

# Polaritonic features in the THz displacement current through RTDs in microcavities

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(electrons and fields at the same foot)

# INTRO

## Matter (electrons)

- Micrometer or larger sizes

Semiclassical models. Electrons as particles. Trajectories, ...

- Nanometer scale

Quantum models. Energy level quantization. NDR, ...

## Electromagnetic fields

- GigaHertz or smaller frequencies

Poisson equation ( $\mathbf{E}_{\parallel}(\mathbf{r})$ ) within a quasistatic approximation.

- 0.1-10 TeraHertz (THz gap)

Maxwell equations ( $\mathbf{E}_{\perp}(\mathbf{r}), \mathbf{B}_{\perp}(\mathbf{r})$ ) coupled to a transport model.

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## Nanoscale devices at THz (RTDs in engineered microcavities)

- Similar energy scales. Quantization of both electrons and electromagnetic fields.
- Light-matter resonant coupling parameter  $\gamma = \omega_r / \omega$  [  $\omega = (E_1 - E_0) / \hbar$ ,  $\omega_r = \text{Rabi}$  ].
- Closed system models: Jaynes-Cummings, ...
- Open system models: ???

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### Small coupling ( $\gamma < 0.1$ )

- Perturbative models. Fermi Golden Rule.
- Collisions. Photon absorption/emission.



- Experimental advances.
- Platforms with  $\gamma = 1.2$ .

### Strong coupling ( $\gamma > 0.5$ )

- Need of new theoretical models.
- 3N-electron 2M-mode undoable. QEDFT, ...

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- Resonant single-mode cavity field.
- Dipole approximation ( $\lambda_{cavity} \gg W_{device}$ ).

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## Our work

- Qualitative initial model for nanoscale at THz within strong coupling.
- Born-Huang wavefunction. Ramo-Shockley-Pellegrini current.
- Signatures of field quantization in electron transport are identifiable?

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Resonant tunneling diodes strongly coupled to the cavity field

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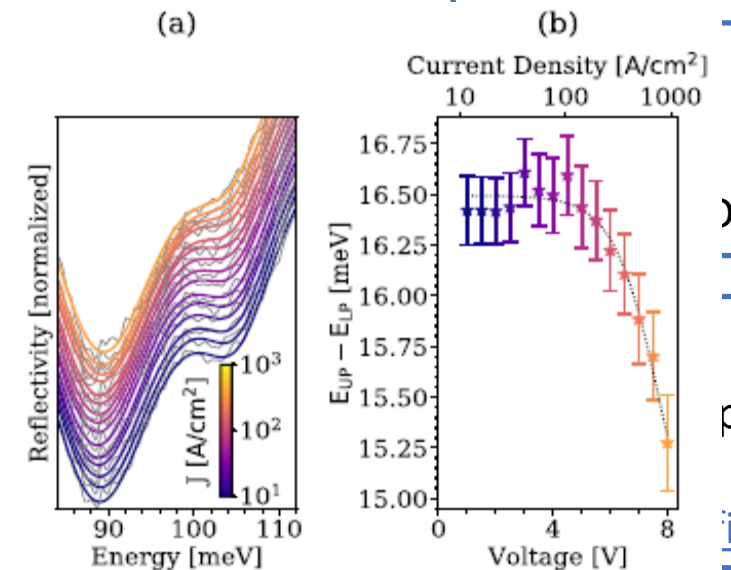
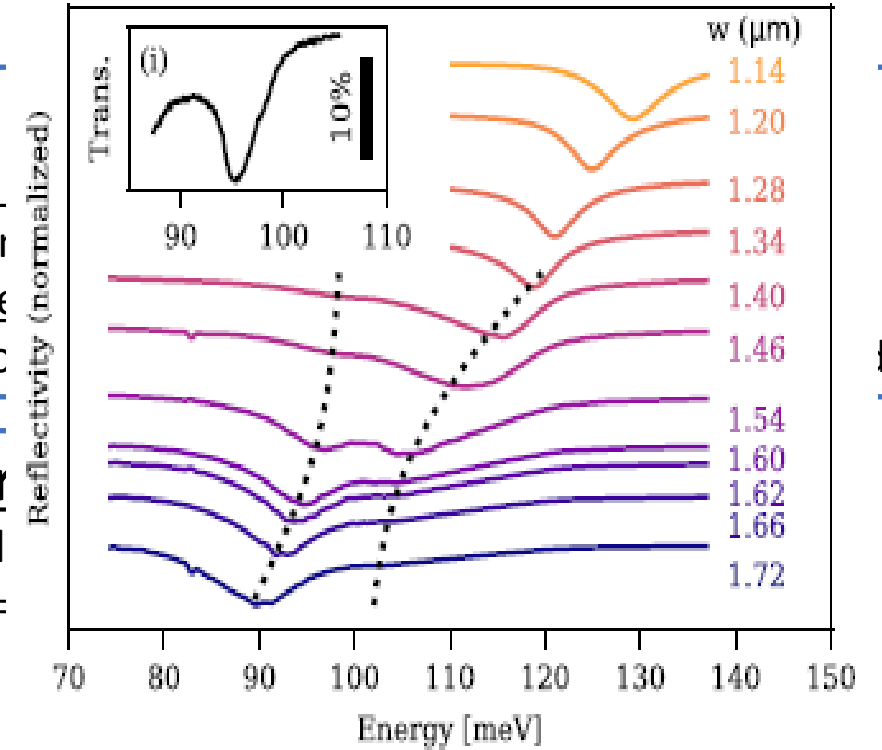
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# HAMILTONIAN ( $H = H_0 + H_{\omega 0}$ )

Spinless non-relativistic minimal coupling (Coulomb gauge, dipole approximation)

Transversal fields

$$H_0 = \sum_{j=1}^N \left\{ \frac{1}{2m_e} [i\hbar\nabla_j + e\mathbf{A}(\mathbf{r}_j)]^2 + eU(\mathbf{r}_j) + V(\mathbf{r}_j) \right\}$$

Longitudinal field  $\mathbf{E}_{\parallel}(\mathbf{r})$

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Quantization procedure (  $n = 1, \dots, M ; \lambda = 1, 2$  )

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$a_{n,\lambda}^{\dagger}/a_{n,\lambda}$  in terms of displacement coordinates  $q_{n,\lambda}$  and their conjugate momenta  $\partial/\partial q_{n,\lambda}$ .

$$a_{n,\lambda} = \frac{1}{\sqrt{2}} \left( q_{n,\lambda} + \frac{\partial}{\partial q_{n,\lambda}} \right)$$

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Power-Zienau-Wooley (PZW) gauge transformation (3N + 2M degrees)

$$\{ \chi_{n,\lambda} = i/\sqrt{2\epsilon_0\hbar\omega_n} L_c^3 \epsilon_{n,\lambda} \cdot e \sum_{j=1}^N \mathbf{r}_j \}$$

$$H^{(D)} = \sum_{j=1}^N \left[ -\frac{\hbar^2 \nabla_j^2}{2m_e} + V(\mathbf{r}_j) + eU(\mathbf{r}_j) \right] + \sum_{n,\lambda} \hbar\omega_n |\chi_{n,\lambda}|^2 + \sum_{n,\lambda} \left( \frac{\hbar\omega_n}{2} \left[ q_{n,\lambda}^2 - \frac{\partial^2}{\partial q_{n,\lambda}^2} \right] + \sqrt{2}\hbar\omega_n |\chi_{n,\lambda}| q_{n,\lambda} \right)$$

$H_e^{(D)}$ 
 $\mathcal{E}_{s-dip}$ 
 $H_f^{(D)}$ 
 $H_{ef}^{(D)}$

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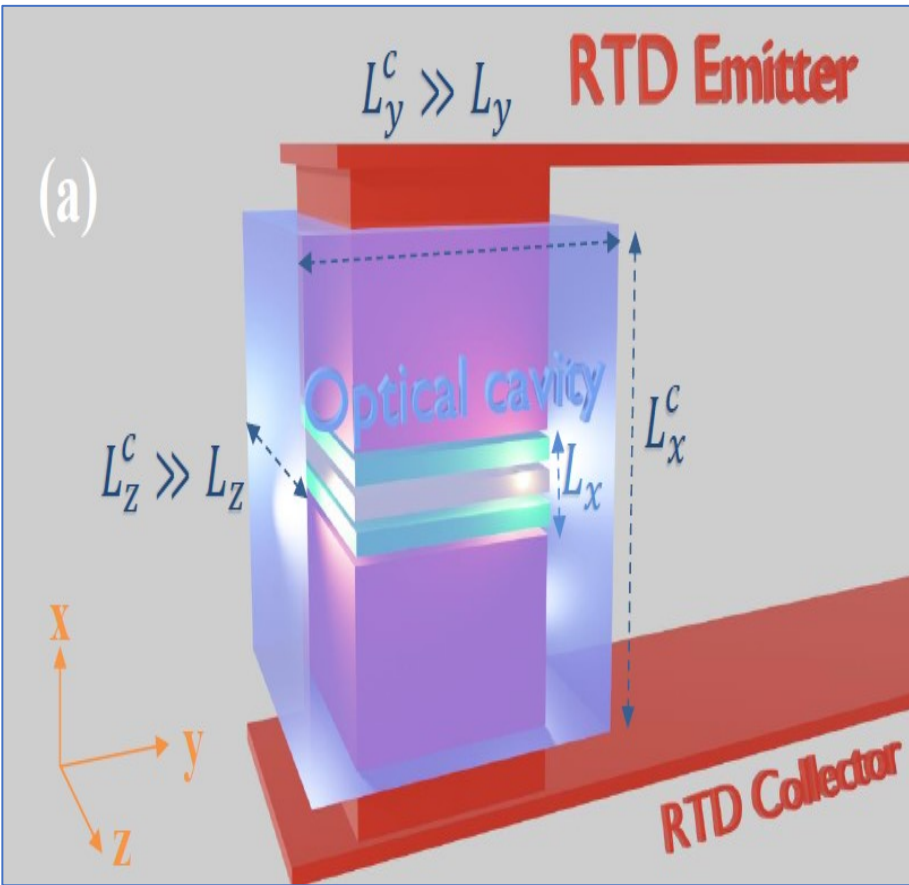
Initial approximations and use of conditional wave functions (effective 2D problem: single electron x, single mode q)

$$H_{xq}^{(D)} = -\frac{\hbar^2}{2m_e} \frac{\partial^2}{\partial x^2} + V(x) - \frac{\hbar\omega}{2} \frac{\partial^2}{\partial q^2} + \frac{\hbar\omega}{2} q^2 + \sqrt{2}\alpha qx$$

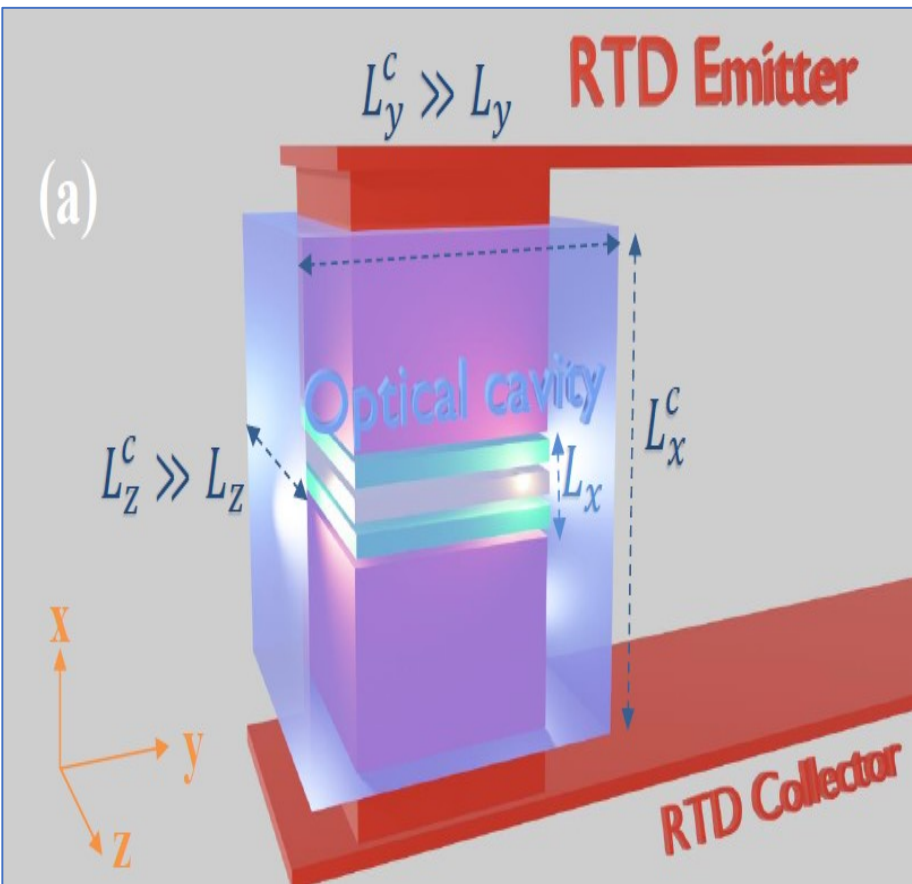
$$\alpha = \sqrt{e^2 \hbar \omega N / (2\epsilon_0 L_c^3)}$$

$$\omega_r = \sqrt{2}\alpha L_x / \hbar \propto \omega_p$$

# SETUP

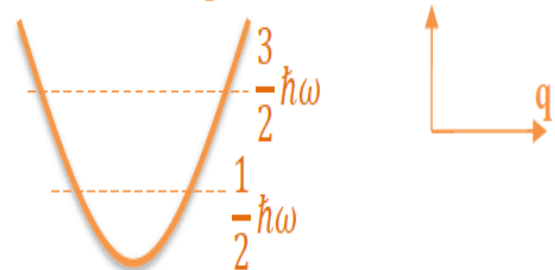


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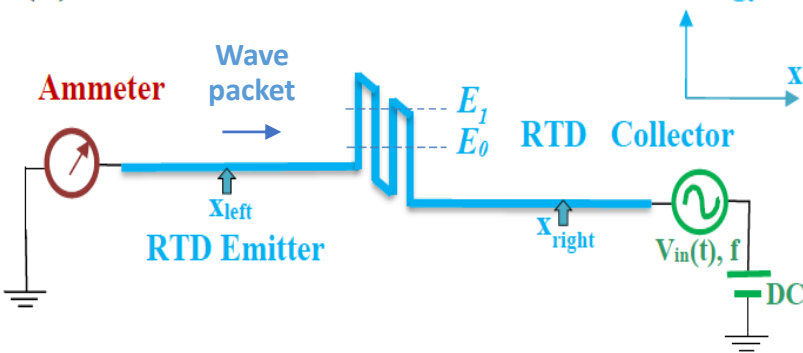
(b)

Potential for  $H_0$  and photon states

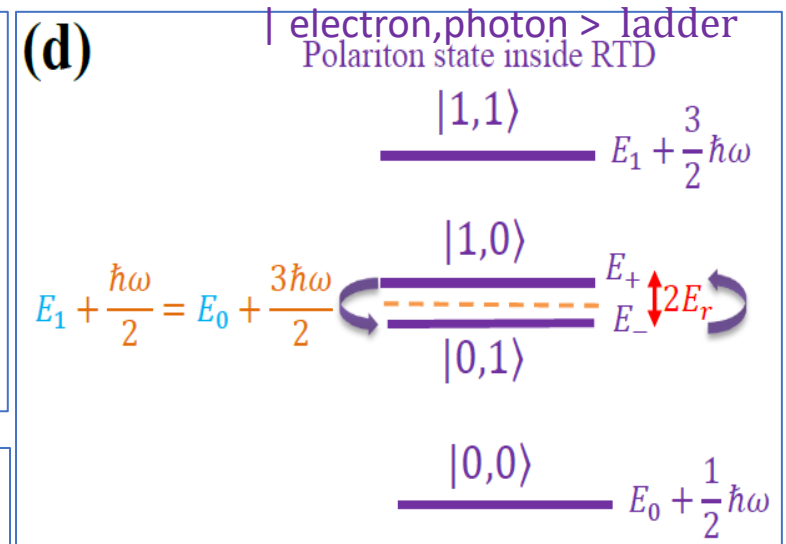
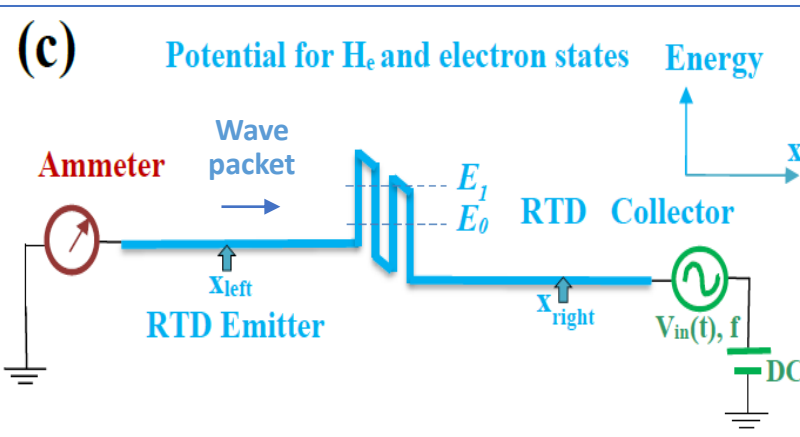
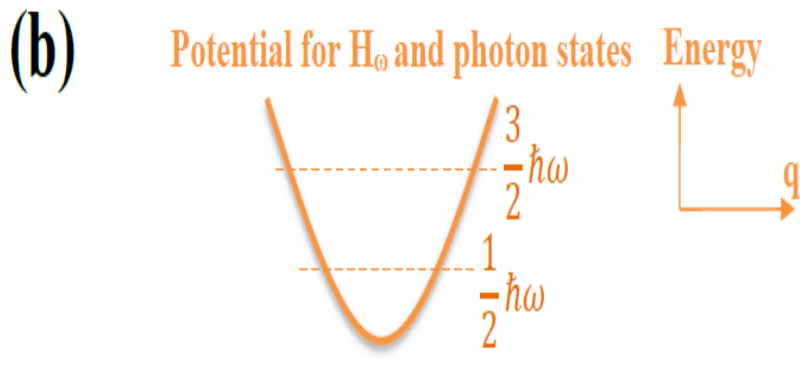
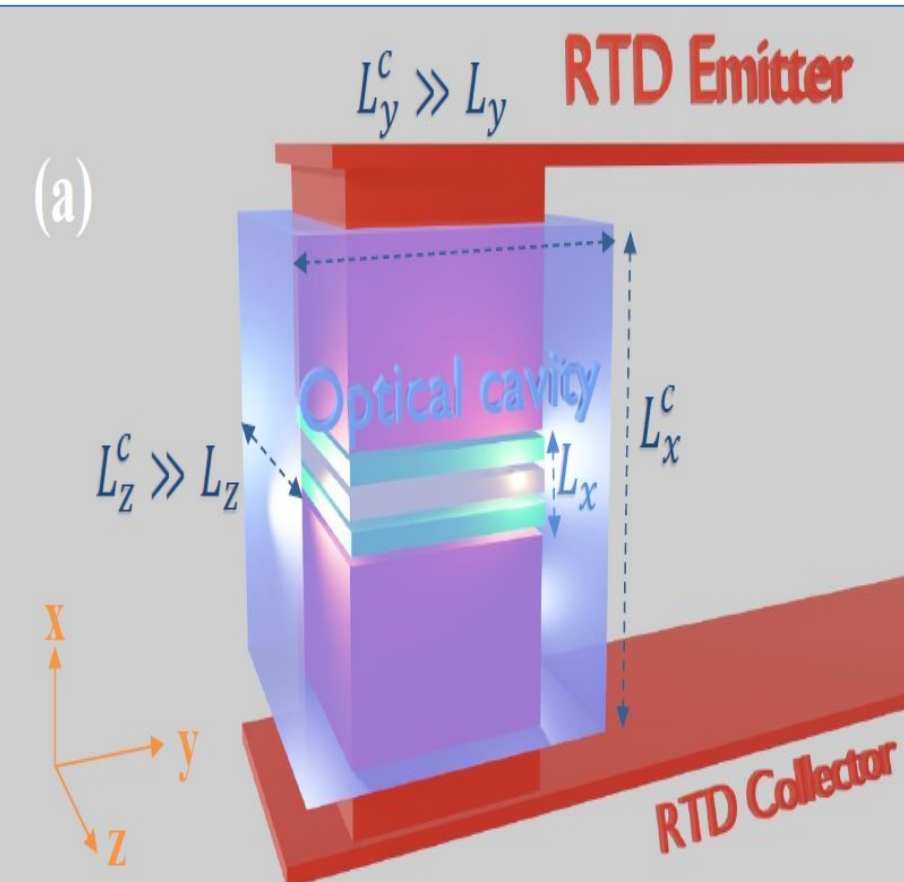


(c)

Potential for  $H_e$  and electron states



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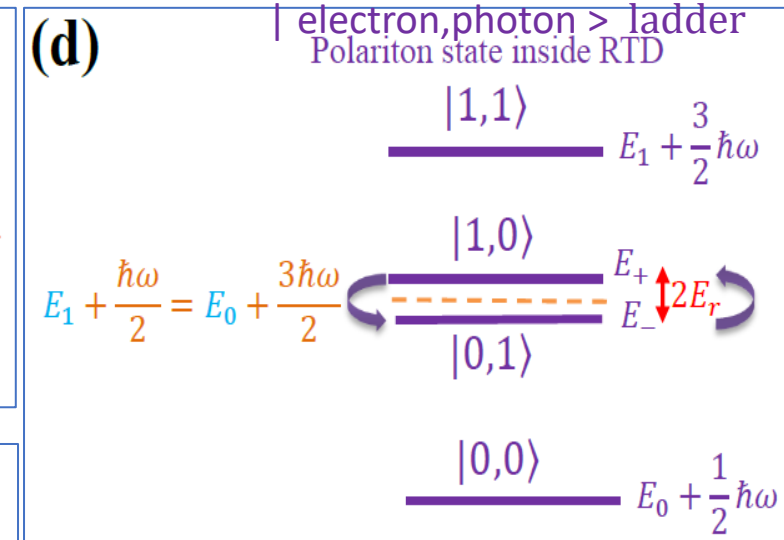
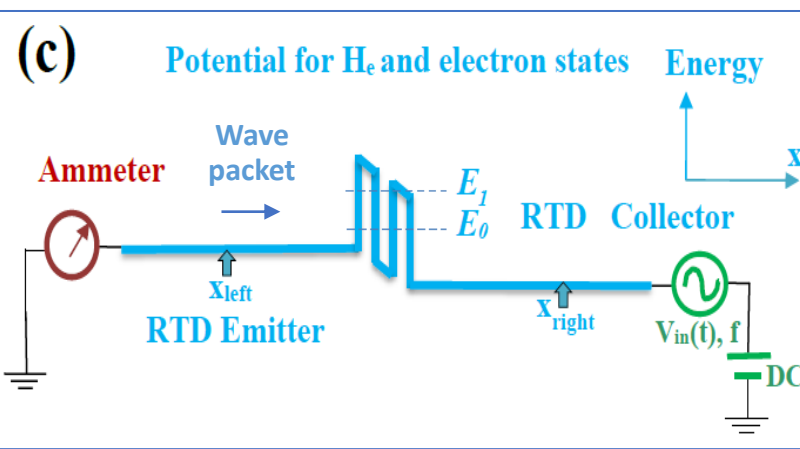
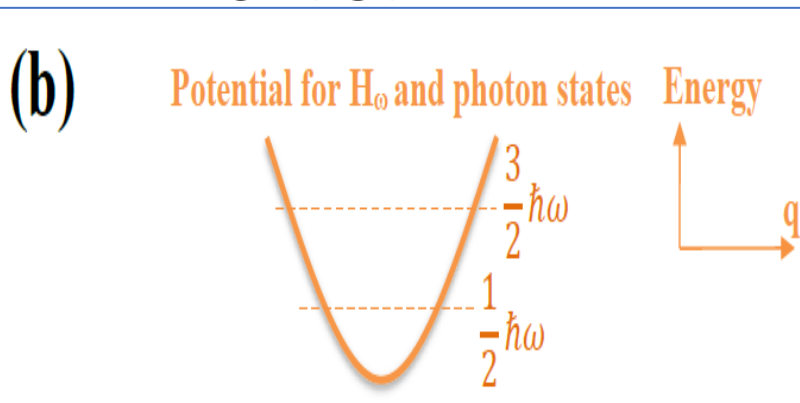
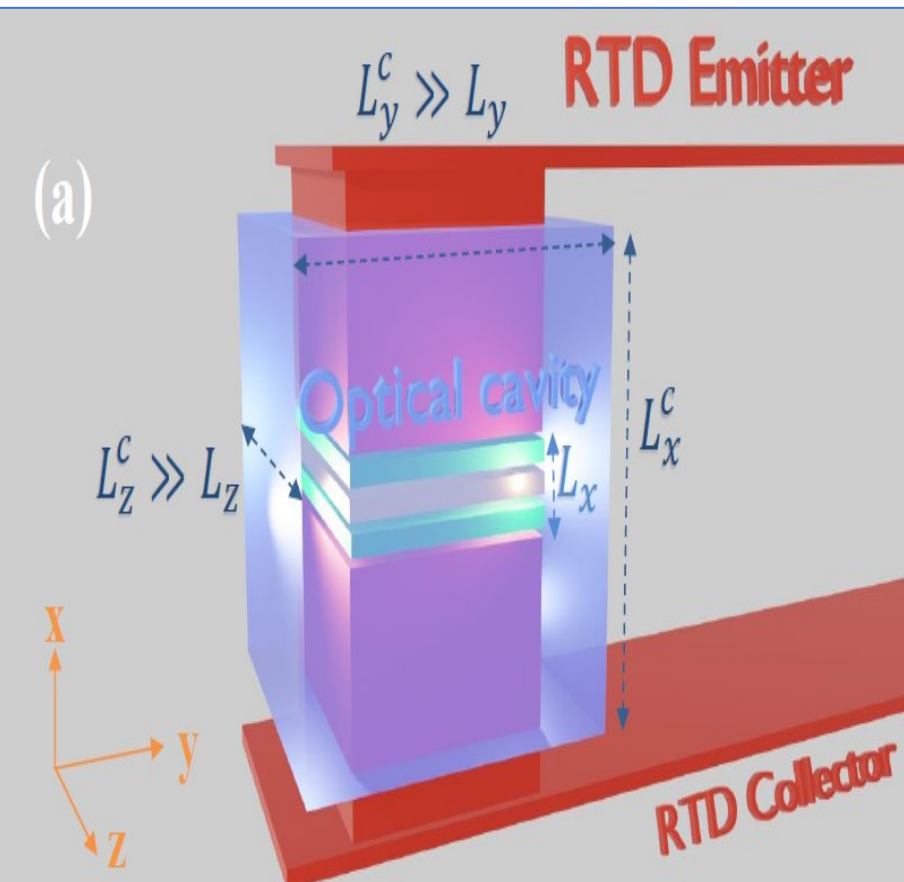


(e) **Polariton subspace ( $m = 0$ )**

$$|\psi_{\pm, m}\rangle = \frac{1}{\sqrt{2}}[|1, m\rangle \pm |0, m+1\rangle]$$

$$E_{+, m} - E_{-, m} \propto 2\sqrt{(m+1)}\hbar\omega_r$$

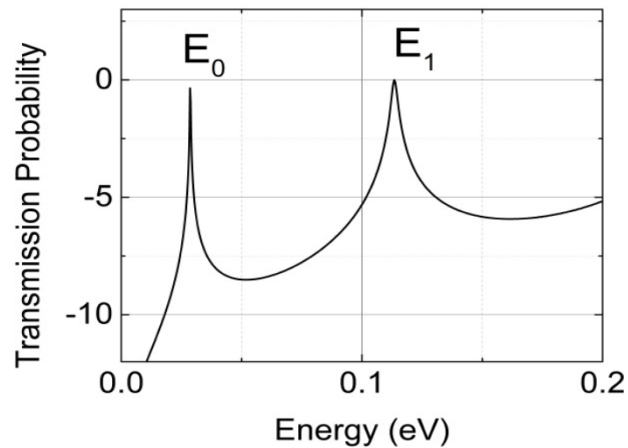
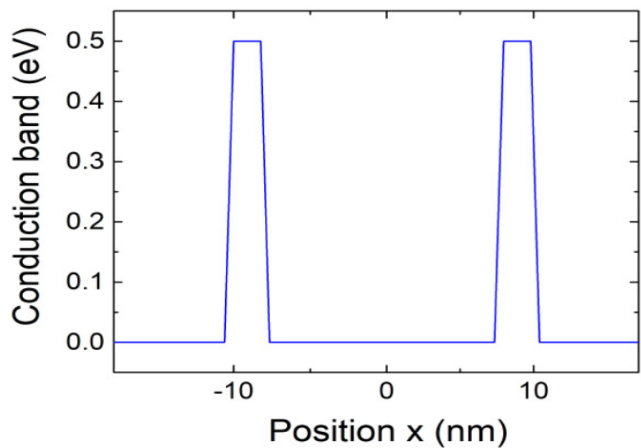
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**AlAs/InGaAs/AlAs**

$$m_e = 0.041, \quad \epsilon = 12.9, \quad (L_B, L_x, L_B) = (2, 16, 2) \text{ nm}$$

$$V_B = 500 \text{ meV}, \quad (E_0, E_1) = (28, 106) \text{ meV}$$

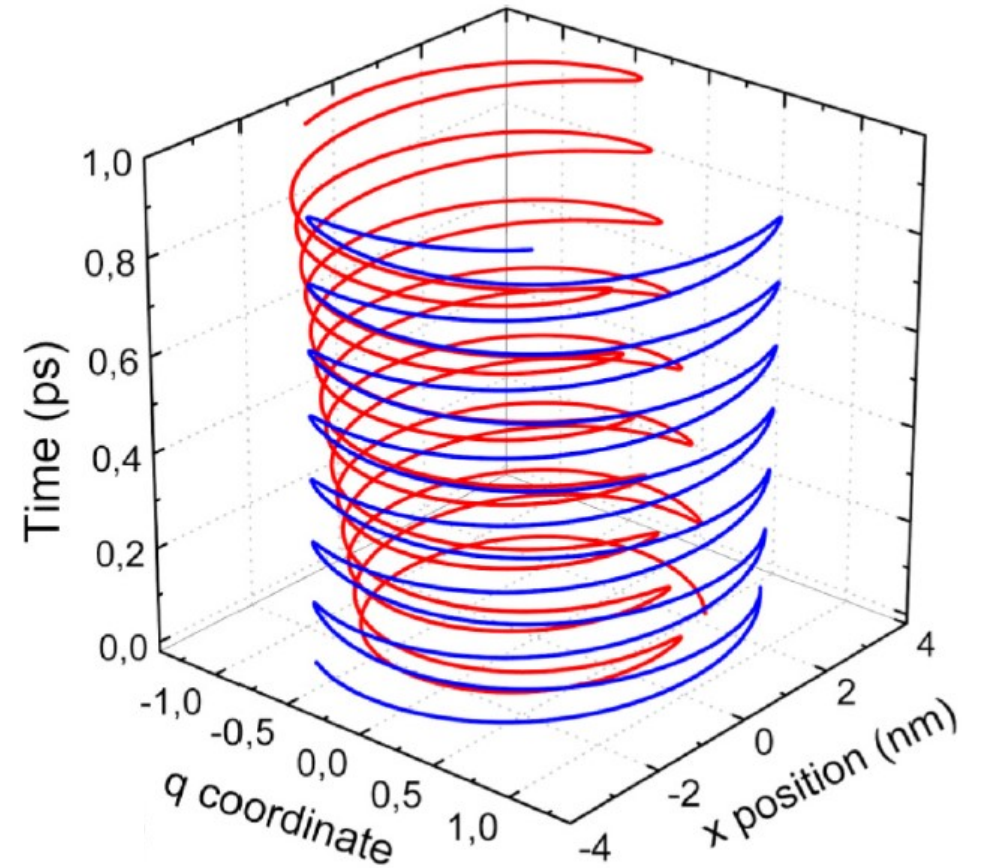
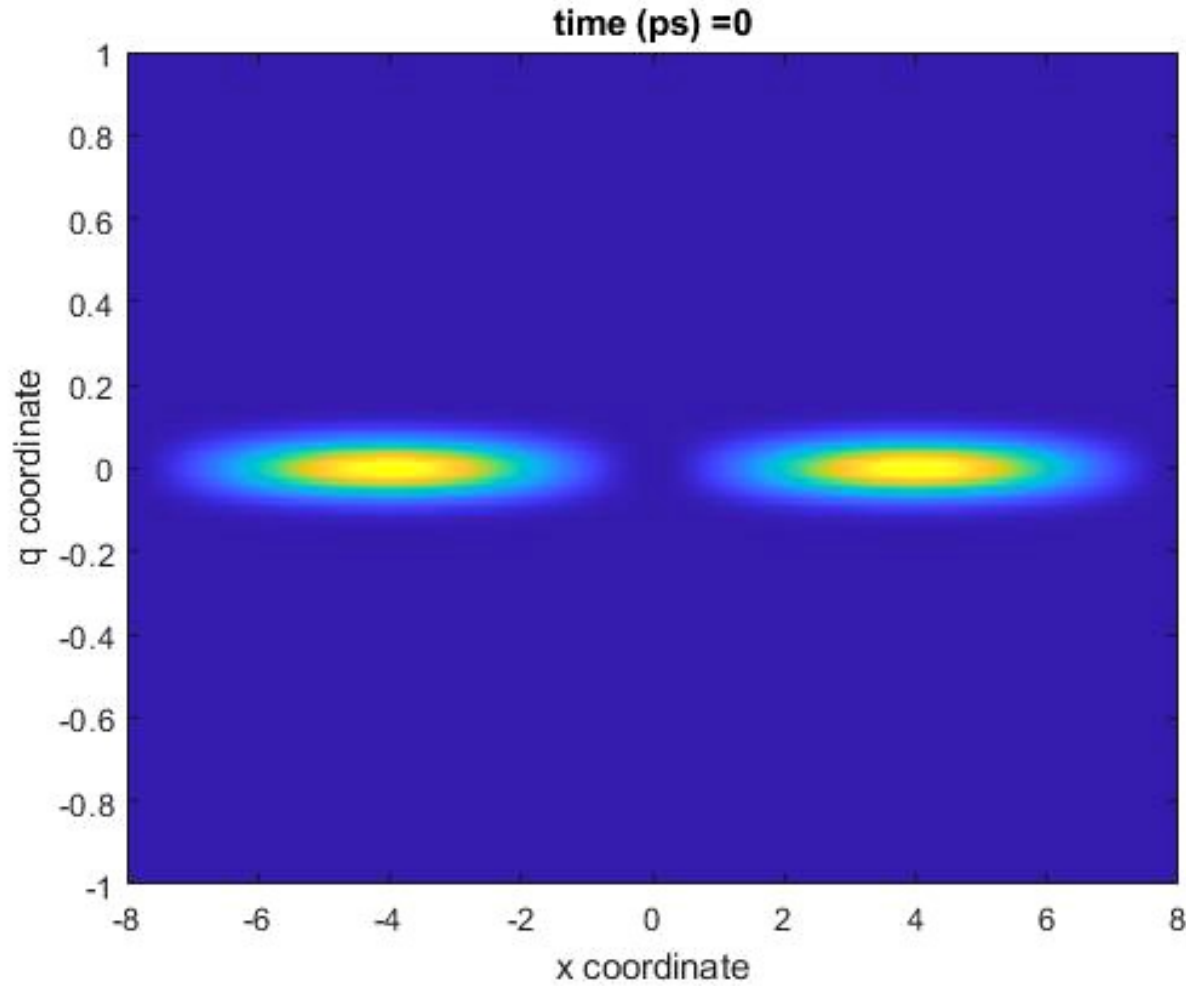
$$\frac{\omega}{2\pi} = 19 \text{ THz}, \quad L_{c,x} \cong \mu\text{m}, \quad \alpha = 1.33 \text{ meV/nm}, \quad \gamma \cong 0.4$$

$$x_{\text{left}} = 520 \text{ nm}, \quad \text{simulation box} = 2 \mu\text{m}$$

[  $\lambda_{\text{cavity}} \gg W_{\text{device}}$  ]

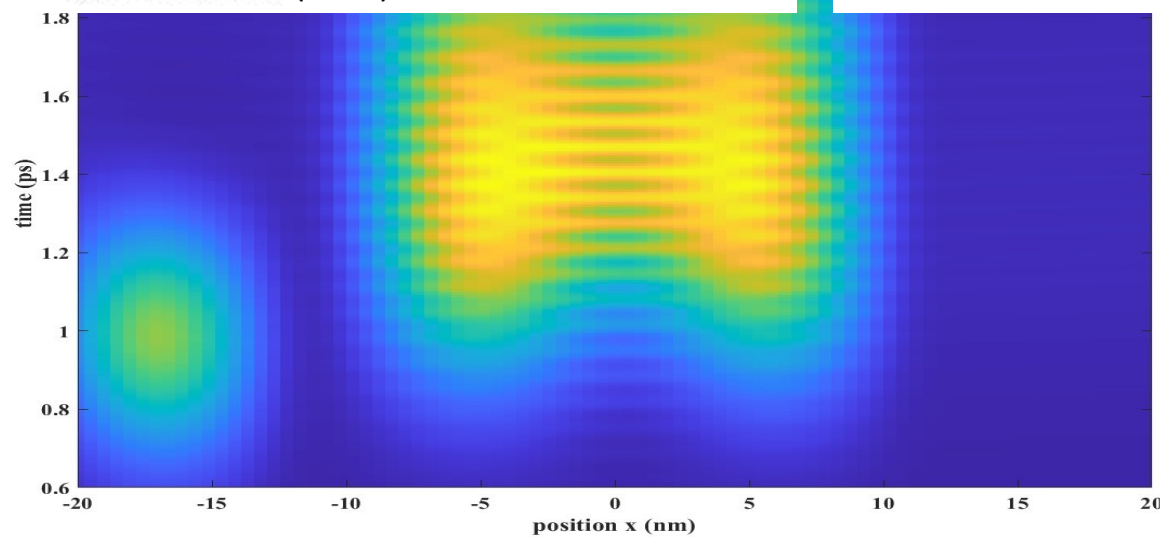
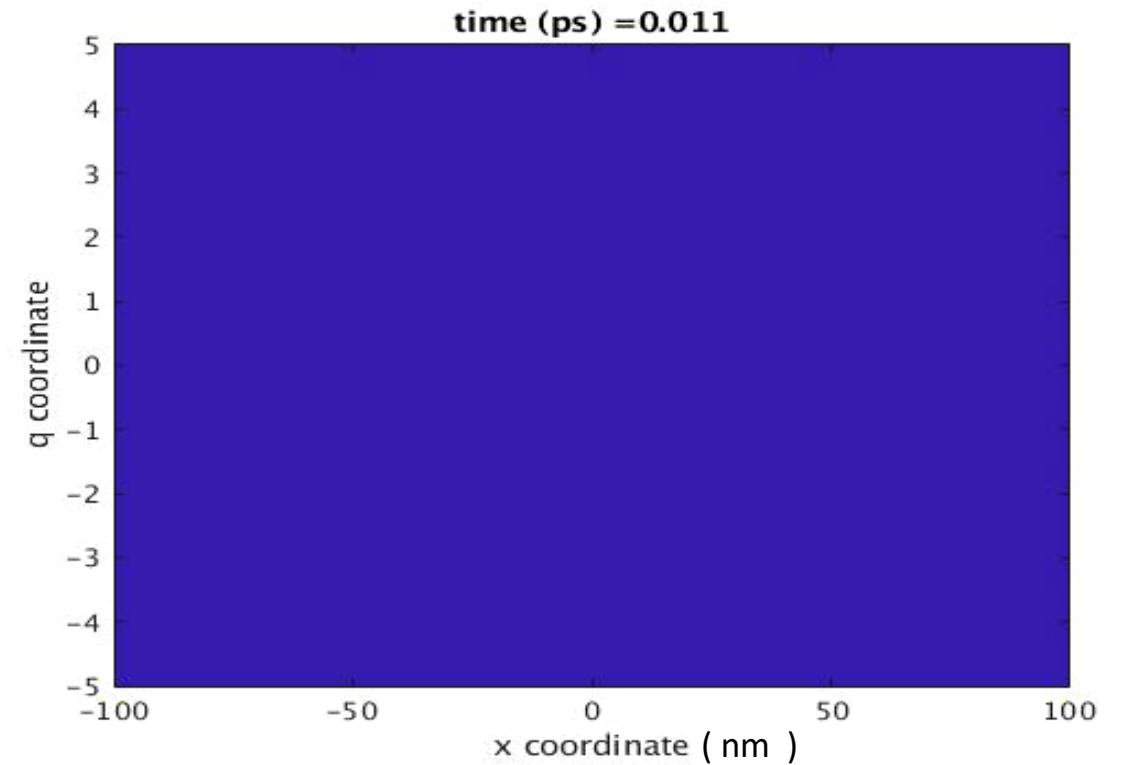
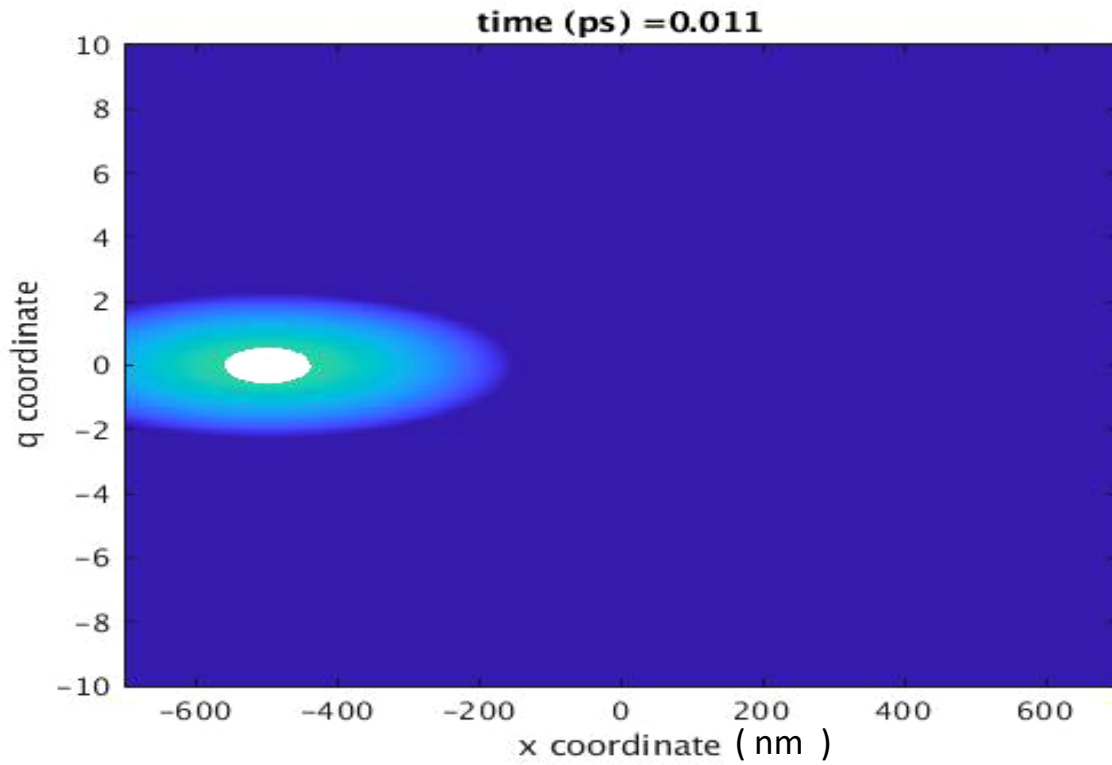
Closed system scenario (infinite well).

Jaynes-Cummings-like RWA solution from initial  $|1,0\rangle$  state (double peak in  $x$ , single peak in  $q$ ).



OK, but JC model not suitable for transport.





OK, but “exact” model undoable for more electrons and/or more modes.

# Born-Huang-like scheme

- Born-Huang : expand over well-known photon states  $\phi(q)$ , with wavepackets  $\Phi(x,t)$ .
- Previous 2D to 1D. More degrees of freedom via conditional wavefunctions.

$$\psi(x, q, t) = \sum_m^{N_\omega} \Phi_m(x, t) \phi_m^{(\omega)}(q)$$

(1D propagation only for  $\downarrow$  electron degree  $x$ )

$$i\hbar \frac{\partial}{\partial t} \Phi_n(x, t) = [H_{xq,e}^{(D)} + \hbar\omega(n + 1/2)] \Phi_n(x, t) + \alpha x [\sqrt{n+1} \Phi_{n+1}(x, t) + \sqrt{n} \Phi_{n-1}(x, t)]$$

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(if only 2  $\downarrow$  lowest levels)

$$\psi(x, q, t) = \Phi_0(x, t) \phi_0^{(\omega)}(q) + \Phi_1(x, t) \phi_1^{(\omega)}(q)$$

$$i\hbar \frac{\partial}{\partial t} \Phi_0(x, t) = \left[ H_{xq,e}^{(D)} + \frac{\hbar\omega}{2} \right] \Phi_0(x, t) + \alpha x \Phi_1(x, t),$$

$$i\hbar \frac{\partial}{\partial t} \Phi_1(x, t) = \left[ H_{xq,e}^{(D)} + \frac{3\hbar\omega}{2} \right] \Phi_1(x, t) + \alpha x \Phi_0(x, t)$$

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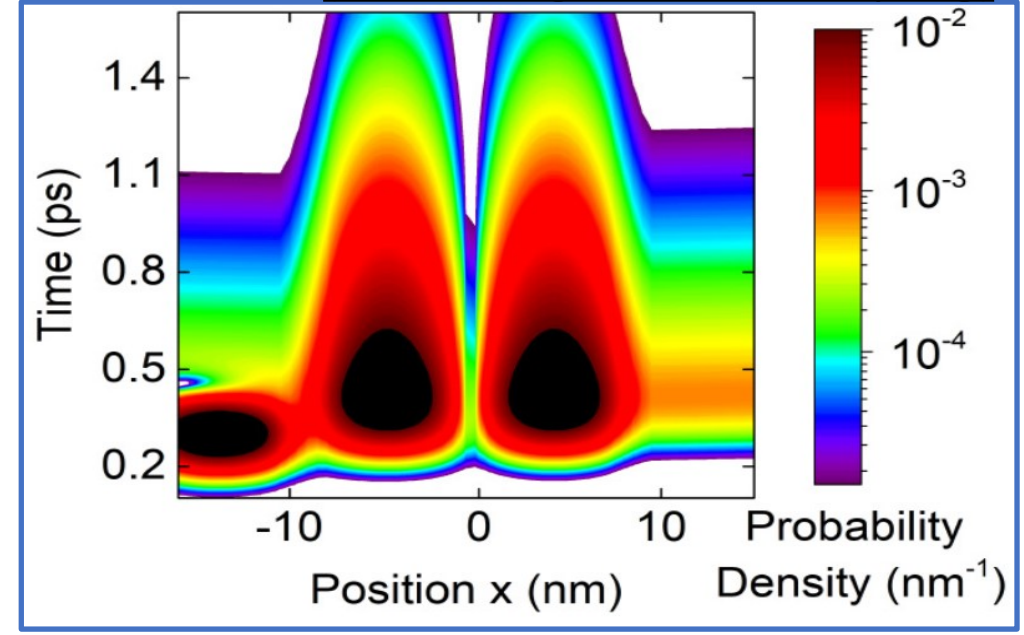
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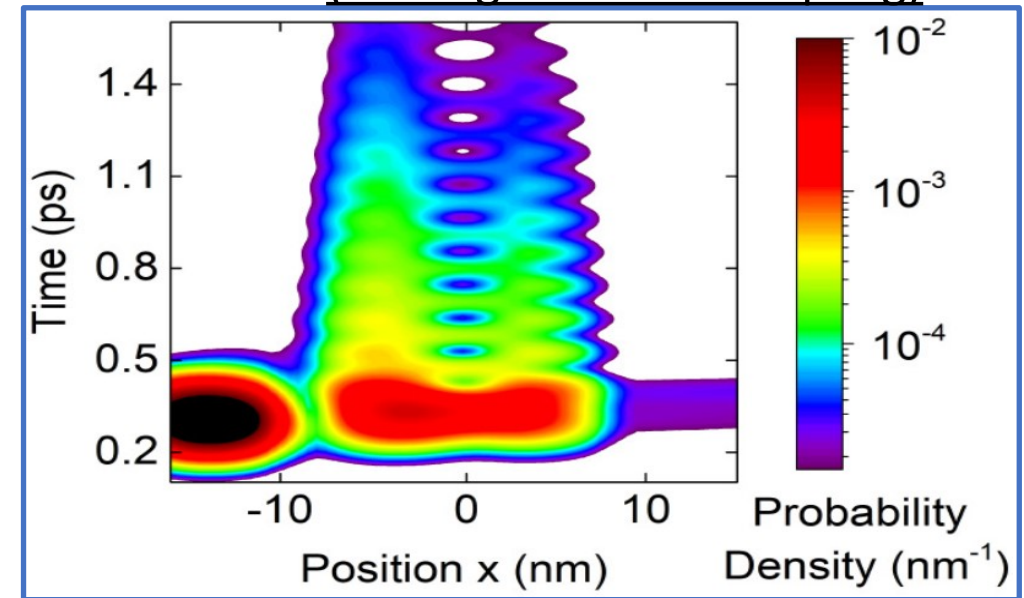
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$$i\hbar \frac{\partial}{\partial t} \Phi_1(x, t) = \left[ H_{xq,e}^{(D)} + \frac{3\hbar\omega}{2} \right] \Phi_1(x, t) + \alpha x \Phi_0(x, t)$$

(without light-matter coupling)



(with light-matter coupling)



# Displacement current

particle plus displacement current ( external  $f$  )

$$\mathbf{J}(\mathbf{r}, t) = \mathbf{J}_c(\mathbf{r}, t) + \epsilon_0 \frac{\partial \mathbf{E}_{\parallel}(\mathbf{r}, t)}{\partial t} + \epsilon_0 \frac{\partial \mathbf{E}_{\perp}(\mathbf{r}, t)}{\partial t}$$

(Particle)                      (displacement )

## Ramo-Shockley-Pellegrini Theorem

[total current from flux of distinct wavepackets (  $E, t_i, \dots$  ).  
Bohmian velocities and conditional wave functions]

$$I^{(f)}(t) = \frac{e}{L_x} \sum_{j=1}^N \mathbf{v}_j(t) \cdot \mathbf{x}$$

$$\sum_{j=1}^{N(t)} \rightarrow \Gamma \int_{-\infty}^t dt_i \int_{-L_x/2}^{L_x/2} dx \int d\mathbf{W}_q |\psi(x, \mathbf{W}_q, t; t_i, E)|^2$$

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AC / DC displacement current coefficient

$$D^{(f)}(E, t) = \frac{I^{(f)}(E, t)}{e\Gamma} \quad (= T(E) \text{ if } f=0)$$

(DC Transmission coefficient)

$$= \frac{1}{L} \int_{-L_x/2}^{L_x/2} dx \int d\mathbf{W}_q \int_{-\infty}^t dt_i J_x(x, \mathbf{W}_q, t; t_i, E)$$

## BITLESS SIMULATOR

Bohmian Interacting Transport in non-equilibrium electronic Structure

# Displacement current

particle plus displacement current ( external  $f$  )

$$\mathbf{J}(\mathbf{r}, t) = \mathbf{J}_c(\mathbf{r}, t) + \epsilon_0 \frac{\partial \mathbf{E}_{\parallel}(\mathbf{r}, t)}{\partial t} + \epsilon_0 \frac{\partial \mathbf{E}_{\perp}(\mathbf{r}, t)}{\partial t}$$

↓ (Particle)
↓ (displacement)

## Ramo-Shockley-Pellegrini Theorem

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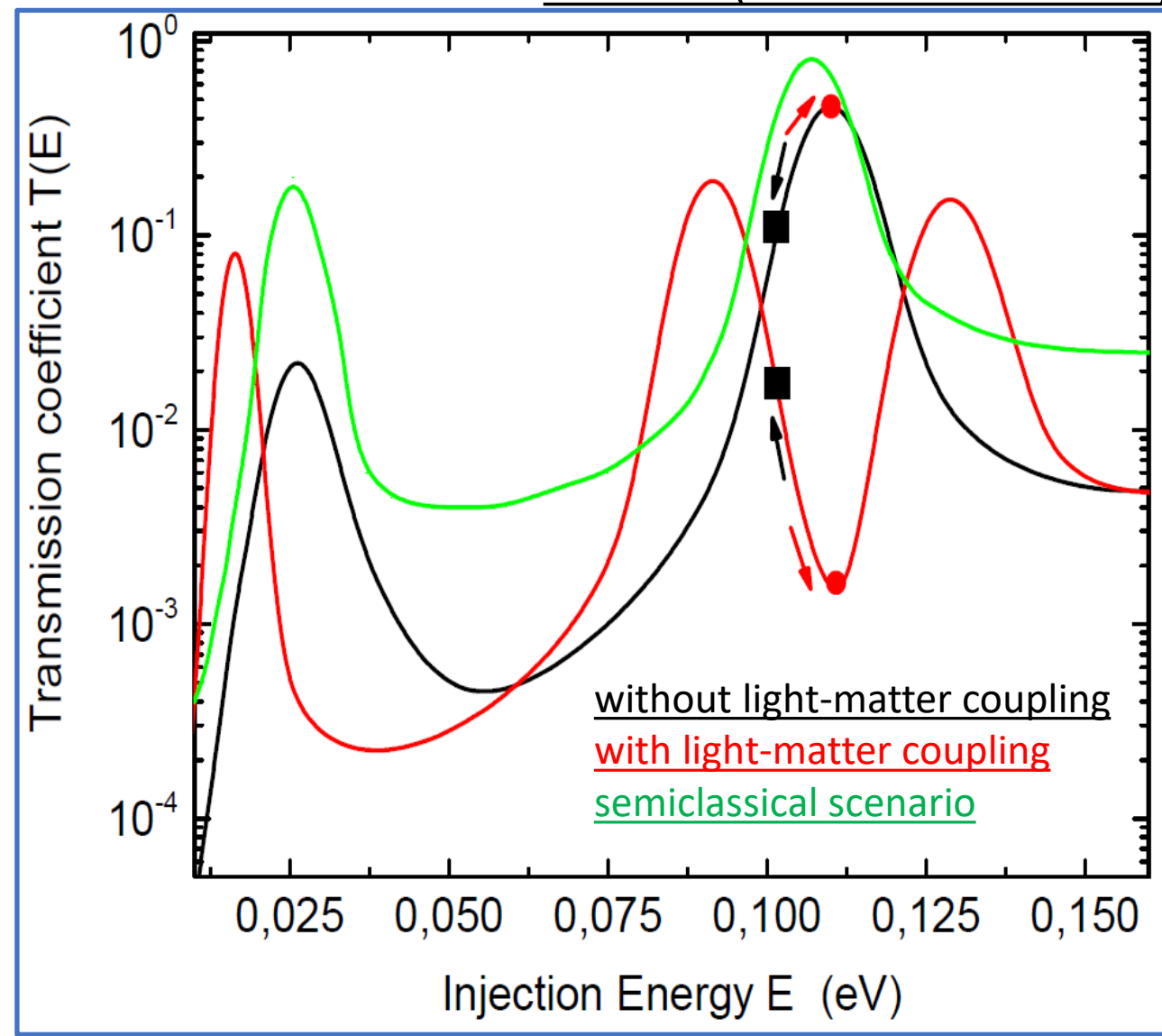
(DC Transmission coefficient)

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## BITLLES SIMULATOR

Bohmian Interacting Transport in non-equilibrium electronic Structure

DC result ( AC result elsewhere )



- polaritonic splitting of the first excited RTD state.
- ground state uncoupled.
- higher excited states coupled via other resonances.

## SUMMARY

- Polariton signature not new neither unexpected : well-known in other platforms.
- 'Old-fashion' RTD + 'modern' microcavities : unexplored path for nanodevice engineering at THz.
- Theoretical side : need of new models at the strong coupling regime.
- Experimental side : RTD-based oscillators at THz need to improve output power.
- No photonics. Still electronics : no need of NDR.

### Next steps

- Applying such models in simple structures like 'exciton polariton' (3D electron-hole-photon) or coupled QWs.
- Improving the initial approximations of these qualitative models.



THANK YOU for the attention!

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