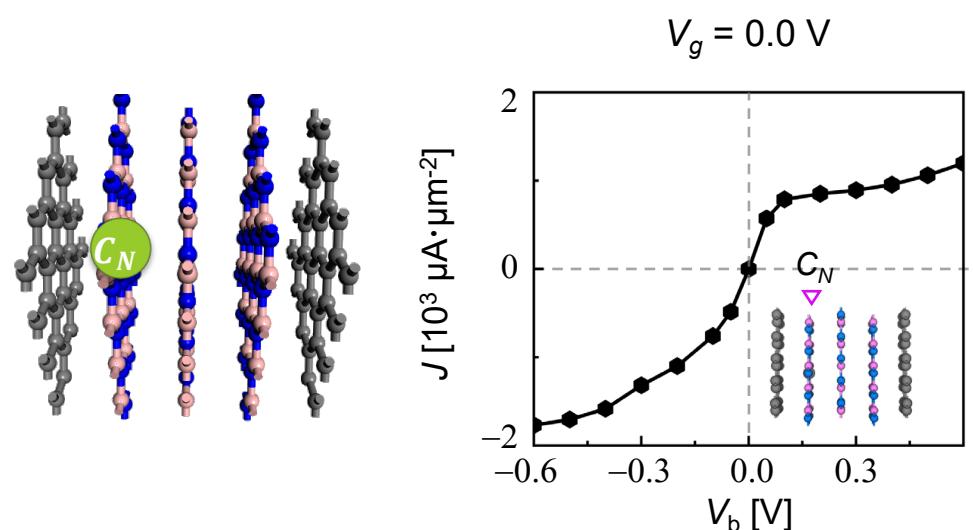
# Gr/defective hBN/Gr: I-V & voltage drop

## Computational setup

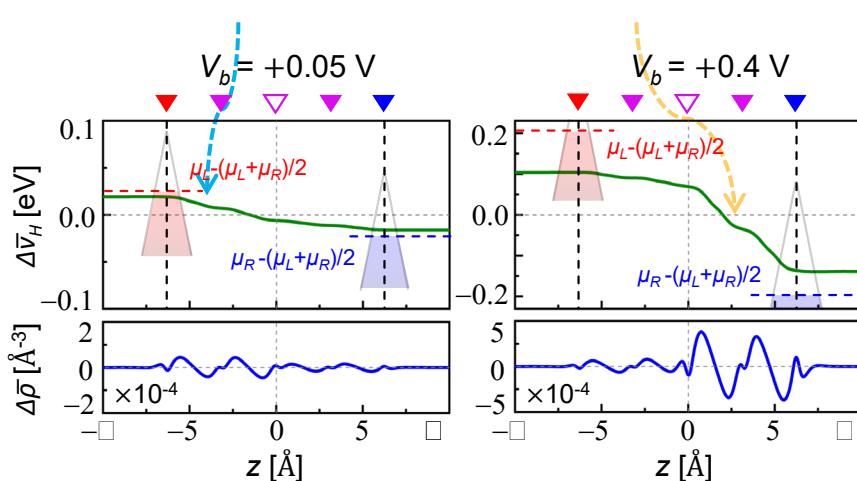
$C_N$  defect @ middle hBN



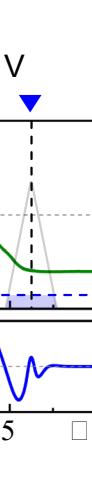
$C_N$  defect @ interfacial hBN



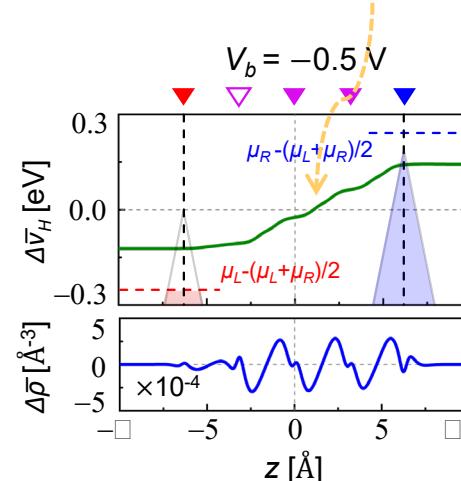
$V$  drop @ left



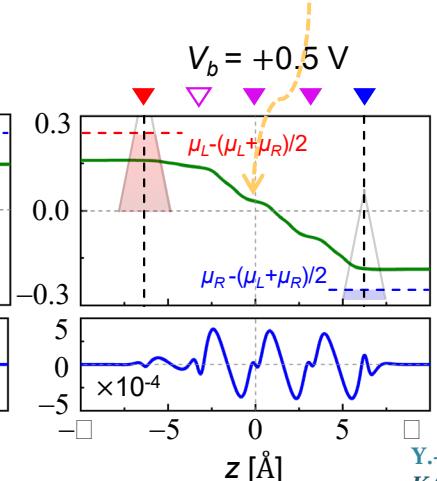
$V$  drop @ right



$V$  drop @ right

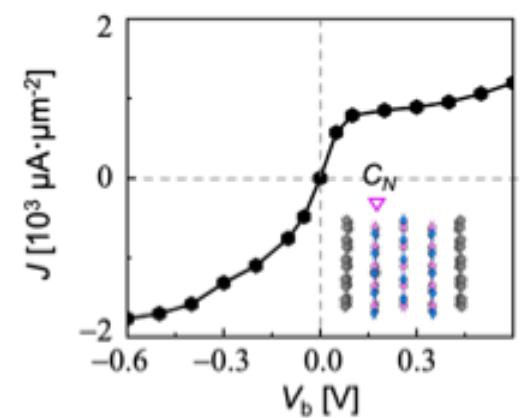
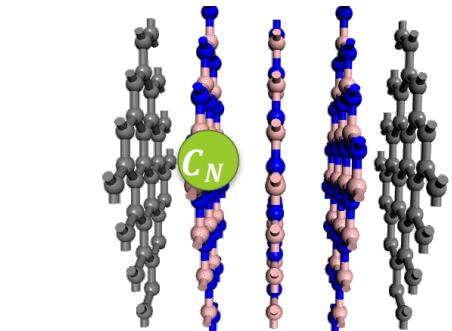
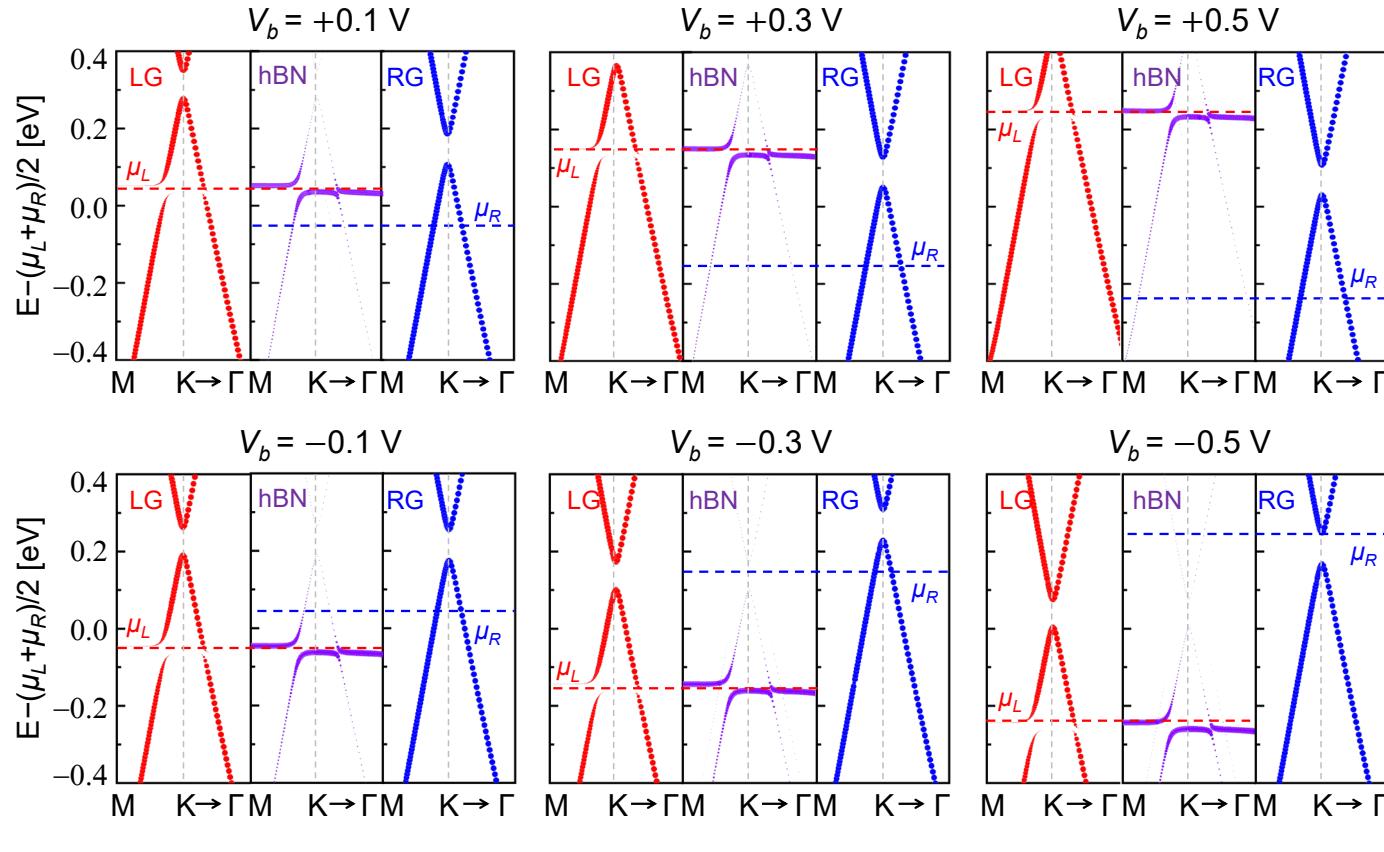


$V$  drop @ right



# Gr/defective hBN/Gr: $C_N$ @ interfacial hBN $\rightarrow$ No NDR

T.H. Kim, J. Lee, R.-G. Lee, & YHK,  
Npj Comput. Mater. **8**, 50 (2022)

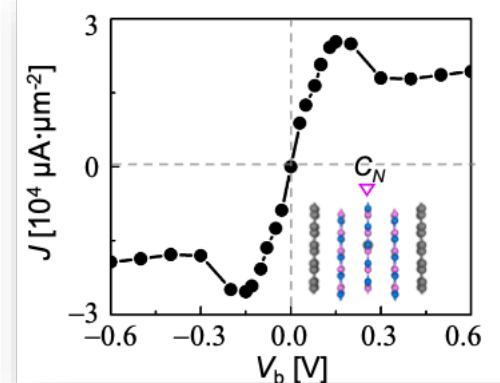
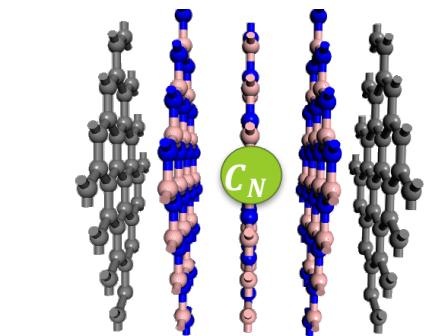
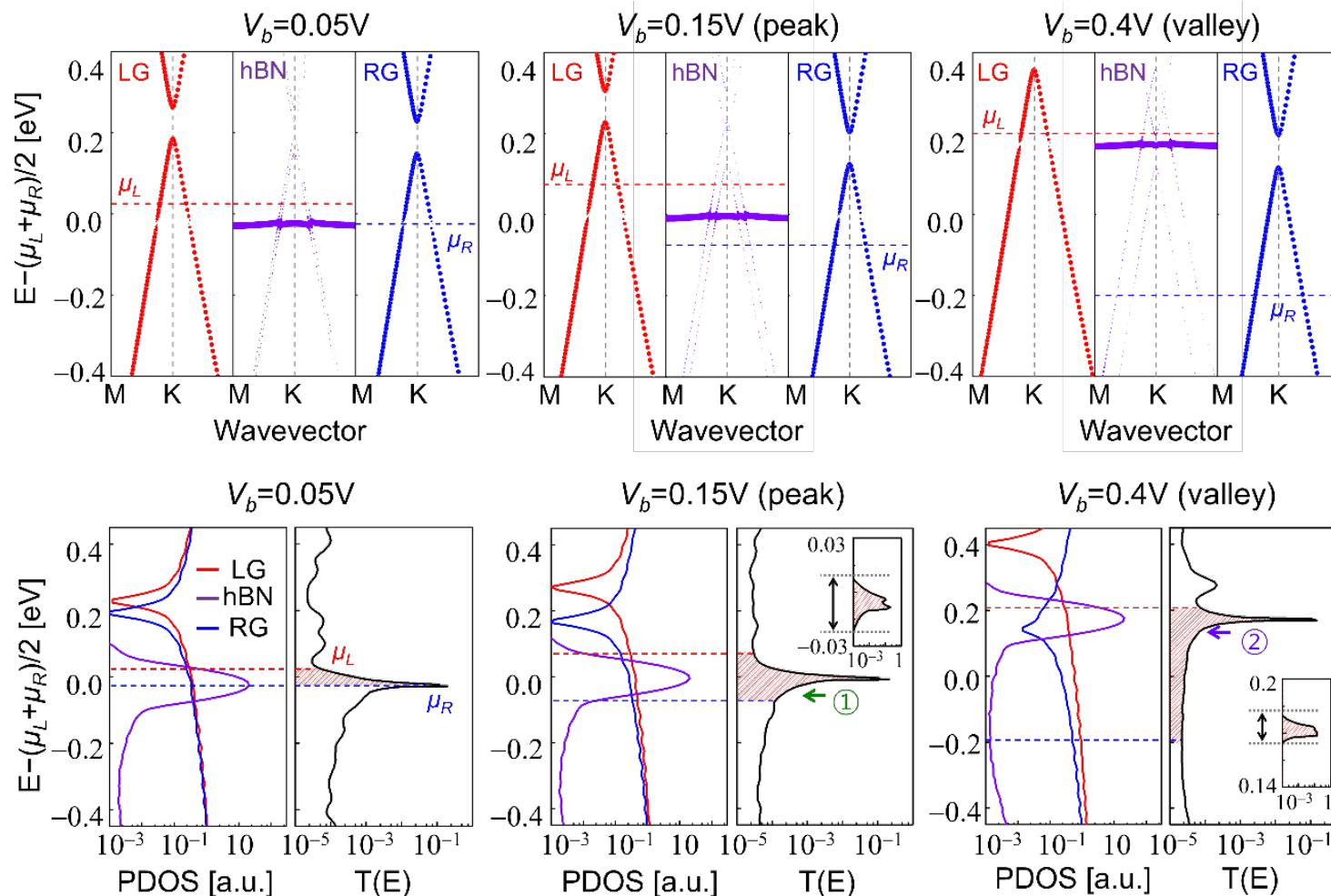


- Pinning of  $C_N$  defect @ left Gr

# Gr/defective hBN/Gr: $C_N$ @ middle hBN → symmetric NDR

IWCN 2023  
June 12, 2023

T.H. Kim, J. Lee, R.-G. Lee, & YHK,  
Npj Comput. Mater. **8**, 50 (2022)

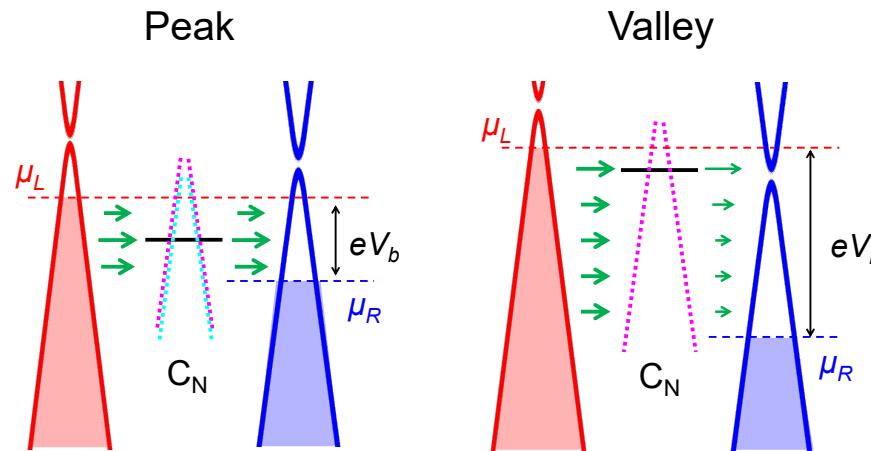
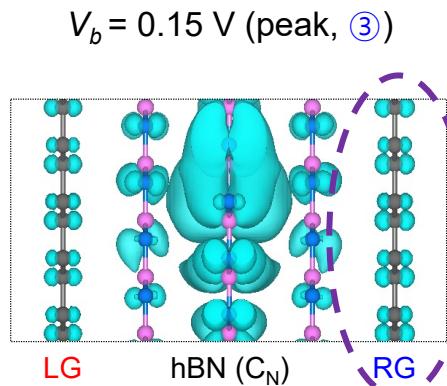


- Self-consistent filling of  $C_N$  defect levels → upshift with  $V_b$
- $C_N$  defect level-mediated symmetric NDR

# Gr/defective hBN/Gr: $C_N$ @ middle hBN $\rightarrow$ QH-NDR

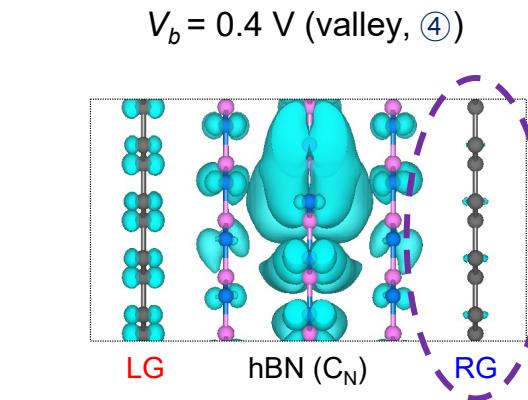
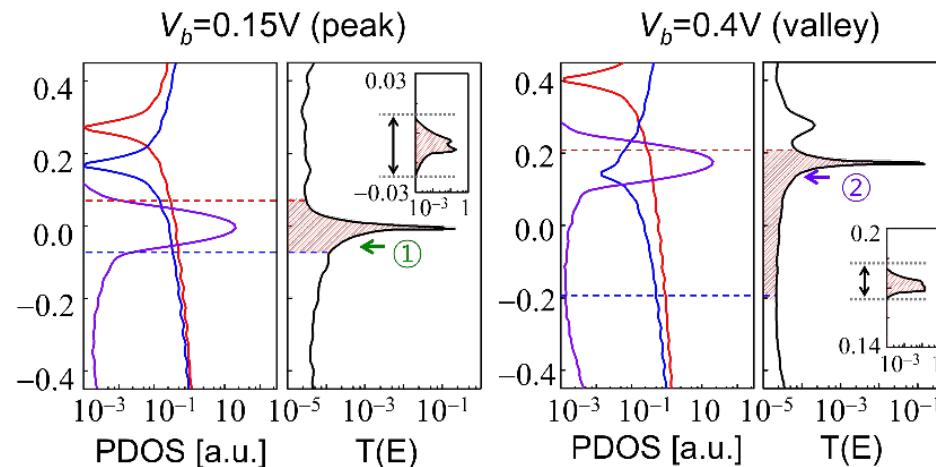
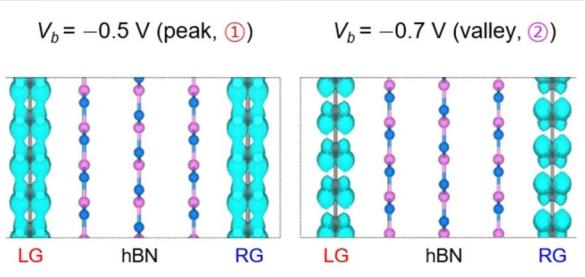
## Quantum-Hybridization NDR

T.H. Kim, J. Lee, R.-G. Lee, & YHK,  
Npj Comput. Mater. **8**, 50 (2022)

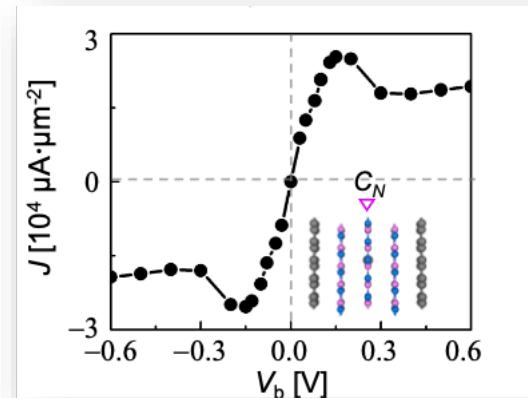


Quantum  
hybridization (QH):  
Strong

cf.



Quantum  
hybridization (QH):  
Weak



- Self-consistent filling of  $C_N$  defect levels  $\rightarrow$  upshift with  $V_b$
- $C_N$  defect level-mediated NDR  $\rightarrow$  QH-NDR

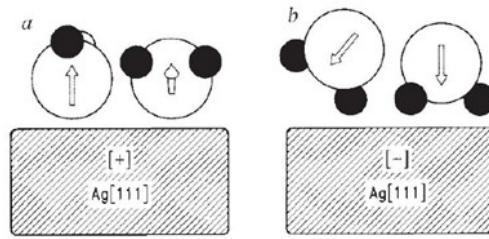
# 4. Interfacial water from first-principles?

LETTERS TO NATURE

M. F. Toney *et al.* Nature 368, 444 (1994)

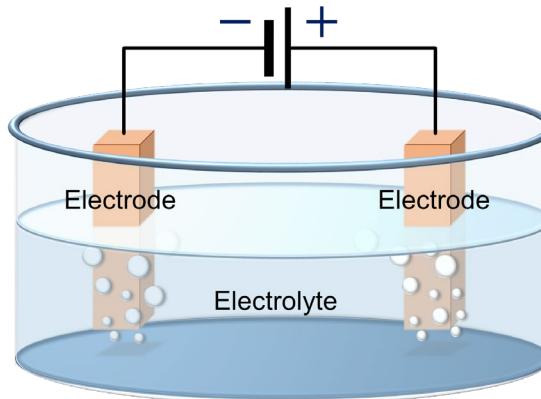
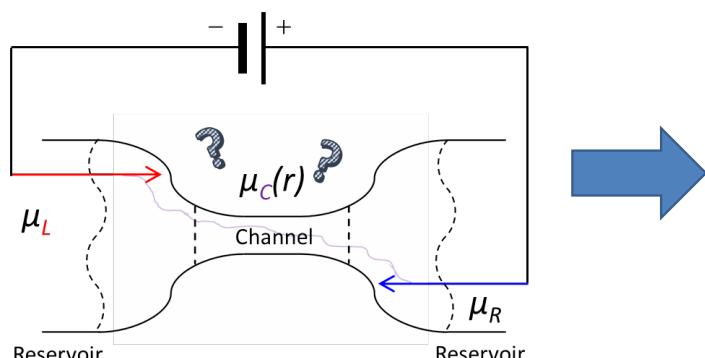
## Voltage-dependent ordering of water molecules at an electrode–electrolyte interface

Michael F. Toney\*, Jason N. Howard\*†,  
Jocelyn Richer\*†, Gary L. Borges\*,  
Joseph G. Gordon\*, Owen R. Melroy\*,  
David G. Wiesler†, Dennis Yee§  
& Larry B. Sorenson§



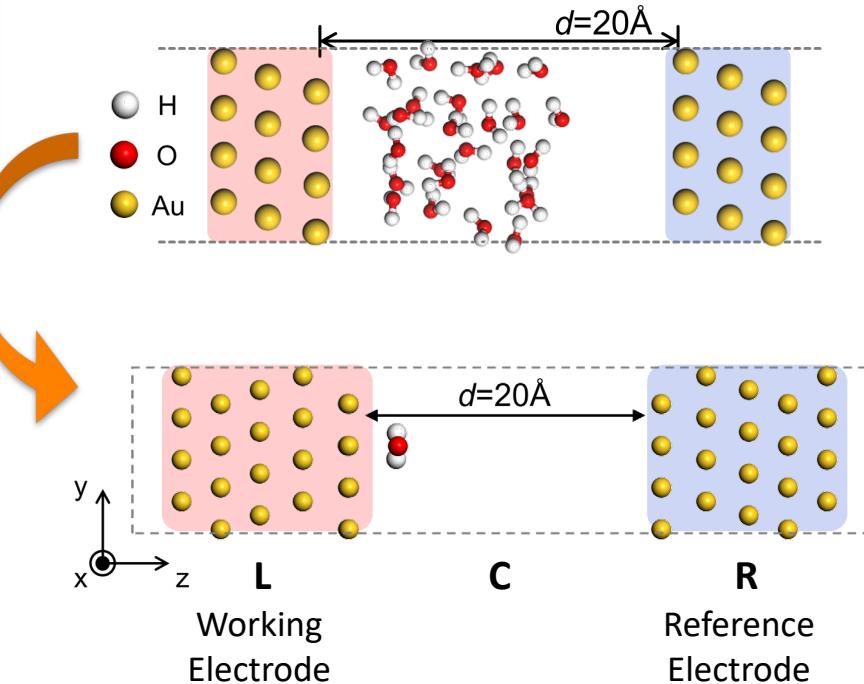
Quantum transport → Electrolytic cell

$$V = \Delta\mu = \mu_L - \mu_R$$



$$\Phi = -\frac{V_b}{2} = -\frac{(\mu_L - \mu_R)}{2e}$$

Models

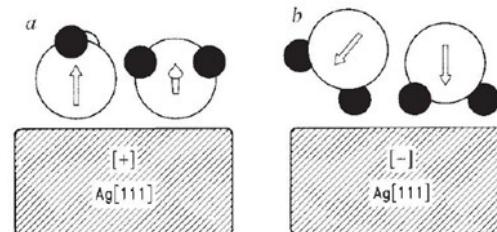


## LETTERS TO NATURE

M. F. Toney *et al.* Nature 368, 444 (1994)

### Voltage-dependent ordering of water molecules at an electrode–electrolyte interface

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?

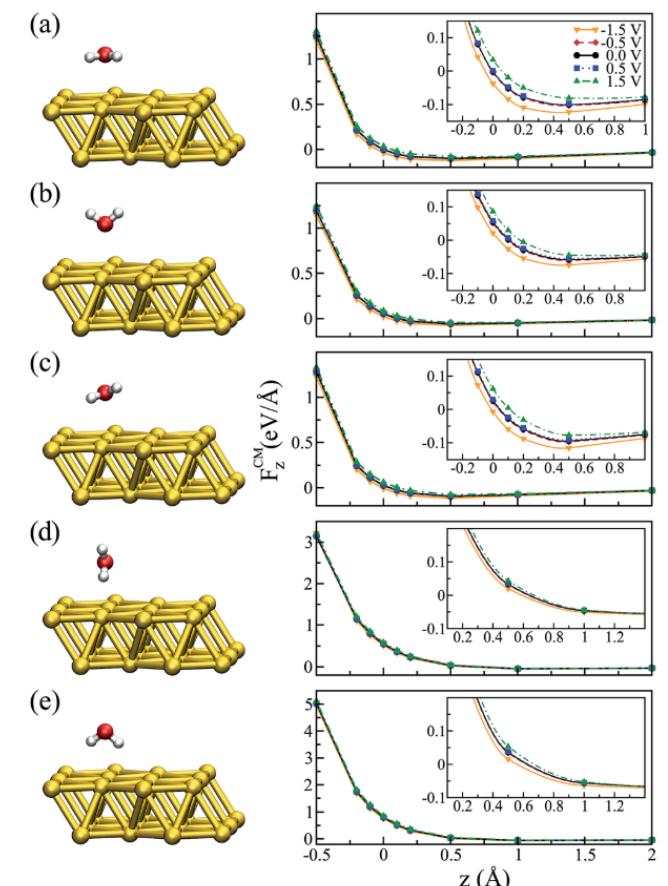
### Bias-dependent local structure of water molecules at a metallic interface†

Luana S. Pedroza,\*<sup>ab</sup> Pedro Brandimarte,<sup>ID cd</sup> Alexandre Reily Rocha<sup>ID e</sup>  
and M.-V. Fernández-Serra<sup>ID fg</sup>

- Hellmann-Feynman forces:

$$\vec{F}_I = - \frac{\partial \langle \psi^{L/C/R} | \hat{H} | \psi^{L/C/R} \rangle}{\partial \vec{R}_I}$$

- But no energy ...  $\langle \psi^{L/C/R} | \hat{H} | \psi^{L/C/R} \rangle$  ?



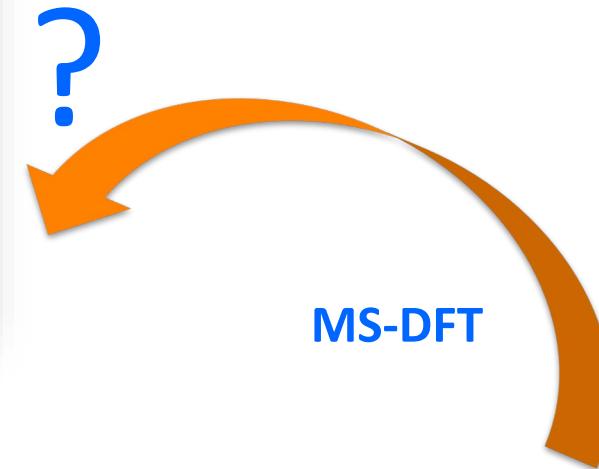
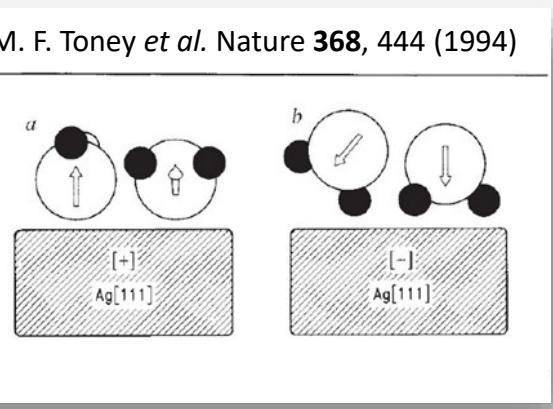
# Q. Interfacial water ← MS-DFT?

LETTERS TO NATURE

M. F. Toney *et al.* Nature 368, 444 (1994)

## Voltage-dependent ordering of water molecules at an electrode–electrolyte interface

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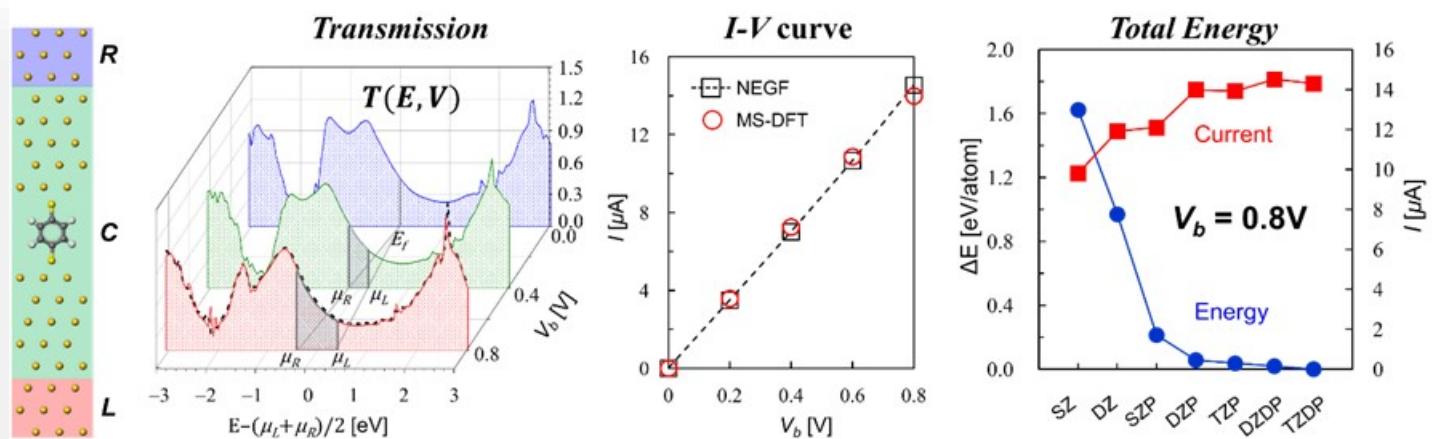


Total energy  $E_{L+C+R}^V$ :

NOT enough!

→ Q. Appropriate

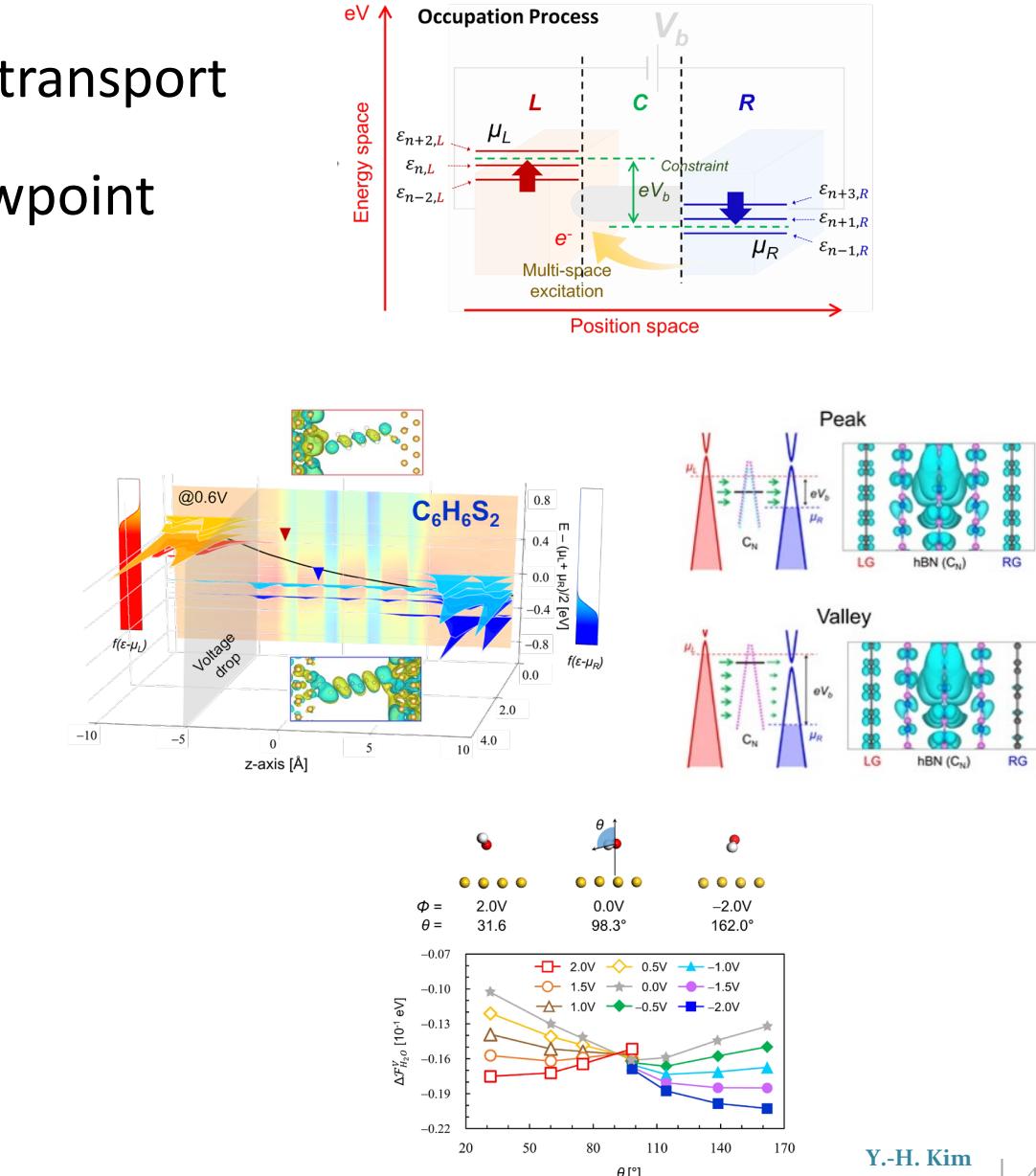
Free energy ?



- I. Background information: DFT, NEGF, & Landauer
- II. MS-DFT: development & its applications
- III. Summary

# Summary

- “Multi-space excitation” for quantum transport
  - An alternative to the Landauer viewpoint
  - Formulation of MS-DFT (vs. NEGF)
- Advantages and Applications
  - Quasi-Fermi levels: “Voltage drop”
  - Graphene-based nanodevices
  - Total energy
  - Electric enthalpy (of formation)
  - Interfacial water (and beyond ...)



## Group Members

<http://nanocore.kaist.ac.kr/yhklab>

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- Dr. Junho Park
- Dr. Junho Lee
- **Dr. Kaptan S. Rajput**
- Ms. Hyo Jin Jeon

### PhD Students

- Tae Hyung Kim
- Hyunwoo Yeo
- Ryongyu Lee

### Alumni

- Dr. Juho Lee
- Dr. Han Seul Kim

### MS Students

- |      |                |                  |
|------|----------------|------------------|
| Thu. | • Seunghyun Yu | Wed.<br>(poster) |
| Tue. | • Jaeun Kim    |                  |
|      | • Jiyoong Song |                  |



## Funding



한국연구재단  
National Research Foundation of Korea



감사합니다.

*Thank you!*